REVIEWS OF TOPICAL PROBLEMS

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### Semiconductor nanocrystalline sulfides

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Abstract. The paper presents data on phase equilibria in Cu–S, Ag–S, Zn–S, Cd–S, Hg–S, Sn–S, and Pb–S systems and generalizes experimental results on the crystal and electronic structure of twenty polymorphic phases of coarse- and nanocrystalline semiconductor sulfides of copper, silver, zinc, cadmium, mercury, tin, and lead, including information on the band gap width of the sulfides considered. For the first time, using data on the effective masses of charge carriers and dielectric constants, information on the sizes of excitons in coarse-crystalline sulfides is generalized. Allowing for the sizes of excitons, the size effects observed in the electronic (optical) properties of the above sulfides in the nanocrystalline state are considered. It is shown that a decrease in the size of sulfide nanoparticles can be accompanied by a change in the stoichiometry of sulfides as well as their lattice properties.

**Keywords:** nanocrystalline sulfides, crystal structure, band gap, exciton size, size effects

### 1. Introduction

Among binary semiconductor compounds, an important place is occupied by such compounds of metals with sulfur as sulfides CuS, Cu<sub>2</sub>S, Ag<sub>2</sub>S, ZnS, CdS, HgS, SnS, PbS. These sulfides are used in various fields of modern technology. Devices for the conversion and storage of energy (including fuel cells, photoelectrochemical cells for obtaining hydrogen from water, direct converters of solar energy into electricity, and high-capacity batteries and energy storage devices) play an important role in the development of sustainable technologies, solving energy and environmental problems. Sulfides are widely used in micro- and optoelectronics for manufactur-

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Received 1 February 2024, revised 3 June 2024 Uspekhi Fizicheskikh Nauk 195 (3) 223 – 244 (2025) Translated by V L Derbov ing elements of various optical instruments and devices, and in biology and medicine. They are used to create infrared sensors and photodetectors, near and medium infrared lasers, resistance switches, nonvolatile memory devices, ultrasound detectors, thermoelectric converters, and optical switches. These sulfides are used as phosphors for fluorescent devices, light-emitting diodes, and liquid crystal displays, and as photocatalysts, biosensors, and antibacterial drugs. Due to increased interest, the synthesis, structure, and properties of coarse- and nanocrystalline sulfides PbS, ZnS, CdS, Ag<sub>2</sub>S, CuS, including colloidal quantum dots, have been analyzed in recent reviews and monographs [1-25]. Coarse-crystalline sulfides of copper and silver are described in monograph [26]; many original publications are devoted to sulfides of copper, mercury, and tin. Particularly noteworthy are the very informative reviews [1, 6], which are rich in references and cover colloidal nanoparticles of not only sulfides, but also selenides and tellurides of various metals, as well as heteronanostructures.

Unfortunately, intensive studies of the synthesis and properties of nanostructured sulfides with different morphologies are usually not accompanied by a detailed study of the crystal structure and do not provide a comprehensive understanding of its possible modification. Conclusions about the structure of nanostructured sulfides are made by visually comparing experimental X-ray diffraction spectra with standard data for the corresponding coarse-crystalline sulfides and comparing the estimated unit cell parameters with the cell parameters of the coarse-crystalline sulfide. However, much data on the crystal structure of coarsecrystalline sulfides was obtained back in the 1950s-1970s and even earlier using samples of natural minerals. Synthesized sulfides are usually purer and do not contain many impurities present in natural samples. This is one of the reasons for the difference between the crystal structures of natural and synthesized sulfides.

The crystal structures of most sulfide phases are quite complex. Therefore, in many experimental studies of the synthesis and properties of sulfide phases, especially nanocrystalline ones, the determination of the crystal structure of the synthesized sulfide is either completely absent [27–30] or is carried out by comparing the experimental results [31–44] of

X-ray diffraction or transmission electron microscopy (TEM) with outdated diffraction data [45-49], presented in JCPDS cards 14-0072 and 65-2356 for Ag<sub>2</sub>S, 19-0798 for HgS, 26-1116 for Cu<sub>2</sub>S, 06-0464 for CuS, etc. Thus, in Refs [31, 33, 50, 51], without a full-profile refinement of the structure, it is assumed that the Ag<sub>2</sub>S sulfide, synthesized in the form of a film, nanocrystalline powder, or nanoparticles, has the crystal structure of natural acanthite. In the recent paper [52], the structure of Ag<sub>2</sub>S quantum dots with an average size of 4.5 nm without a full-profile analysis is described as an outdated monoclinic (space group (sp. gr.)  $P2_1/n$ ) structure of stoichiometric acanthite. The authors of Refs [53–55], devoted to the synthesis of Ag<sub>2</sub>S nanoparticles and quantum dots, present X-ray diffraction data without discussing the structure of the synthesized nanocrystalline silver sulfide at all. In Ref. [56], it is assumed that the synthesized silver sulfide film Ag<sub>2</sub>S has an argentite structure. However, the crystal structure of synthetic sulfide phases, especially nanocrystalline ones, can have noticeable differences from the structure of natural minerals in terms of the unit cell parameters and even in the arrangement of atoms in other crystallographic positions. This is evidenced, in particular, by the detection of reflections not related to the acanthite-type structure in the diffraction pattern of Ag<sub>2</sub>S nanoparticles [50] and the difference in the diffraction reflections in the X-ray patterns of nanostructured CdS from the diffraction reflections of coarse-crystalline cadmium sulfide phases [57-59].

Note that much published experimental diffraction data on sulfide phases is generally not suitable for quantitative determination and refinement of the structure, since they were taken in a narrow range of angles  $2\theta$  (usually  $20^{\circ}-60^{\circ}$ ) and without sufficient signal accumulation.

Clarification of the crystal structure of nanocrystalline sulfides is necessary, since only in this way can one detect changes in nonstoichiometric parameters caused by a decrease in the size of sulfide particles. To clarify the structure, one must know the initial values of the current coordinates (xyz) of the compound's atoms. In the original articles, there is usually no information on the atomic coordinates. Such information is available in the Inorganic Crystal Structure Database (ICSD), FIZ Karlsruhe (Germany), but there is no open access to it. Keeping in mind these difficulties, this paper presents information on the atomic coordinates of the sulfides under consideration.

Note that not all substances with particle sizes in the nanometer range from 1 to 100 nm are nanomaterials. In the full sense, nanomaterials are substances in which size effects are manifested, and their properties differ significantly from those of coarse-crystalline substances. In semiconductor compounds, the ratio of particle sizes to exciton size determines whether size effects will be observed in the properties of these substances. In other words, when the size of crystalline particles decreases to sizes comparable to the exciton size, the crystalline substance finds itself in a nanocrystalline state. Therefore, the review includes a brief description of the exciton as a quasiparticle and the definition of the exciton size as a function of the permittivity and effective masses of charge carriers.

# 2. Phase equilibria and phases of M-S systems with semiconductor sulfides

Phase diagrams of M-S systems (M = Cu, Ag, Zn, Cd, Hg, Sn, Pb) with semiconductor sulfides were constructed

mainly in the period of 1985–1996. Intensive studies of the synthesis and properties of nanostructured sulfides carried out during the last 20–25 years affected phase equilibria mainly in the refinement of the boundaries of the homogeneity regions of sulfides. Noticeable changes, especially related to nonstoichiometry, were discovered during careful studies of the structure of nanostructured sulfide phases

### 2.1 M-S systems of metals in IB group (M = Cu, Ag)

The phase diagram of the Cu-S system in the range from 23 to 55 at.% of S is constructed in Ref. [60]. The main phases of copper sulfide with nonstoichiometry in the copper sublattice are chalcocite  $Cu_2S$  ( $Cu_{2-x}S$ ) and hexagonal covellite CuS. Chalcocite has a low-temperature monoclinic (sp. gr.  $P2_1/c$ ) modification  $\alpha$ -Cu<sub>2-x</sub>S ( $\alpha$ -Cu<sub>1.991-2.002</sub>S), existing at temperatures below 376.5 K [61, 62]. All atoms of copper Cu and sulfur S in the unit cell of low chalcocite  $\alpha$ -Cu<sub>2-x</sub>S are in crystallographic positions 4(e), the filling degree of 4(e)positions by Cu atoms is slightly less than 1.0, and the filling degree of 4(e) positions of the nonmetallic sublattice by S atoms is 1.0. The unit cell of monoclinic chalcocite α-Cu<sub>2</sub>S includes 48 Cu<sub>2</sub>S formula units. With increasing temperature, a polymorphic phase transition of low chalcocite  $\alpha$ -Cu<sub>2-x</sub>S into high-temperature high hexagonal (sp. gr.  $P6_3/mmc$ ) chalcocite  $\beta$ -Cu<sub>2-x</sub>S occurs. The transition temperature, depending on the composition of the low chalcocite, ranges from 263 to 376 K. With increasing temperature, the homogeneity region of the high chalcocite  $\beta$ -Cu<sub>2-x</sub>S decreases and at a temperature of T = 473 K or higher; the high chalcocite has the composition  $\beta$ -Cu<sub>1.9994</sub>S. In the crystal structure of high hexagonal chalcocite  $\beta$ -Cu<sub>2-x</sub>S, Cu atoms statistically (with a probability of less than 1.0) occupy positions 2(b), 4(f), and 6(g) [63] or positions 2(b), 4(f), and 12(k) [48] (Table 1). In the low  $\alpha$ -chalcocite, the filling degree of the metallic sublattice sites with Cu atoms is almost equal to 1, whereas, in the high chalcocite  $\beta$ -Cu<sub>2-x</sub>S at a temperature above 373 K, the filling degree of the metallic sublattice sites with copper atoms is only  $\sim 0.1-0.6$  (see Table 1). There is also information about high-temperature face-centered cubic (sp. gr.  $Fm\bar{3}m$ ) chalcocite  $\gamma$ -Cu<sub>2</sub>S, which is stable at temperatures above 708-709 K. The simplest structure of γ-Cu<sub>2</sub>S may be the antifluorite-type one proposed in Ref. [64]. In this structure, the Cu atoms are located in the 8(c) positions, i.e., in the tetrahedral interstices of the sublattice of sulfur atoms occupying the 4(a) positions. Later, when studying cubic digenite  $Cu_{1.8}S$ , it was shown that, in it, two S atoms occupy the 4(a) positions, and 7.2 Cu atoms are statistically located at the 192(l) [65] or 4(b), 8(c), and 192(l)positions with occupation probabilities of  $\sim 0.25$ ,  $\sim 0.05$ , and  $\sim 0.026$  [66], respectively. In subsequent theoretical papers [67, 68], taking into account the studies [65, 66] of cubic digenite Cu<sub>1.8</sub>S, it was accepted that the unit cell of cubic (sp. gr. Fm3m) chalcocite  $\gamma$ -Cu<sub>2</sub>S is similar to the unit cell of digenite Cu<sub>1.8</sub>S and includes four formula units of Cu<sub>2</sub>S. In the unit cell of cubic chalcocite γ-Cu<sub>2</sub>S, which has a period  $a \approx 0.564 - 0.576$  nm at a temperature of  $\sim 770$  K [50], two S atoms occupy positions 4(a), while eight Cu atoms are statistically located at positions 4(b), 8(c), and 192(l) with occupation probabilities of  $\sim 0.03-0.09$ ,  $\sim 0.25-0.26$ , and  $\sim 0.030 - 0.035$ , respectively. However, the structure of cubic chalcocite  $\gamma$ -Cu<sub>2</sub>S has not been definitively established. The authors of Ref. [69] determined that the temperature of the  $\beta$ -Cu<sub>2</sub>S- $\gamma$ -Cu<sub>2</sub>S transition is 710 K.

Phase, structure type,	Lattice	Atom	Position	A	Filling		
space group	parameters, nm		and multiplicity	x/a	y/b	z/c	degree
High hexagonal chalcocite	a = 0.395	Cu1	2(b)	0	0	1/4	0.870
$\beta$ -Cu <sub>2</sub> S [63], $P6_3/mmc$ ( $D_{6h}^4$ )	c = 0.675	Cu2	<b>4</b> ( <i>f</i> )	1/3	2/3	0.568	0.345
		Cu3	6(g)	0	1/2	0	0.140
		<b>S</b> 1	2( <i>d</i> )	2/3	1/3	1/4	1.0
High hexagonal chalcocite	a = 0.3961	Cu1	2( <i>b</i> )	0	0	1/4	0.60
$\beta$ -Cu <sub>2</sub> S [48], $P6_3/mmc$ ( $D_{6h}^4$ )	c = 0.6722	Cu2	<b>4</b> ( <i>f</i> )	1/3	2/3	0.40	0.10
		Cu3	12(k)	0.2165	0.4330	0.43	0.13
		Cu4	12(k)	0.1665	0.5830	0.467	0.07
		<b>S</b> 1	2( <i>d</i> )	1/3	2/3	3/4	1.0
Hexagonal covellite	a = 0.37938	Cu1	2( <i>d</i> )	2/3	1/3	1/4	1
CuS [73], $P6_3/mmc$ ( $D_{6h}^4$ )	c = 1.6341	Cu2	4(f)	1/3	2/3	0.1073	1
		<b>S</b> 1	2(c)	1/3	2/3	1/4	1
		S2	4( <i>e</i> )	0	0	0.0634	1

Table 1. Crystal structures of high hexagonal (sp. gr. No. 194 —  $P6_3/mmc$  ( $D_{6h}^4$ )) chalcocite β-Cu<sub>2</sub>S [48, 63] and hexagonal (sp. gr. No. 194 —  $P6_3/mmc$  ( $D_{6h}^4$ )) covellite CuS [73].

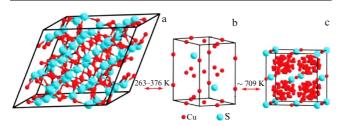
In the literature, the notations of low monoclinic and cubic chalcocite are often confused. For example, in Ref. [70], low monoclinic chalcocite is denoted as  $\gamma$ -Cu<sub>2</sub>S, and cubic chalcocite, as  $\alpha$ -Cu<sub>2</sub>S.

