dimensional image of the object that is indistinguishable from the original. The fact that the two-dimensional hologram reproduces the field on only half of its surface results in phase-reproduction ambiguity and ultimately in the appearance of a spurious additional image.

When three-dimensional holograms are registered, a fragment of the three-dimensional interference pattern surrounding the object is impressed into the volume of the photosensitive layer. Each surface of antinodes of this pattern is a geometric locus of points at which the phase of the object wave coincides with the phase of the source wave. Accordingly, on illumination of each such surface by source radiation, the phase of the wave reflected by this surface coincides with the phase of the object wave over the entire surface of the hologram. As a result, this hologram reproduces the exact value of the object wave field and, accordingly, a unique threedimensional image of the object appears. But a whole ensemble of antinode surfaces is recorded in the volume of the hologram. Like an interference filter, this complex structure exhibits spectral selectivity, with the result that three-dimensional holograms admit of reconstruction of the radiation with a continuous spectrum. The fact that the three-dimensional hologram reflects radiation in the same way as the object makes it possible to regard it as a kind of optical equivalent of this object. It is natural to assume that this property of the three-dimensional hologram results from the fact that its structure tends to reproduce the structure of the object. It is not possible to prove this in the general case, since the method to be used in describing an arbitrary three-dimensional object is still unclear. In order to define the general tendencies that determine the structure of a three-dimensional hologram and the relation of its structure to that of the object, the authors investigated a particular case in which a transparent phase object was registered on the hologram. It was shown as a result that the space-frequency spectrum of the threedimensional hologram equals the product of the spacefrequency spectrum of the object by a certain transfer function that depends exclusively on the parameters of the wave illuminating the object. Thus, just as in the case of formation of an image by an optical system, formation of a hologram is attended by filtration of the object's space frequencies; it can be shown that for a specified propagation direction of the radiation, the space-frequency spectra of the object and its hologram are identical, with the result that their optical properties are also identical in this case. Effects related to the limits on the volume of the registering system were then examined, and the limit transition to the case of the two-dimensional hologram was carried out. It was shown that the hologram spectrum then shows spatial frequencies that did not exist in the object spectrum. The presence of the additional frequencies in the twodimensional hologram leads to the appearance of three additional spurious images and to loss of the spectralselectivity property. On the whole, the relation between the two- and three-dimensional holograms can be described as follows. The most complete set of information on the image of the object is included in the entire limitless three-dimensional standing-wave pattern surrounding it. One of the remarkable properties of this pattern consists in the fact that each fragment of it also creates

a complete image of the object as a whole. Division of the primary pattern into fragments merely results in gradual impoverishment of the reconstructed image, which retains its integrity. For example, a plane section through such a pattern—the two-dimensional hologram—reconstructs spurious images in addition to the true image; moreover, it becomes impossible to accomplish the reconstruction with white light when the plane section is used.

M. I. D'yakonov, B. P. Zakharchenya, V. I. Perel', S. I. Safarov, and V. G. Fleisher. Orientation of Electron Spins in Semiconductors.

The phenomenon of optical orientation of atoms in gases is well known and offers a powerful tool for study of atomic processes. Kastler and his school had a major role in the development of this field. The first experiments that indicated the possibility of optical orientation of free electrons in semiconductors were also performed in France by Lampel<sup>[1]</sup> and Parsons<sup>[2]</sup>.

The present report is devoted to results obtained in this field at the A. F. Ioffe-Physico-technical Institute of the USSR Academy of Sciences. It appears to us that this trend, which is a novelty for semiconductor physics, will be found effective in the investigation of the properties of semiconductors and will also find practical applications.

In the optical-orientation method, nonequilibrium electrons are produced in the conduction band by interband absorption of circularly polarized light. The momentum M of a circularly polarized photon is transferred to the electron-hole system. In crystals with the GaAs band structure, the hole momentum relaxes rapidly, and the electron spins are found to be oriented. The selection rules indicate that in an interband transition  $\Gamma_8 \rightarrow \Gamma_6$ , three times as many electrons are ejected into a state with spin opposed to the momentum of the photon than are ejected into a state with spin of the same direction as the photon momentum. This corresponds to a degree of orientation  $P_0 = 50\%$  of the electrons at their production.

Under stationary excitation, the degree of orientation P depends on the relation between the electron lifetime  $\tau$  and the spin relaxation time  $\tau_s$ :

A magnetic field perpendicular to the direction of the exciting beam of light disturbs the orientation (Hanle effect):

$$P(H) = P \frac{1}{1 + (\mu_0 g H T_s/h)^2}, \qquad (2)$$

where P(H) is the degree of orientation in a magnetic field H,  $\mu_0$  is the Bohr magneton, g is the g factor, h is Planck's constant, and the time  $T_s$  is defined in terms of  $\tau$  and  $\tau_s$  as follows:

$$T_{s}^{-1} = \tau^{-1} - \tau_{s}^{-1}. \tag{3}$$

The presence of spin orientation can be registered from the polarization of the recombination emission.