The unit cells of low  $\alpha$ -Cu<sub>2</sub>S, high  $\beta$ -Cu<sub>2</sub>S, and cubic  $\gamma$ -Cu<sub>2</sub>S chalcocite are shown in Fig. 1.

The low (significantly less than 1) filling degree of the metallic sublattice positions in all polymorphic chalcocite modifications means that the Cu atoms (ions) in the  $Cu_2S$  ( $Cu_{2-x}S$ ) phases are highly disordered, behave like a 'liquid,' and possess high mobility, ensuring the superionic conductivity of these phases [70–72].

The crystal structure of hexagonal (sp. gr.  $P6_3/mmc$ ) covellite CuS [73] is described in Table 1. The unit cell of covellite includes six formula units of CuS. The unit cell parameters of covellite CuS are a = 0.37917 nm, c = 1.6342 nm [74], or a = 0.3792 nm, c = 1.6344 nm [75] and are close to those given in Table 1. Unlike chalcocite, covellite CuS is a stoichiometric compound, contains 50 at.% of S, and has virtually no homogeneity region. Covellite demonstrates peritectic decomposition into digenite  $Cu_{9-x}S_5$  and sulfur S at  $\sim 780$  K.

In addition to  $\alpha$ - and  $\beta$ -chalcocite  $Cu_{2-x}S$  and covellite CuS, in the Cu-S system there are compounds such as djurleite  $Cu_{1.96}S$ , anilite  $Cu_7S_4$  ( $Cu_{1.75}S$ ), and digenite  $Cu_{9-x}S_5$ , which have polymorphic modifications, as well as several metastable phases.



**Figure 1.** Changes in crystal structure of chalcocite  $Cu_2S$  during reversible phase transformations. Shown are unit cells of (a) low monoclinic (sp. gr.  $P2_1/c$ ) chalcocite  $\alpha$ - $Cu_{2-x}S$ , (b) high hexagonal (sp. gr.  $P6_3/mmc$ ) chalcocite  $\beta$ - $Cu_{2-x}S$ , and (c) cubic chalcocite  $\gamma$ - $Cu_2S$ , constructed by the author of the review based on data from Refs [63, 73]. For chalcocite  $\gamma$ - $Cu_2S$ , positions of metallic sublattice are shown in which Cu atoms can be located with a probability of less than  $\sim 0.1$ .

The phase diagram of the Ag-S system [13, 76] includes three main polymorphic modifications of silver sulfide Ag<sub>2</sub>S (Fig. 2). The low-temperature semiconductor phase  $\alpha\text{-}Ag_2S$  with a monoclinic structure (acanthite) exists at temperatures below  $\sim450$  K. The cubic phase  $\beta\text{-}Ag_2S$  (argentite) under equilibrium conditions exists in the temperature range of 452–859 K, has a body-centered cubic (BCC) sublattice of sulfur atoms, and possesses superionic conductivity. The high-temperature cubic phase  $\gamma\text{-}Ag_2S$  with a face-centered cubic (FCC) sublattice of sulfur atoms is stable at temperatures from  $\sim860$  K to the melting point.

In the literature, the notations of monoclinic acanthite and cubic argentite are often confused. For example, in Refs [45, 77–80], the monoclinic phase (acanthite) is denoted as  $\beta$ -Ag<sub>2</sub>S, and the BCC phase (argentite) is denoted as  $\alpha$ -Ag<sub>2</sub>S.

The parameters of the crystal lattices of the phases  $\alpha$ -Ag<sub>2</sub>S,  $\beta$ -Ag<sub>2</sub>S, and  $\gamma$ -Ag<sub>2</sub>S and the coordinates of the Ag and S atoms in them are presented in Table 2.

Usually the monoclinic  $\alpha$ -Ag<sub>2</sub>S phase is considered stoichiometric, whereas the cubic  $\beta$ -Ag<sub>2± $\delta$ </sub>S and  $\gamma$ -Ag<sub>2± $\delta$ </sub>S phases with  $\delta \cong 0.002$  are nonstoichiometric and can exhibit both a slight deficit and a slight excess of silver. The homogeneity regions of the cubic allotropic forms of silver sulfide Ag<sub>2</sub>S are determined in Refs [79, 81–84].

Determination of the crystal structure in a single crystal of the natural mineral acanthite [45] showed that the unit cell of acanthite  $\alpha$ -Ag<sub>2</sub>S is primitive monoclinic and belongs to the space group  $P2_1/n$  ( $P12_1/n1$ ). Later, the authors of Ref. [85] showed that the structure of monoclinic acanthite  $\alpha$ -Ag<sub>2</sub>S is more accurately described in the space group  $P2_1/c$  ( $P12_1/c1$ ). The axes  $\mathbf{a}_{P2_1/c}$  and  $\mathbf{b}_{P2_1/c}$  of the unit cell [85] coincide in magnitude and direction with the axes  $\mathbf{a}_{P2_1/n}$  and  $\mathbf{b}_{P2_1/n}$  of the unit cell [45], and the axis  $\mathbf{c}_{P2_1/c} = (\mathbf{c}_{P2_1/n} - \mathbf{a}_{P2_1/n})$ . The crystal structure of the synthesized coarse-crystalline silver sulfide was refined in Ref. [86], according to which the low-temperature phase of silver sulfide has a monoclinic (sp. gr.  $P2_1/c$ ) structure of the  $\alpha$ -Ag<sub>2</sub>S acanthite type and does not contain vacancies, i.e., the coarse-crystalline acanthite is stoichiometric (see Table 2).

According to Ref. [87], the unit cell of argentite  $\beta$ -Ag<sub>2</sub>S has a cubic (sp. gr.  $Im\bar{3}m$  ( $I4/m\bar{3}2/m$ ) ( $O_h^9$ )) structure and includes two Ag<sub>2</sub>S formula units. Two sulfur atoms S

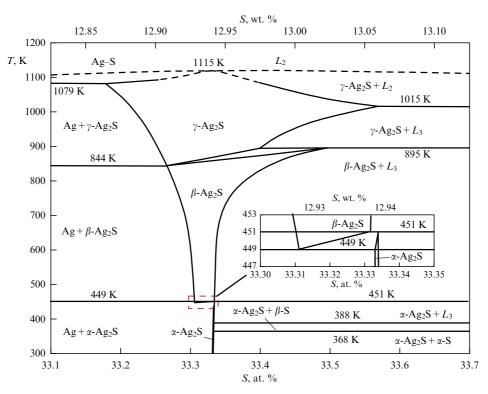


Figure 2. Phase diagram of Ag-S system in vicinity of silver sulfide  $Ag_2S$ , constructed by the author of the review based on data from Refs [13, 76]. Inset shows phase equilibria of  $\alpha$ - $Ag_2S-\beta$ - $Ag_2S$  near temperature of 450 K.

Table 2. Crystal structures of coarse-crystalline low-temperature monoclinic acanthite  $\alpha$ -Ag<sub>2</sub>S at 298 K [86], body-centered cubic argentite  $\beta$ -Ag<sub>2</sub>S at 503 K [90], and high-temperature face-centered cubic phase  $\gamma$ -Ag<sub>2</sub>S of silver sulfide at  $\sim$  923 K [89].

Phase, structure type,	Lattice	Atom	Position	A	Atomic coordinate	es	Filling
space group	parameters, nm		and multiplicity	x/a	y/b	z/c	degree
Monoclinic acanthite $\alpha$ -Ag <sub>2</sub> S, $P2_1/c$ ( $C_{2h}^5$ )	a = 0.42264 b = 0.69282 c = 0.95317 $\beta = 125.55^{\circ}$	Ag1 Ag2 S	4( <i>e</i> ) 4( <i>e</i> ) 4( <i>e</i> )	0.0715 0.7264 0.492	1.00 1.00 1.00	0.3094 0.4375 0.1321	1.00 1.00 1.00
Cubic argentite $\beta$ -Ag <sub>2</sub> S, $Im\overline{3}m$ ( $O_h^9$ )	a = 0.4874	Ag1 Ag2 S	6( <i>b</i> ) 48( <i>j</i> ) 2( <i>a</i> )	0 0 0	0.5 0.3306 0	0.5 0.4122 0	0.0978 0.0711 1.0
Cubic phase $\gamma$ -Ag <sub>2</sub> S, $Fm\bar{3}m(O_h^5)$	a = 0.62831	Ag1 Ag2 Ag3 S	8(c) 32(f) 48(i) 4(a)	0.25 0.3034 0.5 0	0.25 0.3034 0.3814 0	0.25 0.3034 0.3814 0	0.088 0.150 0.027 1

occupy crystallographic positions 2(a) and form a BCC sublattice. Four silver atoms Ag are statistically distributed with equal probability among 42 positions 6(b), 12(d), and 24(h).

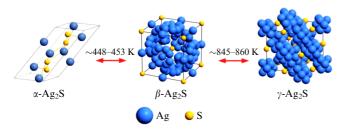
Neutron diffraction study [88] of artificial crystal of argentite  $\beta$ -Ag<sub>2</sub>S in the temperature range of 459–598 K confirmed the cubic (sp. gr.  $Im\bar{3}m$ ) structure of this phase but significantly clarified the distribution of Ag atoms. According to Ref. [88], four Ag atoms are statistically distributed over 18 positions 6(b) and 12(d). The probabilities of filling positions 6(b) and 12(d) depend on the temperature.

According to high-temperature X-ray data [89], in contrast to [88], in argentite  $\beta$ -Ag<sub>2</sub>S, four Ag atoms are statistically distributed over 54 positions 6(b) and 48(j)

with occupation probabilities of  $\sim 0.097$  and  $\sim 0.0715$ , respectively.

The latest refinements of the crystal structure of the synthesized coarse-crystalline argentite  $\beta$ -Ag<sub>2</sub>S were carried out in Ref. [90]. According to these data, in cubic (sp. gr.  $Im\bar{3}m$ ) argentite  $\beta$ -Ag<sub>2</sub>S at a temperature of  $\sim$  460 K, a deviation from stoichiometry in silver content is observed.

A model for the structure of the high-temperature cubic (sp. gr.  $Fm\bar{3}m$ ) phase in  $\gamma$ -Ag<sub>2</sub>S silver sulfide was proposed in Ref. [91]: four S atoms occupy crystallographic positions 4(a) and form an FCC sublattice, and eight Ag atoms are statistically distributed over positions 8(c) and 32(f). The authors of Ref. [89], using high-temperature X-ray data, refined model [91] by placing Ag atoms also at positions 48(i). According to Ref. [90], a noticeable silver deficiency is



**Figure 3.** Changes in crystal structure of silver sulfide during reversible phase transformations. Shown are unit cells of monoclinic (sp. gr.  $P2_1/c$ ) acanthite α-Ag<sub>2</sub>S, cubic (sp. gr.  $Im\bar{3}m$ ) argentite β-Ag<sub>2</sub>S, and cubic (sp. gr.  $Fm\bar{3}m$ ) phase γ-Ag<sub>2</sub>S. In unit cells of β-Ag<sub>2</sub>S and γ-Ag<sub>2</sub>S, positions of metallic sublattice are marked in which Ag atoms can be located with a probability of less than  $\sim 0.1$ . (Reproduced from [92] with permission from Springer.)

observed in the cubic  $\gamma$ -phase, corresponding to nonstoichiometric sulfide Ag<sub>1.7</sub>S (see Table 2).

The unit cells of monoclinic acanthite  $\alpha$ -Ag<sub>2</sub>S, BCC argentite  $\beta$ -Ag<sub>2</sub>S, and high-temperature FCC phase  $\gamma$ -Ag<sub>2</sub>S are shown in Fig. 3.

The presence of vacancies in the metallic sublattice of nanocrystalline silver sulfide was experimentally established by one of the methods of electron-positron annihilation that implies measuring the lifetime of positrons [93].

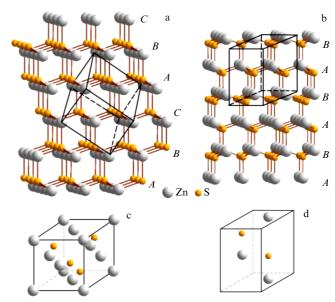
Low degrees of filling the positions of the metallic sublattice of cubic phases  $\beta$ -Ag<sub>2</sub>S and  $\gamma$ -Ag<sub>2</sub>S mean, as in the case of copper sulfides Cu<sub>2-x</sub>S, that atoms (ions) of silver in phases  $\beta$ -Ag<sub>2</sub>S and  $\gamma$ -Ag<sub>2</sub>S are strongly disordered. Indeed, the number of Ag atoms in cubic phases  $\beta$ -Ag<sub>2</sub>S and  $\gamma$ -Ag<sub>2</sub>S is much less than the number of sites in the metallic sublattice; therefore, significant positional disorder in the distribution of Ag and a huge (more than 92%) concentration of vacant sites facilitate jumps of silver cations and provide superionic conductivity of these phases. In the general case, the metallic sublattice of  $\beta$ -Ag<sub>2</sub>S argentite can be considered an anisotropic strongly interacting Coulomb liquid of Ag<sup>+</sup> cations which diffuse under the action of an effective potential of BCC anionic sulfur lattice.

In addition, in cubic argentite, the possible distances between silver atoms are too small for the 6(b) and 48(j) positions to be occupied by Ag atoms with a probability equal to unity. Therefore, the degrees of filling the 6(b) and 48(j) positions by Ag atoms (i.e., the probability of detecting Ag atoms in the 6(b) and 48(j) positions) are very small (less than 0.1: see Table 2). Physically, this means that, in the cubic argentite lattice, four silver atoms are in continuous motion over 54 possible crystallographic positions. It is precisely this continuous motion of the Ag<sup>+</sup> cations that ensures the stability of the cubic argentite crystal lattice and its superionic conductivity. The diffusion of silver atoms in argentite occurs via a vacancy mechanism, when an Ag atom (ion) jumps to a neighboring unoccupied site.

## 2.2 M-S systems of metals in IIB group (M = Zn, Cd, Hg)

The only compound of the Zn-S system is zinc sulfide, which contains 50 at.% of S, exists in two polymorphic modifications, and has a melting point of  $\sim 1991$  K [94].

The low-temperature cubic (sp. gr.  $F\overline{4}3m$  ( $T_d^2$ )) modification of  $\alpha$ -ZnS has the cubic structure of zinc blende, or sphalerite, ZnS (type B3) and is stable at temperatures below 1290 K. At 1293 K, the low-temperature cubic zinc sulfide



**Figure 4.** Sequences of alternating close-packed layers of Zn and S atoms for (a)  $\alpha$ -ZnS with B3 structure and (b)  $\beta$ -ZnS with B4 structure with contours of unit cells shown. Unit cells of zinc sulfides: (c) low-temperature cubic (sp. gr.  $F\overline{4}3m$ )  $\alpha$ -ZnS (B3 structure (zinc blende or sphalerite)), (d) high-temperature hexagonal (sp. gr.  $P6_3mc$ )  $\beta$ -ZnS (B4-type structure (wurtzite)). (Figure constructed by the author of the review based on data from [46, 47].)

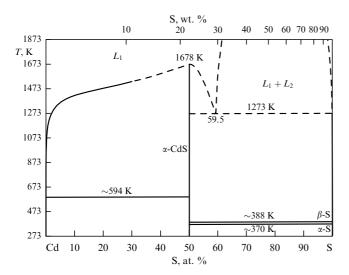
transforms into the high-temperature hexagonal (sp. gr.  $P6_3mc$  ( $C_{6v}^4$ )) modification of  $\beta$ -ZnS with a wurtzite structure (type B4) [94], which retains semiconductor properties.

At a temperature of 300 K, cubic  $\alpha$ -ZnS with a sphalerite structure has a lattice period of a=0.54109 nm [46]. According to X-ray data, the unit cell of hexagonal wurtzite  $\beta$ -ZnS has parameters a=0.38230 and c=0.62565 nm [47], while, according to neutron diffraction data [95], its parameters are somewhat different. There is also information [47, 96–98] on the face-centered cubic (sp. gr.  $Fm\bar{3}m$ ) phase of  $\gamma$ -ZnS, formed at a temperature of  $\sim 1000$  K and a pressure of  $\sim 27-35$  GPa.

Low-temperature cubic  $\alpha$ -ZnS and high-temperature hexagonal  $\beta$ -ZnS modifications of coarse-crystalline zinc sulfide differ in the sequence of alternating close-packed layers of atoms (ions) of different types, displaced relative to each other.

The B3 structure of zinc sulfide  $\alpha$ -ZnS (zinc blende or sphalerite) is a cubic closest packing (Fig. 4a), in which the close-packed layers are located perpendicular to the  $[111]_{B3}$  direction (or equivalent directions). The B4 structure of zinc sulfide  $\beta$ -ZnS (wurtzite type) has a hexagonal close packing, in which the close-packed layers are located perpendicular to the z-axis, the  $[001]_{B4}$  direction (Fig. 4b). In the ideal wurtzite-type structure, the lattice basis contains two metal atoms in the 2(b) positions with coordinates  $(1/3\ 2/3\ 0)$  and  $(2/3\ 1/3\ 1/2)$  and two nonmetal atoms in the 2(b) positions with coordinates  $(1/3\ 2/3\ 3/8)$  and  $(2/3\ 1/3\ 7/8)$ . In the real  $\beta$ -ZnS structure, the sulfur atoms are slightly shifted along the z coordinate. The unit cells of cubic  $\alpha$ -ZnS and hexagonal  $\beta$ -ZnS zinc sulfides are shown in Fig. 4c and 4d, respectively.

In Ref. [99], a nanocrystalline ZnS powder with a particle size of  $\sim 5$  nm was obtained. According to [99], the ZnS nanopowder has the same disordered hexagonal structure with random (nonperiodic) alternation of close-packed atomic planes as that previously discovered in nanocrystal-



**Figure 5.** Phase diagram of Cd-S system. (Figure constructed by the author of the review based on data from [13, 101].)

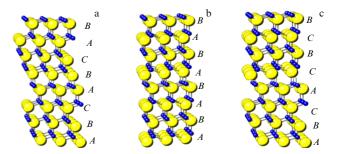
line cadmium sulfide CdS [100]. The periods of the unit cell of the ZnS nanopowder with an average hexagonal lattice are a=0.216 nm and c=0.306 nm. In Ref. [99], there is no information on the refinement of the structure of the ZnS nanopowder; therefore, its results on the structure, obtained by analogy with the previous study [100], are not entirely reliable.

The cubic sphalerite type and hexagonal wurtzite type crystal structures are typical not only of zinc sulfide, but also of cadmium and mercury sulfides, as well as of a number of selenides, arsenides, and tellurides.

Cadmium sulfide CuS is the only compound existing in the Cd-S system (Fig. 5). Cadmium sulfide contains 50 at.% of S and has a melting point of 1678 K [13, 101]. According to Ref. [102], the melting point of CdS at a pressure of 10.5 atm is 1748  $\pm$  15 K. At atmospheric pressure, sublimation of CdS begins at 1253 K. Coarse-crystalline cadmium sulfide has a low-temperature cubic (sp. gr.  $F\bar{4}3m$ )  $\beta$ -CdS and a high-temperature hexagonal (sp. gr.  $P6_3mc$ )  $\alpha$ -CdS modification, identified as zinc blende (sphalerite) structures of ZnS (type B3) and wurtzite ZnS (type B4), respectively [103].

The unit cell parameters of cubic  $\beta$ -CdS and hexagonal  $\alpha$ -CdS are presented in [104, 105], respectively. At a pressure of 27 kbar, a phase transition from the hexagonal (sp. gr.  $P6_3mc$ ) structure B4 to the cubic (sp. gr.  $Fm\bar{3}m$ ) structure B1 is observed in CdS, while cadmium sulfide retains its semiconductor properties [106].

Experimental studies of CdS films with thicknesses from 6 to 70 nm, synthesized using various methods [107–109], nanoparticles [110, 111], and complex forms of nanostructured CdS, indicate that their structures do not correspond to those of coarse-crystalline CdS wurtzite or sphalerite modifications. The authors of Refs [58, 100] found that CdS nanoparticles have a specific disordered hexagonal structure with random (nonperiodic) alternation of close-packed atomic planes. The authors of Ref. [57] analyzed the structure of nanocrystalline sulfides, which in the normal state have *B*3 and *B*4 structures. They showed that, in sulfide nanoparticles with a small number of closely packed atomic planes, the principle of a regular sequence of packings is not observed and, consequently, there is no crystalline periodicity in them [57]. This means that, in nanosized crystals, a



**Figure 6.** Alternation of close-packed planes in ordered and disordered phases of cadmium sulfide CdS: (a) cubic sphalerite *B*4 structure; (b) hexagonal wurtzite *B*3 structure; (c) disordered structure. (Reproduced from [57] with permission of JUCr Journals.)

disordered structure is more important than a periodic arrangement of packing layers.

The authors of Ref. [57] considered the nonperiodic structure of sulfide nanoparticles using cadmium sulfide CdS as an example. The explanation of the nanostructured cadmium sulfide CdS structure is based on the principle of closest packing, common to B3 and B4 structures, since these structures contain alternating close-packed planes consisting of either cadmium or sulfur atoms. The superposition of the planes is carried out in such a way that all cadmium atoms are in a tetrahedral environment of sulfur atoms, and all sulfur atoms are in a tetrahedral environment of cadmium atoms. The difference among the B3, B4, and polytype structures consists only in the sequence of alternating close-packed planes. Thus, in a cubic structure of type B4, the closest packing ABC... is realized, in a hexagonal structure of type B3, the closest packing AB... is realized, and in a disordered CdS structure, the planes alternate randomly (Fig. 6).

To calculate the positions of the peaks in the X-ray diffraction pattern of such a disordered structure, the authors of Refs [57–59, 100] examined its average crystal lattice. This lattice has hexagonal (sp. gr. P6) symmetry and is described by a unit cell with parameters  $a = a_0/\sqrt{3} = 0.238$  nm and c = 0.337 nm ( $a_0$  is the distance between like atoms in a plane, c is the distance between the nearest closepacked planes of cadmium or sulfur in an ordered CuS crystal). The unit cell of disordered CdS contains a Cd atom with coordinates (000) and an S atom with coordinates (000) and an S atom with coordinates (100) (1) (100) (

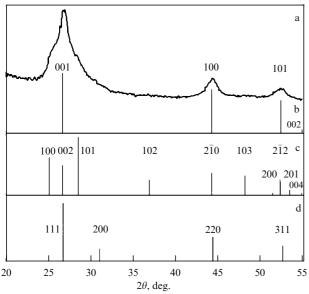
**Table 3.** Model hexagonal (sp. gr. no. 168 - P6 ( $C_6^1$ )) disordered close-packed structure of CdS nanoparticles with a size of 3–9 nm with 'average' lattice at 298 K [13, 59]; a = 0.236 nm, c = 0.334 nm.

Atom	Position	Α	Atomic coordinates			
	and multiplicity	x/a	y/a	z/c	degree	
Cd	1(a)	0	0	0	1/3	
S	1(a)	0	0	$1/\sqrt{24}\approx 0.204$	1/3	

In Fig. 7, the position of the peaks in the line spectrum from the disordered structure of cadmium sulfide with the *P6* space group is compared with the experimental spectrum (Fig. 7a) of nanostructured cadmium sulfide obtained in Refs [58, 59, 100]. The experimental spectrum has features characteristic of the spectra of CdS thin films and nanopowders. The large width of the peaks in the experimental X-ray

Phase, structure type,	Lattice	Atom	Position	A	Filling		
space group	parameters, nm		and multiplicity	x/a	y/b	z/c	degree
Trigonal phase $\alpha$ -HgS, $P3_121$ ( $D_3^4$ )	a = 0.41488 $c = 0.95039$	Hg S	3( <i>a</i> ) 3( <i>b</i> )	0.280 0.508	0	0.3333 0.8333	1.0 1.0
Cubic phase $\beta$ -HgS, type $B3$ ( $\alpha$ -ZnS), $F\bar{4}3m$ ( $T_d^2$ )	a = 0.58514	Hg S	4( <i>a</i> ) 4( <i>c</i> )	0 0.25	0 0.25	0 0.25	1.0 1.0

Table 4. Crystal structures of  $\alpha$ -HgS and  $\beta$ -HgS phases [113] of mercury sulfide.



**Figure 7.** Comparison of experimental X-ray diffraction pattern of (a) CdS nanopowder with calculated line spectra; (b) disordered structure with an 'average' hexagonal (sp. gr. P6) lattice; (c) hexagonal (sp. gr.  $P6_3mc$ ) wurtzite type structure B3; (d) cubic (sp. gr.  $F4\bar{3}m$ ) sphalerite structure B4. (Figure constructed by the author of the review based on data from [57–59, 100].)

diffraction pattern of CdS (Fig. 7a) is due to the small size of the coherent scattering regions (CSRs) in the nanostructured CdS sample. The periods of the unit cell of CdS with an average hexagonal lattice, taken for the model calculation, are a=0.236 nm and c=0.334 nm.

As can be seen, the positions and relative intensities of the diffraction reflections in the spectrum calculated for the average lattice (Fig. 7b) are in good agreement with the experimental data. The calculated line spectra of cadmium sulfide with wurtzite (Fig. 7c) and sphalerite (Fig. 7d) structures differ significantly from the experimental X-ray diffraction pattern.

In general, nonempirical calculations of X-ray diffraction patterns of CdS powders in Refs [57–59, 100] and comparison with experimental spectra showed that the atomic structure of cadmium sulfide nanoparticles with a size of less than 5 nm is disordered.

Mercury sulfide HgS is the only compound in the Hg-S system. Mercury sulfide contains  $\sim 50$  at.% of S and has a melting point of  $\sim 1093$  K [112]. Mercury sulfide has three polymorphic modifications.

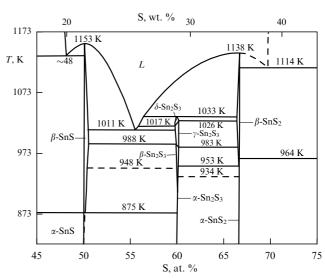
The low-temperature trigonal (sp. gr.  $P3_121$  ( $D_3^4$ )) modification  $\alpha$ -HgS (cinnabar) is stable at temperatures below  $\sim 607-618$  K [113]. In the temperature range of  $\sim 618-754$  K, there is a cubic (sp. gr.  $F\bar{4}3m$  ( $T_d^2$ )) modification  $\beta$ -HgS (metacinnabar) with a B3 structure (sphalerite  $\alpha$ -ZnS). The

high-temperature hexagonal phase γ-HgS (hypercinnabar) with lattice parameters a = 0.7010 nm and c = 1.4130 nm or a = 0.6860 nm and c = 1.4070 nm, stable from  $\sim 745 - 754 \text{ K}$ to the melting point of  $\sim 1093$  K, was discovered in synthesized and natural samples of mercury sulfide [112]. In the same paper, a section of the phase diagram of the Hg-S system was constructed in the region of existence of three modifications of mercury sulfide. According to the data from Ref. [112], the hexagonal phase  $\gamma$ -HgS is defective in the metallic sublattice, and the unit cell of this phase includes 12 formula units of HgS. Traces of the  $\gamma$ -HgS phase were also discovered in Ref. [114]. According to Ref. [115], weak reflections appear in the X-ray diffraction pattern of mercury sulfide at a temperature of 798 K, indicating a phase transition  $\beta$ -HgS- $\gamma$ -HgS. Presumably, the structure of  $\gamma$ -HgS is described in the space group P6/mmm. In none of the above papers were the atomic coordinates determined in the structure of the  $\gamma$ -HgS hexagonal phase.

The parameters of the unit cells of  $\alpha$ -HgS and  $\beta$ -HgS and the coordinates of the Hg and S atoms in them are given in Table 4.