For the  $\Gamma_6 \rightarrow \Gamma_8$  transition, the degree of polarization  $\rho$  of the radiation is 0.5P (for observation with or against the direction of the spin). Then the maximum degree of polarization is 25%. According to<sup>[1]</sup>, it is reached at  $\tau_s \gg \tau$ .

Study of  $\rho$  as a function of the energy  $E_{h\nu}$  of the photon of circularly polarized exciting light makes it possi-

ble to determine the spin-orbital splitting  $\Delta$  of the valence band. Figure 1 shows experimental (1) and theoretical (2)  $\rho(E_{h\nu})$  curves for a GaAs crystal. Curve 2 was computed without allowance for spin relaxation and corresponds to the case with  $\tau_S \gg \tau^{[3]}$ . The knee on the theoretical curve at  $E_{h\nu} = 1.84 \text{ eV}$  results from inclusion of the band  ${}^2\Gamma_7$ , which is shifted by an amount  $\Delta = 0.33 \text{ eV}$  relative to  ${}^4\Gamma_8$ , in the optical transitions. Since the  ${}^2\Gamma_7 \rightarrow {}^2\Gamma_6$  transitions create a preferential orientation of the electron spins in the direction of M, the resultant value of P diminishes with increasing  $E_{h\nu}$ . The experimentally observed value of  $\rho$  diminishes accordingly. Over the entire range of variation of  $E_{h\nu}$ , we have  $\rho_{\text{theor}} > \rho_{\text{exp}}$ , which is explained by the influence of spin relaxation ( $\tau_S$  is comparable with  $\tau$ )<sup>[4]</sup>. The similarity of the theoretical and experimental  $\rho(E_{h\nu})$  curves indicates preservation of the spin orientation on energy relaxation in a broad range of  $E_{h\nu}$ .

Circular polarization is sensitive to the surface properties of semiconductors. On measurements of depolarization in an external magnetic field in the case of GaAs crystals, the time  $T_s$  for which the spin orientation exists is found to depend on  $E_{h\nu}^{\Gamma^5}$ . This dependence is explained by the difference between the spin-relaxation times on the surface and in the bulk of the semiconductor.

As is seen from (1) and (2), measurement of the stationary degree of luminescence polarization and its depolarization in a transverse magnetic field makes possible separate determinations of the lifetime and spin-relaxation time of a nonequilibrium electron. Figure 2 presents the results of such measurements in the temperature range 77–300°K for a Ga<sub>x</sub>Al<sub>1-x</sub>As crystal<sup>[6]</sup>. We see that the spin-relaxation time depends strongly on temperature. It satisfies approximately the relationship  $\tau_{\rm S} \sim {\rm T}^{-5/2}$ , which corresponds to the case of spin relaxation on acoustic phonons. The lifetime  $\tau \approx 10^{-10}$  sec is practically independent of temperature and, as it turned out, is governed basically by nonradiative recombination of electrons via deep-lying impurity centers.

We note that in these experiments, the very short times,  $10^{-9}-10^{-11}$  sec, are measured under stationary conditions in a procedure that does not require registration of rapidly varying processes.

In n-type crystals, the oriented electrons generated by light represent only a small fraction of the total number of carriers (n), although the rate of recombination does not depend on electron spin. Clearly, oriented carriers will in this case accumulate in the conduction band. The degree of orientation would depend on the intensity I of the exciting light<sup>[7]</sup>:

$$P = \frac{P_0}{1 + (n/I\tau_s)} \,.$$

This dependence of P on the excitation intensity was observed at  $4.2^{\circ}$ K in crystals of n-Ga<sub>0.7</sub>Al<sub>0.3</sub>As for the band due to transitions from the donor level, at which all equilibrium electrons are situated at low temperature<sup>[8]</sup>. In the same crystal, however, the degree of orientation remained unchanged for emission of an exci-



FIG. 1. Dependence of the degree  $\rho$  of circular polarization of luminescence in GaAs on the energy of the photon of circularly polarized exciting light (1-experimental curve, 2-theoretical curve).

FIG. 2. Temperature curves of lifetime  $\tau$  and spin-relaxation time  $\tau_s$  of nonequilibrium electrons in Ga<sub>0.7</sub>Al<sub>0.3</sub>As.



ton in whose formation only nonequilibrium carriers participate.

Thus, optical orientation makes it possible to create "spin-tagged" electrons in semiconductors. This offers new opportunities for study of band structure, lifetimes, recombination channels, and spin-relaxation mechanisms in semiconductors.

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