### 2.3 M-S systems of metals in IVA group (M = Sn, Pb)

In the Sn-S system, there are three stable compounds, SnS, Sn<sub>2</sub>S<sub>3</sub>, SnS<sub>2</sub>, and the metastable phase Sn<sub>3</sub>S<sub>4</sub>. Tin sulfides SnS and SnS<sub>2</sub> have two polymorphic modifications each, and the sulfide Sn<sub>2</sub>S<sub>3</sub> has four polymorphic modifications  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$  [119]. A part of the phase diagram for the Sn-S system in the region of existence of tin sulfides is shown in Fig. 8.



**Figure 8.** Phase diagram of Sn–S system in region from 45 to 70 at.% S, where tin sulfide phases are observed. (Figure constructed by the author of the review based on data from Refs [116, 119, 121].)

<b>Table 5.</b> Crystal structures of coarse-crystalline orthorhombic low-temperature $\alpha$ -SnS phase [119] and high-temperature $\beta$ -SnS phase	se of tin sulfide at
298 K [121].	

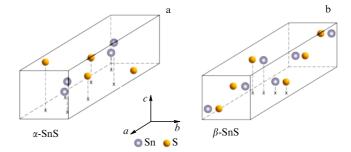
Phase, structure type,	Lattice	Atom	Position	Atomic coordinates			Filling
space group	parameters, nm		and multiplicity	x/a y/b	z/c	degree	
Orthorhombic $\alpha$ -SnS, $Pnma\ (Pbnm)\ (D^{16}_{2h})$	a = 1.1200 b = 0.3987 c = 0.4334	Sn S	4(c) 4(c)	0.1194 0.3508	0.25 0.25	0.1198 0.0207	1.0 1.0
Orthorhombic $\beta$ -SnS, $Cmcm(D_{2h}^{17})$	a = 1.1481 $b = 0.4177$ $c = 0.4148$	Sn S	4(c) 4(c)	0	0.120 0.349	0.25 0.25	1.0 1.0

Tin monosulfide SnS contains  $\sim 50$  at.% of S and has a melting point of  $\sim 1148-1153$  K [117, 118]. Tin sulfide SnS has two polymorphic modifications. The low-temperature orthorhombic (sp. gr.  $Pnma(D_{2h}^{16})$ ) modification  $\alpha$ -SnS is stable at temperatures below  $\sim 875-878$  K. Initially, with a different choice of axial directions, the space group of the α-SnS modification (herzenbergite) was determined as Phnm [117-119]. The unit cell parameters of the low-temperature orthorhombic (sp. gr. *Pnma*) phase of  $\alpha$ -SnS are a = 1.1195 - 1.1200 nm, b = 0.3987 - 0.3988 nm, and c = 0.4332 - 0.4334 nm [120, 121]. At a temperature above  $\sim 878$  K, the low-temperature orthorhombic tin sulfide transforms into the high-temperature orthorhombic (sp. gr. *Cmcm*) modification of  $\beta$ -SnS. According to neutron diffraction data [122], the unit cell parameters of hightemperature orthorhombic (sp. gr. *Cmcm*) tin sulfide  $\beta$ -SnS at a temperature of 1000 K are a = 1.1481 nm, b = 0.4173 nm, and c = 0.4128 nm. The unit cell parameters of the  $\alpha$ -SnS phase and the coordinates of the Sn and S atoms, transformed from the data for space group Pbnm [119] to the data for space group *Pnma*, are given in Table 5. Table 5 also presents the unit cell parameters of the high-temperature  $\beta$ -SnS phase and the coordinates of the Sn and S atoms in it [121].

The authors of Ref. [123] reported the formation of a cubic (sp. gr.  $Fm\bar{3}m$ ) SnS phase with a lattice period of a = 0.580 nm in a film epitaxially deposited on an NaCl substrate. The calculation [124] performed within the framework of the density functional theory (DFT) using the generalized gradient approximation (GGA) showed that cubic tin sulfide SnS has a lattice period of a = 0.575 nm. In enthalpy of formation (-0.95 eV), cubic SnS sulfide is close to orthorhombic (sp. gr. Pnma) α-SnS, which has an enthalpy of formation of -1.03 eV. According to experimental results [125, 126] and theoretical ab initio calculations [127], the formation of a metastable, strongly distorted cubic (sp. gr.  $P2_13$ ) phase of  $\pi$ -SnS is possible in thin films, including 32 formula units of SnS and having a unit cell period of a = 1.1603 - 1.1506 nm. According to Ref. [128], the formation enthalpy of the  $\pi$ -SnS phase is 0.01 eV atom<sup>-1</sup> higher than that of orthorhombic  $\alpha$ -SnS tin sulfide. According to Ref. [128], the thermodynamic stabilization of the  $\pi$ -SnS phase is facilitated by the presence of vacancies in the metallic sublattice.

The unit cells of the orthorhombic phases of  $\alpha$ -SnS and  $\beta$ -SnS tin sulfide are shown in Fig. 9.

Lead sulfide is the only compound that exists in the Pb-S system (Fig. 10). It contains ~ 50 at.% of S, has a melting point of 1391 K, and has a narrow homogeneity region [129]. A detailed analysis of the phase diagram of the Pb-S system near 50 at.% of S (see the inset in Fig. 10) shows that the maximum melting point of lead sulfide corresponds to the



**Figure 9.** Unit cells of orthorhombic phases (a)  $\alpha$ -SnS (sp. gr. *Pnma*) and (b)  $\beta$ -SnS (sp. gr. *Cmcm*) of tin sulfide, constructed by the author of the review based on data from Refs [119, 121].

nonstoichiometric composition PbS<sub>0.9998</sub>. From the data of Ref. [129], it follows that, at a temperature of 1300 K, lead sulfide has a very narrow homogeneity region from 49.9905 to 50.003 at.% of S. Coarse-crystalline (bulk) lead sulfide is considered to be a stoichiometric compound with a negligibly narrow homogeneity region of PbS<sub>0.9995-1.0005</sub> at 298 K.

Under normal conditions, coarse-crystalline lead sulfide PbS has a cubic (sp. gr.  $Fm\bar{3}m$ ) structure of type B1 with a lattice period of a = 0.59362 nm [130] (Fig.11a).

Under a pressure of 2.5 GPa, lead sulfide with the B1 structure acquires the orthorhombic B16 (B33) structure, i.e., a phase transition from the cubic (sp. gr.  $Fm\bar{3}m$ ) structure of the B1 type to the orthorhombic (sp. gr. Pnma) structure of the GeS type is observed [129]. With a decrease in the particle size, the surface energy of the substance increases; therefore, the pressure required to change the crystal structure must increase. Indeed, in PbS nanopowder, the phase transition from the cubic B1 structure to the orthorhombic structure begins at a higher pressure of 3.0 GPa [131]. Both phases with the B1 and B16 (B33) structures can exist simultaneously up to 8 GPa. With an increase in pressure to 25 GPa, a second phase transition of lead sulfide to the cubic structure of the CsC1 (B2) type is observed [132].

Studies of nanopowders, isolated nanoparticles, and quantum dots of lead sulfide using X-ray and electron diffraction methods [133–137] in combination with high-resolution transmission electron microscopy (HRTEM) data confirm their type *B*1 cubic structure.

The crystal structure of PbS nanofilms was also considered to be a B1 type structure for a long time, but studies in recent years have shown that this opinion is erroneous. The crystal structure of  $\sim 100$ -nm-thick PbS nanostructured films was quantitatively determined in [138] using different models of the cubic structure. As a result of the quantitative analysis, it was established that the real structure of the PbS nanofilm belongs to the  $Fm\bar{3}m$  space group, but the sulfur atoms S in it

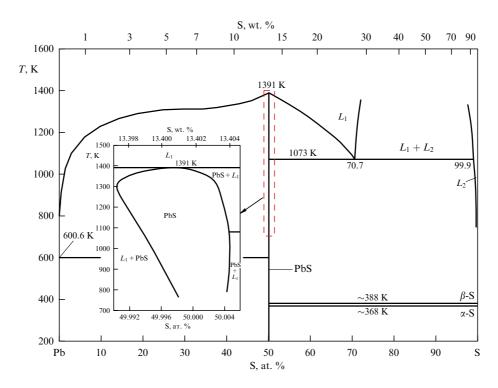
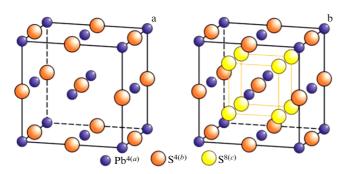


Figure 10. Phase diagram of Pb – S system. Inset shows an enlarged section of diagram near 50 at.% of S, showing presence of a very narrow homogeneity region in lead sulfide. (Figure constructed by the author of the review based on data from Refs [13, 129]).



**Figure 11.** Crystal structures of lead sulfide PbS: (a) unit cell of coarse-crystalline (bulk) cubic (sp. gr.  $Fm\bar{3}m$ ) lead sulfide with structure of B1 type (b) distribution of Pb and S atoms in unit cell of cubic (sp. gr.  $Fm\bar{3}m$ ) structure of  $D0_3$  type of PbS  $\equiv PbS_y^{4(b)}S_{1-y}^{8(c)}$  nanofilm. In unit cell with  $D0_3$  type structure, S atoms statistically occupy octahedral positions 4(b) with probability y and statistically occupy tetrahedral positions 8(c) with probability (1-y)/2. (Figure constructed by the author of the review based on data from Refs [13, 138].)

are located not only in octahedral interstices (4(b) positions), but also in tetrahedral interstices (8(c) positions) (Fig. 11b). In such a structure, the probabilities of filling the 4(b) and 8(c) positions with S atoms are equal to y and (1-y)/2, respectively.

Minimization of experimental X-ray diffraction patterns of PbS nanofilms recorded in situ at temperatures from 293 to 423 K with a step of 30–40 K showed that at all temperatures the degrees of filling of positions 4(b) and 8(c) by S atoms are equal to  $\sim 0.84$  and  $\sim 0.08$ , respectively (Table 6).

The value of the convergence factor  $R_I$  for all X-ray diffraction patterns did not exceed 0.017. Thus, in the lattice of the PbS film, a hidden nonstoichiometric distribution of S atoms over positions 4(b) and 8(c) is realized. The new cubic

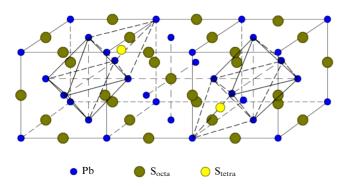
**Table 6.** Cubic (sp. gr.  $Fm\bar{3}m$ ) structure of type  $D0_3$  of nanostructured PbS film at temperature of 293 K: a = 0.59395 nm [138].

Atom	Position	Atoı	Filling		
	and multiplicity	x/a	y/a	z/a	degree
Pb	4( <i>a</i> )	0	0	0	1
S	4(b)	0.5	0.5	0.5	0.84
S	8( <i>c</i> )	0.25	0.25	0.25	0.08

(sp. gr.  $Fm\bar{3}m$ ) structure found in lead sulfide nanofilms belongs to the structural type  $D0_3$  with a partially disordered (statistical) distribution of S atoms over positions of two types (Fig. 11b). Taking into account the crystal structure of the nanofilm and the degrees of filling the positions 4(b) and 8(c), the formula of the lead sulfide nanofilm can be represented as  $PbS_{0.84}^{4(b)}S_{0.16}^{8(c)} \equiv Pb(S_{0.84}\square_{0.16})^{4(b)}(S_{0.16}\square_{0.84})^{8(c)}$ , where  $\square$  is a structural vacancy.

Let us consider a model of the  $D0_3$  structure of a PbS nanofilm, which includes three unit cells (Fig. 12). This model cell contains 12 octahedral interstices, i.e., 12 positions (b). In a cubic structure with the space group  $Fm\bar{3}m$ , the number of tetrahedral interstices is twice the number of octahedral interstices. Therefore, for 12 octahedral interstices, there are 24 tetrahedral interstices, i.e., 24 positions (c). The filling of positions (b) and (c) by S atoms with probabilities of  $\sim 0.84$  and  $\sim 0.08$  means that, approximately, out of every 12 octahedral interstices, 10 are occupied by S atoms, and two are empty. Two tetrahedral interstices are also occupied by S atoms, and the rest are vacant. The absence of superstructural reflections means that the arrangement of S atoms at positions of each type is disordered, statistical.

Thus, the considered semiconductor sulfides have a nonmolecular coordination structure, and some semiconductor sulfides (in particular, copper and silver sulfides) have a



**Figure 12.** Model of cubic (sp. gr.  $Fm\bar{3}m$ ) structure of type  $D0_3$  of the PbS nanofilm: S atoms statistically occupy ten of the 12 octahedral interstices (positions (b)) and two tetrahedral interstices (positions (c)) out of 24 tetrahedral interstices. The 10 occupied and two empty octahedral interstices, as well as the two occupied tetrahedral interstices, are shown.

nonstoichiometry of the metallic sublattice both in the coarsecrystalline and nanocrystalline states. A nonstoichiometric distribution of sulfur atoms S over two different positions of the nonmetallic sublattice was found in lead sulfide nanofilms. However, due to the lack of study, information on the nonstoichiometry of most nanocrystalline sulfides is still absent. In review [139], using carbides as an example, it was shown that a decrease in the particle size of solid-phase substances, including sulfides, to the nanometer scale leads to the appearance or increase of nonstoichiometry. Among the publications of recent years on the nonstoichiometry of semiconductor sulfides, papers [140–143] are also worth mentioning.

# 3. Characteristics of electronic structure of semiconductor sulfides

To understand the properties of nanocrystalline semiconductor sulfides, it is useful to know the characteristics of the electronic structure of the corresponding coarse-crystalline semiconductors. An important property of semiconductors is the band gap width  $E_{\rm g}$ . Information on the value of  $E_{\rm g}$  of coarse-crystalline elementary and binary semiconductors obtained before 1971 is summarized in Ref. [144]. In subsequent years, measurements and estimates of the band gap width were carried out mainly in nanostructured semiconductor compounds.

It is known that decreasing the particle size to the nanometer scale noticeably affects the properties of substances [145–147]. From a scientific point of view, not all substances with a particle size in the nanometer range from 1 to 100 nm are nanomaterials, but only those in which size effects are manifested and whose properties differ significantly from the properties of coarse-crystalline substances. In general, size effects unite a complex of phenomena associated with a change in the properties of a substance due to (1) a direct change in the size and morphology of particles, (2) a high development and area of intergranular boundaries, which, with a grain size from 100 to 10 nm, contain from 10 to 50% of the nanocrystalline solid atoms and contribute to the properties of the system, (3) commensurability of the particle size with physical parameters having the dimension of length [145–147]. If the sizes of particles (grains, crystallites) of a solid in one, two, or three directions are commensurate with some characteristic physical parameters that have the dimension of length (size of magnetic domains, electron mean free path, de Broglie wavelength, exciton diameter), then size effects will be observed in the corresponding properties. In semiconductor compounds, the ratio of particle sizes to the exciton size determines whether size effects will be observed in their properties. In other words, when the size of crystalline particles decreases to sizes comparable to the exciton size, the semiconductor crystalline substance passes into a nanocrystalline state.

For example, the size of an exciton in semiconductors is up to tens of nanometers and exceeds the size of a unit cell. This opens the possibility of creating semiconductor sulfide nanomaterials whose properties are changed by regulating the sizes of their constituent structural elements (particles, grains, crystallites).

An exciton is a quasiparticle which is an electronic excitation migrating through a crystal without transferring electric charge or mass. An exciton in a semiconductor is a bound state of an electron and a hole occupying different sites of the crystal lattice. The exciton can be considered an independent elementary particle in cases where the interaction energy of an electron and a hole is of the same order as the energy of their motion, and the interaction energy between two excitons is small compared to the energy of each of them. An exciton in a semiconductor, called a Wannier–Mott exciton, is a bound state of a conduction electron and a hole located at a distance greater than the interatomic distance. Excitons in semiconductors with high permittivity are characterized by a large size (many times greater than the distance between atoms) and low energy.

The characteristic size of a Wannier–Mott exciton (or the Bohr radius of an exciton) in a macroscopic semiconductor crystal is equal to  $R_{\rm ex}\approx n^2\hbar^2\varepsilon/\mu_{\rm ex}e^2=(n^2\varepsilon m_0/\mu_{\rm ex})a_{\rm B}$ , where  $\varepsilon$  is the permittivity;  $\mu_{\rm ex}=m_{\rm e}m_{\rm h}/(m_{\rm e}+m_{\rm h})$  is the reduced mass of an exciton;  $m_{\rm e}$  and  $m_{\rm h}$  are the effective masses of an electron and a hole, expressed through the rest mass of a free electron  $m_0=9.109\times10^{-31}$  kg;  $a_{\rm B}=\hbar^2/m_0e^2=0.0529$  nm is the Bohr radius;

$$\hbar = \frac{h}{2\pi} = 1.055 \times 10^{-34} \text{ J s} = 1.055 \times 10^{-27} \text{ g cm}^2 \text{ s}^{-1}$$
  
=  $6.583 \times 10^{-16} \text{ eV s}$ 

is the Planck constant; and  $e=4.8032\times 10^{-10}~\rm cm^{3/2}~g^{1/2}~s^{-1}$  is the elementary charge.

If the particle size of the nanostructured sulfide is smaller than the exciton size, then size effects will be observed in the electronic properties of the sulfide, including the band gap width  $E_{\rm g}$ . The quantum size effect in semiconductors, namely the short-wave shift of the exciton absorption lines of CuCl nanoparticles in a glass matrix, was first discovered in Ref. [148].

Biexciton effects also play a significant role in semiconductors. A biexciton is a bound complex of two electrons and two holes. In direct band semiconductors, the formation and decay of biexcitons occur under nonequilibrium conditions.

In an experimental study of the induced conversion of excitons to biexcitons, the sample is excited by laser radiation in the region of interband transitions, where broad one-photon absorption bands are observed, indicating the formation of biexcitons [149]. Resonant excitation of biexcitons in the process of giant two-photon absorption was experimentally detected in the transmission spectra of CdS under laser excitation [150]: against the background of a flat tail of the exciton absorption band, a narrow absorption line

at 2.5499 eV was clearly observed, associated with resonant two-photon absorption and with the creation of a biexciton in cadmium sulfide. For coarse-crystalline (bulk) CdS at a temperature of 2 K, the biexciton binding energy and its excitation energy are  $4.4 \pm 0.2$  meV and 5.0998 eV. With increasing temperature, the biexciton absorption lines disappear from the transmission spectra at 20-25 K due to thermal dissociation of biexcitons and their scattering by phonons. An important tool for studying the structure and spectrum of biexcitons in direct band semiconductors is hyper-Raman (or two-photon Raman) scattering. In Ref. [151], using the example of CdS quantum dots in a glass matrix, it was shown experimentally and theoretically that the biexciton binding energy in semiconductors increases with decreasing quantum dot size. M.G. Bawendi et al. [152] noted that, in nanocrystals, due to the almost exact balance between absorption and emission, the optical gain condition can be achieved only by exciting biexcitons. Note that M.G. Bawendi et al. [153] previously created a method for synthesizing colloidal solutions of nearly monodisperse chalcogenide quantum dots in organic solvents. Among many other papers by M.G. Bawendi, it is necessary to mention studies on the synthesis of core/shell heterostructures based on cadmium telluride and cadmium selenide, cadmium and zinc sulfides, etc. [154-157].

Exciton and biexciton effects in quantum dots of semiconductor chalcogenides have been considered in many studies, including [158–162].

A decrease in the particle size of nanostructured compounds compared to crystallite ones also leads to a transformation of the density of states, which is most clearly manifested in quantum dots. According to Ref. [1], in the regime of strong quantum localization in nanostructured semiconductors, such fundamental properties as the density of electron states and the width of the band gap  $E_{\rm g}$  change. In Refs [163, 164], it was noted that a decrease in the dimensionality of a semiconductor can increase the electron density of states near the Fermi level. Such features in the density of electron states of nanostructured semiconductors can arise because of two- or three-dimensional quantum confinement.

Information on the effective masses of electrons and holes in Cu<sub>2</sub>S sulfide is limited to theoretical paper [67], in which the values of  $m_{\rm e}$  and  $m_{\rm h}$  are given for the model cubic chalcocite  $\gamma$ -Cu<sub>2</sub>S (Cu<sub>32</sub>S<sub>16</sub>). The permittivity  $\varepsilon=4.79$  was estimated in Ref. [165] for a thin film of orthorhombic chalcocite Cu<sub>2</sub>S. According to the data in Ref. [166], the permittivity  $\varepsilon$  of the Cu<sub>2-x</sub>S phase at small values of x is 10–15. Taking into account the data from [67, 165], the reduced mass of the exciton in Cu<sub>2</sub>S is equal to  $(0.21-0.25)m_0$ . The radius of the first exciton state (n=1) is  $R_{\rm ex}\approx 1.0-1.2$  nm with  $\varepsilon\approx 4.8$  [165] or  $R_{\rm ex}\approx 2.5-3.8$  nm with  $\varepsilon$  from 10 to 15 [166].

The band gap width for indirect and direct transitions in the coronal crystalline sulfide  $Cu_2S$  is 1.05–1.30 eV [167–169] and 1.3–1.9 eV [167, 168, 170, 171], respectively.

According to various data [172–174], hexagonal covellite CuS has a band gap width from  $\sim 1.2-2.0$  eV for coarse-crystalline samples to 3.0–3.5 eV for nanocrystalline films.

Under normal conditions, coarse-crystalline (bulk) silver sulfide with the acanthite structure  $\alpha$ -Ag<sub>2</sub>S is a direct semiconductor with a wide band gap  $E_{\rm g}$  and low carrier mobility. For coarse-crystalline acanthite  $\alpha$ -Ag<sub>2</sub>S, the effective electron and hole masses are  $m_{\rm e}=0.286m_0$  and  $m_{\rm h}=1.096m_0$ , and the permittivity  $\varepsilon$  is 5.95 [175]. Taking

this into account, the reduced exciton mass  $\mu_{ex}$  for acanthite  $\alpha$ -Ag<sub>2</sub>S is  $\sim 0.23m_0$ . However, the data in [175] on the effective masses of an electron and a hole in α-Ag<sub>2</sub>S are most likely not entirely correct, since this paper does not contain any information on estimating the Brillouin zones or measuring the effective masses by the cyclotron resonance method. According to the calculation of the electronic structure of the coarse-crystalline (bulk) monoclinic silver sulfide  $\alpha$ -Ag<sub>2</sub>S, which was obtained in Ref. [176] within the framework of the density functional theory (DFT) using the generalized gradient approximation (GGA), the effective masses of the electron and hole corresponding to the lower conduction band and the higher valence band (the  $\Gamma$  points of the Brillouin zone) are  $m_e = 0.42m_0$  and  $m_h = 0.81m_0$ , and the band gap width is 0.914 eV. For such values of the effective masses of the carriers, the reduced exciton mass  $\mu_{\rm ex}$ for acanthite  $\alpha$ -Ag<sub>2</sub>S is equal to  $\sim 0.28m_0$ .

The permittivity of silver sulfide is a complex quantity. According to Refs [177, 178], the real part of the permittivity  $\varepsilon$  in silver sulfide is 8.36 or 8.8, respectively. Considering the value of  $\varepsilon$  from  $\sim$  6 to  $\sim$  8.8, the characteristic size of the first (n=1) Wannier–Mott exciton  $R_{\rm ex}$  in coarse-crystalline acanthite  $\alpha$ -Ag<sub>2</sub>S is  $\sim$  1.4–2.1 nm for  $\mu_{\rm ex}=0.23m_0$  or  $\sim$  1.1–1.7 nm for  $\mu_{\rm ex}=0.28m_0$ . The exciton diameter is  $D_{\rm ex}\approx$  2.8–4.2 nm or 2.2–3.4 nm and is 3–8 times greater than the periods of the unit cell of monoclinic acanthite. According to Ref. [179], the exciton diameter of silver sulfide is  $\sim$  4.4 nm.

The authors of Ref. [176] also found an empirical dependence of the energy of the ground exciton state (deviation of the energy of the ground exciton state from the band gap width of coarse-crystalline Ag<sub>2</sub>S),  $\Delta E_{\rm ex}$ , on the diameter D of the quantum dot of silver sulfide:  $\Delta E_{\rm ex}$  [eV] =  $4.8366D^{-2.1525} - 0.0959$ . The diameter D of the quantum dot in this dependence is taken in nanometers. It follows from this dependence that, in the limit  $D \to \infty$ , i.e., for coarse-crystalline (bulk) silver sulfide, the exciton binding energy is 0.096 eV.

The band gap width of  $\alpha$ -Ag<sub>2</sub>S depends on temperature. According to Refs [77, 78], the value of  $E_{\rm g}$  in acanthite  $\alpha$ -Ag<sub>2</sub>S at a temperature of 300 K is  $\sim 0.8-1.0$  eV. The generally accepted band gap width  $E_{\rm g}$  for acanthite  $\alpha$ -Ag<sub>2</sub>S at 300 K is 0.9–1.1 eV [11].

Under normal conditions, coarse-crystalline (bulk) zinc sulfide is a direct band semiconductor. For coarse-crystalline hexagonal zinc sulfide at T=300 K, the effective masses of the electron and hole are  $m_{\rm e}=0.28m_0$  and  $m_{\rm h}=0.49m_0$  [180]. With these values taken into account, the reduced exciton mass  $\mu_{\rm ex}$  of hexagonal zinc sulfide ZnS is  $\sim 0.18m_0$ .

The permittivity of hexagonal zinc sulfide at 300 K is  $\varepsilon_{11} = \varepsilon_{33} = 8.7$  [181],  $\varepsilon_{11} = 8.1$ , and  $\varepsilon_{33} = 8.5$  [182], or  $\varepsilon_{11} = 8.31$  and  $\varepsilon_{33} = 8.76$  [183]. According to [180], the permittivity of cubic and hexagonal zinc sulfide is 8.9 and 8.75, respectively. With the reduced exciton mass  $\mu_{\rm ex} = 0.18m_0$  and the permittivity  $\varepsilon_{\rm ZnS}$  from 8.1 to 8.76, in coarse-crystalline zinc sulfide ZnS, the size  $R_{\rm ex}$  of the first exciton state is from  $\sim 2.4$  to  $\sim 2.6$  nm; the diameter  $D_{\rm ex}$  is  $\approx 4.8-5.2$  nm.

The band gap width  $E_{\rm g}$  of cubic  $\alpha$ -ZnS at a temperature of 300 K is 3.54–3.76 eV [180, 184];  $E_{\rm g}$  of hexagonal wurtzite  $\beta$ -ZnS is  $\sim$  3.74–3.91 eV [184, 185].

Coarse-crystalline (bulk) cadmium sulfide is a direct band semiconductor. For coarse-crystalline cadmium sulfide at T = 300 K, the electron and hole effective masses are

 $m_{\rm e}=0.19m_0$  and  $m_{\rm h}=0.80m_0$  [186],  $m_{\rm e}=0.21m_0$  [187] or  $m_{\rm e}=0.205m_0$  and  $m_{\rm h}=0.81m_0$  [188]. With these values taken into account, the reduced exciton mass  $\mu_{\rm ex}$  of cadmium sulfide CdS is  $\sim 0.16m_0$ .

The dielectric constants  $\varepsilon_{11}$  and  $\varepsilon_{33}$  of cadmium sulfide, measured by the ultrasonic resonance method at 300 K, are 8.67 and 10.2, respectively [189]. According to ellipsometry measurements [190],  $\varepsilon_{\perp}=8.28$  and  $\varepsilon_{\parallel}=8.73$  at 300 K. Considering the generalized data [189–191], the dielectric constant  $\varepsilon$  of cadmium sulfide at 300 K is  $\sim$  9.0. With the reduced mass  $\mu_{\rm ex}=0.16m_0$  and the dielectric constant  $\varepsilon_{\rm CdS}=9.0$  in coarse-crystalline cadmium sulfide CdS, the size  $R_{\rm ex}$  of the first exciton state with n=1 is  $\sim$  3.0 nm; the diameter  $D_{\rm ex}$  is  $\approx$  6.0 nm.

The band gap width of CdS is highly dependent on temperature. A detailed analysis of the temperature dependence  $E_{\rm g}(T)$  for cadmium sulfide was performed in Ref. [192]. According to [192],  $E_{\rm g}(T)$  decreases monotonically from  $\sim 2.58$  to  $\sim 2.49$  eV with a temperature increase from 0 to 300 K. The generally accepted band gap width of CdS at 300 K is  $\sim 2.42$  eV [13].

The trigonal  $\alpha$ -HgS and cubic  $\beta$ -HgS phases of mercury sulfide are direct band semiconductors. The coarse-crystalline (bulk) trigonal phase of  $\alpha$ -HgS is a wide-band semiconductor with a band gap width of  $E_{\rm g}=2.0-2.3$  eV [144, 193, 194]. There is no data in the literature on the effective masses of electrons and holes in trigonal  $\alpha$ -HgS.

According to Ref. [195], the effective masses of the electron and hole in cubic mercury sulfide  $\beta$ -HgS are  $m_e = 0.032m_0$  and  $m_h = 0.041m_0$ , and the permittivity is  $\varepsilon = 11.36$ . According to the calculations in [196], the value of  $\varepsilon$  is 12.9. For the indicated values of  $m_e$ ,  $m_h$ , and  $\varepsilon$ , the mass and radius of the exciton in cubic  $\beta$ -HgS are  $\sim 0.018m_0$  and  $\sim 33.4-37.9$  nm. The size (diameter) of the exciton is more than 100 times greater than that of the unit cell of  $\beta$ -HgS sulfide.

According to various data, the band gap of  $\beta$ -HgS is from 0.54 eV [197] to 0.05 eV [198] or -0.15 eV [199] and -0.19 eV [200]. According to calculations [196] using the generalized gradient approximation in the Engel–Vosko scheme, the value of  $E_{\rm g}$  for cubic mercury sulfide  $\beta$ -HgS is -0.1 eV. The small value and even the negative sign of the energy gap in  $\beta$ -HgS is associated with the small spin-orbit splitting in sulfur [198].

Until about the 1970s, orthorhombic tin sulfide  $\alpha$ -SnS was identified as an indirect transition semiconductor based on optical measurements. However, later in Ref. [201], a direct transition was discovered in tin sulfide along with an indirect transition.

At T=300 K, the effective masses of a hole in single-crystal  $\alpha$ -SnS, depending on the direction, are  $m_{ha}=m_{hb}=0.2m_0$  and  $m_{hc}=m_0$  [202–204], and the average effective mass of a hole is  $\sim 0.34m_0$ . According to Ref. [205], the effective masses of an electron in bulk tin sulfide, depending on the direction, are  $m_{ea}=0.45m_0$ ,  $m_{eb}=0.16m_0$ , and  $m_{ec}=0.20m_0$ , and the average effective mass of an electron is  $\sim 0.24m_0$ . For the above values, the average reduced mass  $\mu_{\rm ex}$  of an exciton in orthorhombic  $\alpha$ -SnS is  $\sim 0.14m_0$ .

The experimental average value of the permittivity  $\varepsilon$  at 300 K is 12.5 [206]. According to calculations [205], in coarse-crystalline orthorhombic tin sulfide, it is 11.7, 13.8, and 11.4 for the a-, b-, and c-axes, the average value being 12.3. According to Ref. [204], the permittivity of  $\alpha$ -SnS sulfide is 19.5. With the reduced exciton mass  $\mu_{\rm ex}=0.14m_0$  and the

permittivity  $\varepsilon_{\rm SnS}$  from 12.3 to 19.5, in coarse-crystalline tin sulfide, the exciton radius  $R_{\rm ex}$  is from  $\sim$  4.6 to  $\sim$  7.4 nm; the diameter  $D_{\rm ex}$  is  $\approx$  9.2–14.8 nm.

The band gap width  $E_{\rm g}$  of  $\alpha$ -SnS sulfide is 2.21 eV [207] or 2.07 eV [208] for the indirect transition. According to calculations [205], the band gap width  $E_{\rm g}$  for the direct transition is 1.32–1.62 eV. In orthorhombic  $\alpha$ -SnS films, the band gap widths for the indirect and direct transitions depend on the stoichiometry of the sulfide and vary from 1.07 to 1.25 eV and from 1.30 to 1.39 eV, respectively [204]. According to Ref. [209], the temperature dependence of the indirect optical gap width is described by the function  $E_{\rm g}=1.21-0.00048T$  [eV].

Under normal conditions, coarse-crystalline (bulk) lead sulfide PbS is a narrow direct band semiconductor. At T=4 K, the effective masses of an electron and a hole in PbS are  $m_{\rm e}=(0.092\pm0.012)m_0$  and  $m_{\rm h}=(0.090\pm0.015)m_0$  [210]. According to [211], the effective masses of an electron and a hole in bulk lead sulfide at 300 K are  $m_{\rm e}=m_{\rm h}=0.105m_0$ , so that the exciton mass is  $\mu_{\rm ex}=0.0525m_0$ . The permittivity  $\varepsilon$  of lead sulfide at 300 K is 18 [212], 17.2 [213], 17.0 [211], or 16.4 [214]. At  $\mu_{\rm ex}=0.0525m_0$  and a permittivity  $\varepsilon$  of  $\approx 17-18$  for lead sulfide, the size  $R_{\rm ex}$  of the first exciton state with n=1 is  $\sim 19\varepsilon a_{\rm B}$  or 17–18 nm.

According to the results of early studies in the 1950s and 1960s and many other studies summarized by the authors of Refs [212, 215, 216], at a temperature of 300 K in single-crystal PbS and in polycrystalline PbS films, the band gap width  $E_{\rm g}$  for direct transitions is equal to 0.41 and 0.42 eV, respectively.

Generalized parameters of coarse-crystalline sulfides necessary for estimating the exciton size, as well as the exciton sizes in the considered sulfides, are given in Table 7.

The exciton size is proportional to the dielectric constant  $\varepsilon$ , which increases noticeably in the series  $Cu_2S \to Ag_2S$ ,  $ZnS \rightarrow CdS \rightarrow HgS$ , and  $SnS \rightarrow PbS$ , as well as when transitioning from sulfides of metals of the IB group (Cu, Ag) to sulfides of metals of the IIB group (Zn, Cd, Hg) and to sulfides of metals of the IVA group (Sn, Pb). The exciton masses of the considered sulfides change much less strongly; therefore, the exciton size, like the value of  $\varepsilon$ , also increases in the series  $Cu_2S \to Ag_2S$ ,  $ZnS \to CdS \to HgS$ ,  $SnS \to PbS$ , as well as in the transition from sulfides of copper group metals to sulfides of zinc group metals and further to sulfides of tin group metals. Considering the sizes of excitons, the effects on the electronic properties of the considered sulfides can be observed in fairly large  $(\leq 15 \text{ nm})$  nanoparticles of lead sulfide and significantly smaller nanoparticles ( $\leq 3-4$  nm and  $\leq 1.5-2$  nm) of zinc and cadmium or copper and silver sulfides, respectively, which is in good agreement with numerous experimental data, summarized in Refs [9, 11–13]. The size effects in the electronic and optical properties are most clearly observed in colloidal solutions of sulfide quantum dots [11, 22–24, 179, 217, 218], in quantum dots dispersed in glass [219, 220] or polymer matrices [221–225], and in sulfide nanofilms [138]. The size effects in various properties of the considered semiconductor sulfides, associated both with the size of excitons and with other factors (enhancement of quantum localization, biexciton effects, transformation of the density of states, influence of the morphology of nanoparticles, change in the type and boundaries of the phonon spectrum) and synthesis conditions, are discussed in Section 4.

Table 7. Characteristics of electronic structure of coarse-crystalline (bulk) semiconductor sulfides at 300 K and exciton radii.

Sulfide	Effective masses o	f electron and hole	Exciton mass	Dielectric	Band gap	Literature	Exciton radius	
	$m_{\rm e}/m_0*$	$m_{ m h}/m_0$	$\mu_{\rm ex}/m_0$	constant $\varepsilon$	width $E_{\rm g}$ , eV		$R_{\rm ex}$ , nm	
$Cu_2S$	0.30 - 0.37	0.8	0.21-0.25	4.79	1.05–1.30 **,	[67, 165, 167 – 171]	~ 1.0-1.2	
					1.3-1.9 ***			
α-Ag <sub>2</sub> S	0.286	1.096	0.227	$\sim 6.0\!-\!8.8$	0.9 - 1.1	[11, 77, 78, 175, 177, 178]	1.4-2.1	
α-Ag <sub>2</sub> S	0.42	0.81	0.277	$\sim 6.0\!-\!8.8$	0.914	[176-178]	1.1-1.7	
β-ZnS	0.28	0.49	0.18	8.10-8.76	3.74-3.91	[7, 180 – 185]	2.4–2.6	
α-ZnS	-"-	_"_	-"-	8.9	3.54-3.76	[7, 180, 184]	2.6	
β-CdS	0.19-0.21	0.80-0.81	0.16	9.0	2.42-2.49	[13, 186-192]	3.0	
β-HgS	0.032	0.041	0.018	11.36-12.90	from -0.2 to 0.5	[193–200]	33.4–37.9	
α-SnS	0.24	0.34	0.14	12.3, 19.5	2.1–2.2 **,	[201–208]	$\sim 4.6 - 7.4$	
					1.3-1.6 ***			
PbS	0.105	0.105	0.0525	16.4 - 18.0	0.41-0.42	[210–216]	17–18	

<sup>\*</sup>  $m_0 = 9.1 \times 10^{-31}$  kg (rest mass of a free electron)

# 4. Size effects in properties of nanostructured sulfides

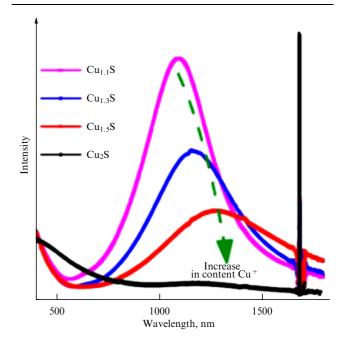
According to Ref. [166], the exciton radius in  $Cu_{2-x}S$  is from 3.5 to 5 nm. According to a more accurate estimate, the maximum exciton radius is 3.8 nm (see Table 7), and the exciton diameter in Cu<sub>2</sub>S sulfide does not exceed 8 nm, so actual, not imagined, quantum size effects in Cu<sub>2</sub>S can be observed for particles 8 nm or less in size. There is no information in the literature on the production and optical properties of nanostructured Cu<sub>2</sub>S sulfide (Cu<sub>2-x</sub>S) with nanoparticles of this size. Paper [166] describes the synthesis of CuS, Cu<sub>1.97</sub>S, and Cu<sub>1.8</sub>S nanocrystals by sonoelectrochemical and hydrothermal methods and by thermolysis. According to Ref. [166], the size of nanocrystals synthesized by the sonoelectrochemical method ranges from  $\sim 5$  to  $\sim$  15 nm, the diameters of nanoparticles obtained by the hydrothermal method are  $\sim 20-25$  nm, and the diameters of nanoparticles obtained by thermolysis reach  $\sim 30$  nm. A broad peak at about 400-600 nm was observed in all measured UV-Vis absorption spectra of synthesized copper sulfide nanocrystals, and for smaller nanocrystals synthesized by sonoelectrochemical and hydrothermal methods, the position of the peak was somewhat shifted to the short-wave region, which, according to the authors of Ref. [166], can be considered a blue shift. However, there is no quantitative processing of the UV-Vis absorption spectra and no estimate of the band gap width in Ref. [166]. In Ref. [49], a significant blue shift was detected in the UV-Vis absorption spectra of hexagonal covellite CuS nanoparticles  $\sim 17-19$  nm in size; the calculated band gap energies were  $\sim 4.3$  eV. Since the size of CuS nanoparticles is quite large (much larger than the exciton diameter), this result raises serious doubts. In general, there is no reliable information on quantum size effects in the literature on nanocrystalline copper sulfide.

Much more reliable are the results concerning the dependence of the band gap of  $Cu_{2-x}S$  sulfides on their composition. An increase in the band gap occurs with an increase in the value of x in coarse-crystalline (bulk) copper sulfides:  $E_g$  is equal to 1.2 eV for  $Cu_2S$ , 1.5 eV for  $Cu_{1.8}S$ , and 2.0 eV for CuS [166]. The optical properties of CuS calculated

in [226] are in reasonable agreement with the experimental results [166].

The optical absorption spectra of copper sulfide nanoparticles  $Cu_{2-x}S$  of the same size (13.0–13.7 nm) but different composition (Fig. 13) were obtained in Ref. [227]. For copper sulfide nanoparticles, observed in the absorption spectra is a plasmonic band associated with a change in the density of charge carriers, the holes. From Fig. 13, the shift of the absorption peak from 1090 nm for  $Cu_{1.1}S$  to 1250 nm for  $Cu_2S$  is clearly visible.

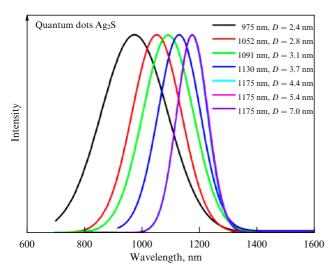
In recent years, CuS nanoparticles with different morphologies have attracted attention due to their potential for use in studying cancer tumors [20]. The potential for biomedical application of nanostructured copper sulfide is related to its photoconversion efficiency, i.e., the ability to



**Figure 13.** Plasmon band shift as a function of copper sulfide composition. Strong peak at 1700 nm is due to the solvent. (Reproduced from [227] with permission from American Chemical Society.)

<sup>\*\*</sup> band gap width for indirect transitions

<sup>\*\*\*</sup> band gap width for direct transitions



**Figure 14.** Photoluminescence emission spectra change depending on size of Ag<sub>2</sub>S quantum dots excited by 785-nm radiation. Quantum dot sizes and wavelengths corresponding to maxima of photoluminescence peaks are indicated. (Reproduced from [179] with permission from American Chemical Society.)

convert NIR radiation into thermal energy, which can then be used to remove cancer cells [228]. In recent paper [229], CuS nanoparticles with a size of  $11 \pm 3$  nm were proposed to be used as an effective contrast agent in the study of biological tissues. CuS nanoparticles are promising for water purification by photocatalytic decomposition (photodegradation) of pollutants (rhodamine, methylene, etc.), even in natural sunlight radiation [228, 230].

The exciton diameter in silver sulfide  $Ag_2S$  is about 4 nm (see Table 7), so obvious size effects in the electronic properties can be observed for sulfide nanoparticles smaller than 4 nm. As an example, Fig. 14 shows the change in photoluminescence emission spectra depending on the size of the  $Ag_2S$  quantum dots [179]. The position of the fluorescence maximum of the  $Ag_2S$  quantum dots changes from  $\sim 975$  to  $\sim 1175$  nm with an increase in their size D from 2.4 to 4.4 nm. With a further increase in the size of quantum dots from 4.4 to 7.0 nm, the position of the photoluminescence peaks remains unchanged and corresponds to 1175 nm.

The continuous blue shift of the photoluminescence of the Ag<sub>2</sub>S quantum dots from 1175 to 975 nm can be associated with the enhancement of the quantum confinement effect and an increase in the band gap  $E_g$  due to a decrease in the size of the Ag<sub>2</sub>S quantum dots. The almost constant position of the photoluminescence peaks at 1175 nm for the Ag<sub>2</sub>S quantum dots with a boundary size of 4.4 nm or more is evidence of a transition from the strong quantum confinement regime to the weak one. Accordingly, the exciton radius  $R_{\rm ex}$  of silver sulfide Ag<sub>2</sub>S can be experimentally estimated as half or less than half the boundary size of 4.4 nm, i.e.,  $\leq 2.2$  nm, which is in good agreement with the estimate of  $R_{\rm ex}$  given in Table. 7. A similar dependence of the photoluminescence of Ag<sub>2</sub>S quantum dots on their size in the range of 2.3-15.0 nm is given in Ref. [11]. The Ag<sub>2</sub>S quantum dots described in Ref. [11] were obtained in colloidal solutions of silver nitrate and sodium sulfide using the technique from [218]. With an increase in the size of Ag<sub>2</sub>S quantum dots from 2.3 to 4.2 nm, the photoluminescence peaks shift from  $\sim 960$  to  $\sim 1170$  nm, but, with a further increase in the size of the quantum dots, the position of these peaks remains virtually unchanged and

corresponds to 1166–1176 nm. According to Ref. [231], the photoluminescence peak of  $Ag_2S$  quantum dots  $\sim 1.5$  nm in size is observed at a wavelength of  $\sim 640$  nm.

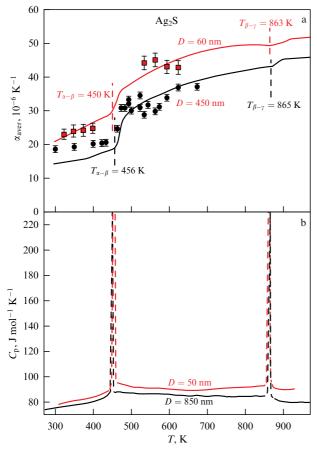
The effect of the Ag<sub>2</sub>S particle size on the position of the photoluminescence peak [179] agrees with the experimental data [218] on the size dependence of the band gap width of silver sulfide, determined from the optical reflectance spectra of Ag<sub>2</sub>S nanopowders with an average particle size of  $\sim 500$ ,  $\sim 90, \sim 60,$  and  $\sim 17$  nm. A quantitative analysis of the experimental data, carried out in the wavelength range from 650–700 to 1400–1500 nm, showed that the gap width  $E_g$  for Ag<sub>2</sub>S powder with a particle size of  $\sim 500$  nm is  $\sim 0.88$  eV and coincides with the value of  $E_g \cong 0.9$  eV for bulk silver sulfide  $\alpha$ -Ag<sub>2</sub>S. For Ag<sub>2</sub>S nanopowders with particle sizes of  $\sim$  90,  $\sim$  60, and  $\sim$  17 nm, the value of  $E_{\rm g}$  was  $\sim$  0.96,  $\sim$  1.21, and  $\sim 1.67$  eV. The presence of a blue shift of the optical absorption band in such rather coarse-particle nanopowders is not entirely clear. The increase in  $E_{\rm g}$  observed in [218] may be due not only to a decrease in the size of the nanoparticles, but also to the peculiarities of the synthesis, which was carried out by precipitation from aqueous solutions of AgNO3 and Na<sub>2</sub>S with a slight excess of sodium sulfide in the presence of sodium acetate. It is known in [232, 233] that, with an excess of sulfur, the formation of S-S bonds is possible, and the resulting  $S_2^{2-}$  and  $S_n^{2-}$  particles will be adsorbed on the  $Ag_2S$  surface, then the  $Ag^+$  ions will react with them, and this can lead to the formation of compounds  $Ag_2S_2$  and  $Ag_2S_n$ , which increase the band gap width of Ag<sub>2</sub>S. The presence of Ag<sub>2</sub>S clusters of the (AgS), type in nanopowders was indirectly confirmed by Raman spectroscopy data [234].

The generation of biexcitons by high-energy photons and multiphoton absorption in  $Ag_2S$  quantum dots was studied in Ref. [235]. Regardless of the size of the  $Ag_2S$  quantum dots, two different lifetimes of  $\sim 10$  and 135–175 ps were obtained, indicating the existence of weakly bound and strongly bound excitons.

In addition to size effects in the electronic and optical properties, size effects in such lattice properties as the coefficient of thermal expansion and heat capacity were found in nanostructured silver sulfide. The influence of small particle size on these properties of Ag<sub>2</sub>S is associated with changes in the type and boundaries of the phonon spectrum. Low-frequency modes that are absent in the spectrum of a bulk crystal appear in the phonon spectrum of small particles [145, 146]. According to Refs [145, 146, 236], waves with a length not exceeding twice the largest particle size D can arise in nanoparticles, i.e.,  $\lambda \leq 2D$ ; therefore, on the side of low-frequency oscillations, the phonon spectrum is limited by a certain minimum frequency  $\omega_{\min} \ge 2\pi c_t/(2D)$ , where  $c_t$  is the propagation velocity of transverse elastic oscillations (the transverse speed of sound). There is no such limitation in bulk crystals. In addition, the phonon spectrum is limited at high frequencies.

In Ref. [237], considering the above limitations of the phonon spectrum, it was shown that the heat capacity and thermal expansion coefficient of a nanocrystalline substance are functions not only of the temperature T, but also of the small particle size D.

The authors of [92, 238] experimentally established that the average thermal expansion coefficient  $\alpha_{\text{aver}}$  and heat capacity  $C_{\text{p}}$  of nanocrystalline silver sulfide in the studied temperature range of 293–970 K are greater than those of coarse-crystalline silver sulfide (Fig. 15). A similar effect, namely, a thermal expansion coefficient  $\alpha$  of a PbS nanofilm



**Figure 15.** Changes in (a) average thermal expansion coefficient  $\alpha_{\rm aver}$  and (b) molar heat capacity  $C_{\rm p}$  of nanocrystalline and coarse-crystalline silver sulfide in temperature range of 293–970 K. For comparison, expansion coefficients  $\alpha_{\rm aver}$  of coarse-crystalline (circles) and nanocrystalline (squares) silver sulfides measured by high-temperature X-ray diffraction are shown. Temperatures  $T_{\alpha-\beta}$  and  $T_{\beta-\gamma}$  of phase transitions  $\alpha$ -Ag<sub>2</sub>S- $\beta$ -Ag<sub>2</sub>S and  $\beta$ -Ag<sub>2</sub>S- $\gamma$ -Ag<sub>2</sub>S are shown by vertical dashed lines. (Figure constructed by the author of the review based on data from Refs [92, 238].)

that is  $\sim 1.7$  times greater than that of bulk coarse-crystalline PbS, was observed by the authors of Ref. [237].

A very interesting result is the effect of the small particle size of silver sulfide with an acanthite structure on the appearance of nonstoichiometry in the metallic sublattice of the sulfide, discovered in [239]. A thorough analysis of the crystal structure of silver sulfide nanopowder with an average particle size of  $43 \pm 6$  nm, performed in [239], showed that the degrees of filling of the metallic sublattice positions by silver atoms are slightly less than 1, being  $\sim 0.96-0.97$ . This means that silver sulfide nanoparticles with a size of less than  $\sim 50$  nm are nonstoichiometric, have a composition of  $\sim$  Ag<sub>1.93</sub>S, and contain vacant sites in the metallic sublattice. Measurements of the positron lifetime in nanocrystalline silver sulfide with a particle size of  $\sim 50$  nm [93] confirmed the presence of vacancies in the metallic sublattice of this compound. Symmetry analysis of the crystal structures of acanthite  $\alpha$ -Ag<sub>2</sub>S and argentite  $\beta$ -Ag<sub>2</sub>S, carried out taking into account the nonstoichiometry of the silver sublattice in these phases, showed that the argentite-acanthite transformation can be considered a disorder-order transition in two sublattices of argentite (non-metallic and metallic), complicated by static displacements of sulfur and silver atoms.

The estimated exciton radius in  $\beta$ -ZnS sulfide is  $\sim 2.5$  nm (see Table 7); the same  $R_{\rm ex}$  value for zinc sulfide is given in

Ref. [240]. Due to the small size of the exciton, size effects on the electronic and optical properties of zinc sulfide can be observed in quantum dots with a diameter of 5 nm or less, which are quite difficult to synthesize. Therefore, most of the studies on nanostructured zinc sulfide are associated with the study of its properties, depending on the morphology, which is very diverse (from nanospheres to nanowires, nanofibers, nanotubes, nanorods, nanobelts, nanoribbons, and films). Indeed, in reviews [4, 5, 7] on nanostructured ZnS, the main focus is on its morphology.

The effect of the size of ZnS nanoparticles (nanocrystallites) on the band gap width was considered in experimental and theoretical papers [241-245]. In Ref. [241], zinc sulfide nanocrystallites with sizes of  $1.8 \pm 0.1$ ,  $2.2 \pm 0.1$ , and  $3.0 \pm 0.2$  nm were synthesized from zinc acetate and thioglycerol dissolved in dimethylformamide using sodium sulfide. Measurements of the UV-vis optical absorption spectra showed that the band gap width  $E_{\rm g}$  of zinc sulfide with nanocrystallites with sizes of 3.0, 2.2, and 1.8 nm increases from 4.3 to 4.55 and 4.85 eV, respectively. Thus, the quantum confinement effect is observed in ZnS nanocrystallites, leading to an increase in the band gap  $E_{\rm g}$  with a decrease in the nanocrystallite size. According to Ref. [242], the value of  $E_{\rm g}$  for a 2-nm zinc sulfide nanocrystallite is 4.5 eV. The experimentally observed blue shift of the absorption band of ZnS nanocrystallites was later confirmed by theoretical calculations [243]. An increase in the band gap width  $E_{\rm g}$ from 3.7 to 3.9 and 4.3 eV with a decrease in the size of ZnS nanoparticles from 7.9 to 5.6 and 5.1 nm was discovered in Ref. [245].

The different changes in  $E_{\rm g}$ , depending on both the size and morphology of zinc sulfide nanotubes, nanowires, and nanosheets, follow from calculations [244]. For example, according to calculations performed in the local density approximation (LDA), the value of  $E_{\rm g}$  in ZnS nanowires with diameters of  $\sim 0.82, \sim 1.19, \sim 1.99,$  and  $\sim 2.66$  nm increases relative to the band gap width  $E_{\rm g-bulk}$  of coarse-crystalline (bulk) ZnS by  $\sim 0.98, \sim 0.78, \sim 0.51,$  and  $\sim 0.26$  eV, respectively. An increase in the diameter of single-layer ZnS nanotubes from 0.79 to 1.15 and 1.88 nm also leads to an increase in  $E_{\rm g}$  of single-layer ZnS nanotubes relative to  $E_{\rm g-bulk}$  by 0.96, 0.86, and 0.80 eV, i.e., by a slightly larger value.

Biexciton emission was discovered in [246] in the photoluminescent properties of ZnS single crystals irradiated with a laser with a wavelength of 325 nm (excitation energy of 3.814 eV). The emission line detected at an energy of 3.791 eV has a biexciton nature, which is confirmed by the superlinear increase in intensity with increasing excitation power. The binding energy of the biexciton and its lifetime in ZnS at a temperature of 12 K are about 9 meV and 52 ps, respectively [246].

In monograph [247], it is indicated that the exciton radius for cadmium sulfide is in the range of  $\sim 2.1-4.5$  nm. According to Ref. [248], for CdS, the exciton radius is 3.0 nm, which agrees with the estimate  $R_{\rm ex}=3$  nm (see Table 7). Considering the value of  $R_{\rm ex}$ , size effects in the electronic and optical properties of cadmium sulfide can be detected when studying nanocrystals and quantum dots with a diameter of 6 nm or less.

The quantum size effect in semiconductors, namely the short-wave shift of the exciton absorption lines of CuCl nanoparticles in a glass matrix, was discovered in Ref. [148].

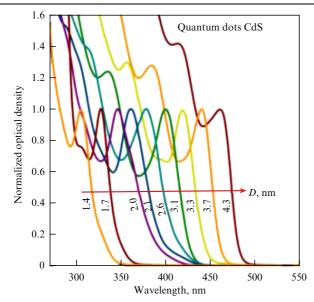
Cadmium sulfide is exactly the semiconductor in which size effects arising in the electronic and optical properties when CdS particles are reduced to the nanoscale have been discovered and explained in detail [186, 187, 249–254]. According to a theoretical model [249] that takes into account the dispersion of nanoparticle sizes, the effective band gap width  $E_{\rm g}$  increases with decreasing nanoparticle radius R:  $E_{\rm g} = E_{\rm g0} + 0.71\pi^2\hbar/(2\mu_{\rm ex}R^2)$ , where  $E_{\rm g0}$  is the optical band gap width in the coarse-crystalline semiconductor. This leads to a blue shift of the absorption band edge. Later, Bruce [186, 253] proposed a formula for estimating the magnitude of the absorption band edge shift depending on the nanoparticle size:  $\Delta E = \pi^2\hbar/(2\mu_{\rm ex}R^2) - 1.78e^2/(\epsilon R)$ .

The density of states transformation and the absorption band blue shift with decreasing CdS nanoparticle size were discovered by L. Bruce [186]. For CdS nanoparticles with sizes from 1.5 to 40 nm, dispersed in a glass matrix, the blue shift increased with decreasing particle size and was 0.8 eV for nanoparticles with a size of 1.5 nm [186]. There were many subsequent publications on size effects in nanostructured CdS; only a few will be mentioned here.

According to Ref. [254], the band gap width  $E_{\rm g}$  corresponding to CdS nanoparticles with sizes of  $\sim 5$ ,  $\sim 2$ , and  $\sim 0.7$  nm is equal to 2.76, 3.57, and 3.85 eV, respectively. A blue shift of the absorption band with decreasing size of CdS nanoparticles was observed in Ref. [255].

In Ref. [256], cadmium sulfide nanocrystals with sizes from 2.0 to 5.3 nm were synthesized from cadmium oxide and sulfur. Measurements of UV-vis optical absorption and photoluminescence spectra revealed a systematic shift of the observed bands to shorter wavelengths with decreasing nanocrystal size. The experimentally observed blue shift of the absorption band and the transformation of the density of states of CAS nanocrystals were confirmed theoretically [243]. A shift of the absorption band to shorter wavelengths (Fig. 16) and, correspondingly, higher energies with decreasing size of CdS quantum dots was discovered in Ref. [257].

Fluorescence of cadmium sulfide quantum dots from 2 to 6 nm in size obtained from colloidal solutions of cadmium



**Figure 16.** Absorption spectra of CdS quantum dots with sizes from 1.4 to 4.3 nm (direction of increasing quantum dot size is shown by the arrow). (Figure constructed by the author of the review based on data from Ref. [257].)

chloride  $CdCl_2$  and sodium sulfide  $Na_2S$  was studied in Refs [258, 259]. The spectra contained a narrow fluorescence peak and a broad long-wavelength peak. The authors of Refs [258, 259] noted the presence of a size effect in the fluorescence spectra. A study of optical absorption and photoluminescence of CdS nanoparticles obtained in a glass matrix [260] revealed a blue shift of the optical absorption band. For CdS nanoparticles 4 and 6 nm in size, the estimated band gap width was  $\sim 2.8$  and  $\sim 2.6$  eV. An increase in the size of CdS nanoparticles was accompanied by a shift of the photoluminescence band to the long-wavelength region, confirming the presence of a size effect.

According to Refs [57–59, 100], the small (less than 10 nm) size of CdS nanoparticles affects their crystal structure by forming a specific disordered hexagonal structure with random (nonperiodic) alternation of close-packed atomic planes. The features of this disordered structure of CdS nanoparticles are described in Section 2.2.

The estimated exciton radius in cubic mercury sulfide  $\beta$ -HgS is 34–38 nm (see Table 7). With such a large value of  $R_{\rm ex}$ , size effects in the electronic and optical properties of  $\beta$ -HgS sulfide can be observed for fairly large particles smaller than 70 nm. However, there are few studies on the quantum size effect in mercury sulfide. Apparently, this is due to the toxicity of mercury compounds.

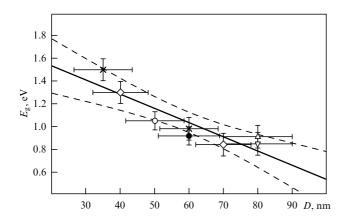
In Ref. [194], nanocrystalline mercury sulfide films with a cubic  $\beta$ -HgS structure and an average crystallite size of 15 nm were synthesized. The band gap width  $E_{\rm g}$ , found from the optical absorption spectra of two different films, was 1.38 and 2.06 eV. According to Ref. [194], the observed noticeable increase in  $E_{\rm g}$  in MO nanofilms compared to  $E_{\rm g-bulk}$  in coarsecrystalline (bulk)  $\beta$ -HgS is due to the quantum size effect.

As is shown in Ref. [194],  $\beta$ -HgS quantum dots with an average size of  $4.0 \pm 0.5$  according to electron microscopy data or  $21 \pm 3$  nm according to X-ray diffraction data have  $E_{\rm g} = 1.21$  eV. Strong absorption in the ultraviolet region at a wavelength of 356 nm, corresponding to  $E_{\rm g} = 3.2$  eV, was found in the UV-vis absorption spectra of  $\beta$ -HgS nanoparticles with an average size of  $\sim 39$  nm [261].

The authors of Ref. [262] synthesized trigonal sulfide  $\alpha$ -HgS nanoparticles with a size of  $\sim 8-9$  nm. Measurements of the optical absorption spectra revealed a blue shift of the absorption band and an increase in the band gap width by 0.1–0.2 eV relative to  $E_{\rm g}$  of coarse-crystalline (bulk)  $\alpha$ -HgS sulfide. Thus, the quantum size effect is also observed for trigonal mercury sulfide  $\alpha$ -HgS.

The exciton diameter in tin sulfide  $\alpha$ -SnS is  $\sim 9-15$  nm (see Table 7); therefore, obvious size effects in the electronic properties can be observed for tin sulfide nanoparticles smaller than 10–15 nm.

In [263], orthorhombic (sp. gr. *Pnma*) tin sulfide  $\alpha$ -SnS nanocrystals with a size of 3.2–4.0 nm were precipitated from a solution of SnCl<sub>2</sub> in triethanolamine with sodium sulfide Na<sub>2</sub>S. Analysis of the UV-Vis optical absorption spectra revealed a strong blue shift, corresponding to the width of the direct band gap of SnS nanocrystals equal to 1.74 eV. Calculation of the optical width of the band gap  $E_{\rm g}$ , depending on the size of the SnS nanocrystals, experimentally confirmed the quantum size effect and an increase in  $E_{\rm g}$  from  $\sim 1.42$  to  $\sim 2.34$  eV with a decrease in the size of the nanoparticles from 10 to 2 nm [263]. According to calculations [205], an increase in the number of SnS layers in model single- and double-layer structures is accompanied by a decrease in the band gap from 2.72 to 1.57 eV, which is a



**Figure 17.** Change in band gap width  $E_{\rm g}$ , in PbS nanofilms with nanoparticles of different sizes D. Dashed curves show 95% confidence interval for determining  $E_{\rm g}$  as a function of particle size D. (Reproduced from [138] with permission from Elsevier.)

manifestation of the size effect. A small increase in  $E_{\rm g}$ , to 1.6–1.7 eV for tin sulfide films with a particle size of  $\sim$  45 nm compared to the band gap width of  $\sim$  1.5 eV for coarse-crystalline (bulk) SnS, discovered in [264, 265], is most likely not due to the size effect, since tin sulfide particles are several times larger than the exciton size. The most likely cause of the observed small increase in  $E_{\rm g}$  [264, 265] may be a change in the phase composition of the films from SnS to Sn<sub>2</sub>S<sub>3</sub>.

The exciton radius in lead sulfide PbS is  $\sim 17-18$  nm (see Table 7), and the exciton diameter does not exceed 36 nm, so quantum size effects can be observed in the electronic and optical properties of nanostructured lead sulfide with particles smaller than  $\sim 35$  nm. The large exciton size and small effective masses of charge carriers (electrons and holes) in PbS nanofilms facilitate charge delocalization and high carrier mobility.

A study of the optical transmission and absorption in PbS nanofilms with different average particle sizes [138] showed that a decrease in the particle size is accompanied by a shift in the absorption band to shorter wavelengths and an increase in  $E_g$ , i.e., a blue shift (Fig. 17).

The average size of PbS particles in nanofilms [138] is approximately twice the exciton size, but the band gap width  $E_{\rm g}$  is noticeably larger than in coarse-crystalline (bulk) PbS sulfide. The reason for this is the noticeable dispersion of the nanoparticle size and the presence of small particles smaller than  $\sim 10-30$  nm in the nanofilms, which cause an increase in the band gap width. A more pronounced size effect was observed in isolated PbS nanoparticles of 18, 12, and 8 nm in size, dispersed in a polymer matrix [266]. For such nanoparticles, the value of  $E_{\rm g}$  was  $\sim 2.4$ ,  $\sim 2.62$ , and  $\sim 2.8$  eV. According to [267], colloidal PbS nanoparticles with a size from 2.4 to 3.0 nm, synthesized in an aqueous heptane microemulsion, have a band gap width of 3.45-3.30 eV. A strong dependence of the band gap width  $E_{\rm g}$  in colloidal quantum dots of PbS and, especially, of PbSe is noted in the review [23] and Ref. [268].

Exciton effects in PbS quantum dots associated with the generation of multiple excitons are described in [269]. At an irradiating photon energy smaller than the band gap width  $E_{\rm g}$ , a quantum dot can absorb more than one photon with the formation of several excitons. The photon energy is too low to create multiple excitons, but sufficient for the emergence of biexcitons in PbS with a lifetime of  $\sim$  80 ps. The generation of

multiple excitons in PbS quantum dots was observed at a photon energy 3.9 times greater than  $E_g$ .

The decrease in the size of PbS nanoparticles in the films led to a change in the crystal structure of lead sulfide [138]. The new cubic (sp. gr.  $Fm\bar{3}m$ ) structure found in PbS nanofilms belongs to the  $D0_3$  structural type. Taking into account the crystal structure of the nanofilm and the degrees of filling of positions 4(b) and 8(c), the formula of the lead sulfide nanofilm can be represented as  $PbS_{0.84}^{4(b)}S_{0.16}^{8(c)} \equiv Pb(S_{0.84} \square_{0.16})^{4(b)}(S_{0.16} \square_{0.84})^{8(c)}$ , where  $\square$  is a structural vacancy.

Regulation of the band gap of semiconductor sulfides allows significantly expanding their application, and the main way of such regulation is to reduce the size of sulfide nanoparticles. Another way is to create composite (hybrid) sulfide nanomaterials like mutual solid solutions and heteronanostructures. A large number of heteronanostructures have been created on the basis of zinc sulfide: isolated ZnSe/ ZnS nanoparticles with a size of ~ 5 nm [270], Mn-doped ZnS:Mn<sup>2+</sup> quantum dots [271], CdSe/ZnS microspheres and MnS/ZnS core/shell nanostructures with high photoluminescence [272, 273], green and red light-emitting CdSe/ZnS/ CdSZnS and CdSe/CdS/ZnS/CdSZnS heteronanostructures [274], and ZnS/Ag<sub>2</sub>S heteronanostructures [275]. Note that CdS is often one of the components of heteronanostructures with zinc sulfide. Cadmium sulfide CdS also forms many heteronanostructures [276–278]. Recently, the production of nanostructured sulfide solid solutions of  $Cu_xPb_{1-x}S$  [279], CdPbS [280], CdZnS [281],  $Ag_xPb_{1-x}S$  [282],  $Cu_2SnS_3$ , Cu<sub>2</sub>ZnSnS<sub>4</sub> [283], and many others, as well as nanostructured spherical ZnS particles [284], has been developed.

Recent publications on the synthesis, properties, and applications of quantum dots of CuS and Cu<sub>2</sub>S [285, 286], Ag<sub>2</sub>S [287, 288], ZnS [289, 290], CdS [291–293], HgS [294, 295], SnS [296, 297], and PbS [298, 299] confirm the relevance of studies of the nanostate of sulfide semiconductors.

### 5. Conclusions

Sulfide nanostructures retain all the advantages of coarsecrystalline semiconductor sulfides, enhancing their applied properties and expanding the scope of application.

Control of the crystal structure and morphology of sulfides, especially nanostructured ones, plays an important role in achieving the desired electronic and lattice properties, since reducing the particle size to the nanoscale can modify the structure, changing its stoichiometry and even symmetry.

The exciton size is a characteristic parameter of the electronic structure, which allows critical evaluation of the observed changes in the properties of nanocrystalline sulfides and relating them to the size of the nanoparticles. The exciton mass of copper, silver, zinc, cadmium, and tin sulfides is  $\sim 0.15-0.25m_0$ , whereas in mercury and lead sulfides the exciton mass is noticeably smaller, being  $\sim 0.02-0.05m_0$ . Due to the small exciton mass and high permittivity, mercury and lead sulfides have the largest excitons, with a diameter of  $\sim 35$  to  $\sim 75$  nm. This allows easy control of the electronic properties of nanostructured mercury and lead sulfides by reducing the size of the nanoparticles to 40-70 nm or less. Various methods for synthesizing HgS and PbS sulfides with nanoparticles of these and smaller sizes are well developed.

The exciton diameter in copper, silver, zinc, cadmium, and tin sulfides is less than 8–10 nm, and size quantum effects in these compounds are experimentally observed for nanoparti-

cles of these and smaller sizes. Due to the difficulty of synthesizing very small nanoparticles, the properties of nanostructured copper, silver, zinc, and tin sulfides are controlled mainly by doping and creating composite nanostructures

The transition from bulk sulfides to nanocrystalline ones leads to transformation of the density of states, an increase in the band gap width, and a blue shift of the absorption spectral band. Another effect of the transition of sulfides to the nanostate is the appearance or increase in their nonstoichiometry, which affects the phonon spectrum and lattice properties

The smallest sulfide nanoparticles (colloidal quantum dots) with a size of less than 5 nm are obtained in colloidal solutions. The colloidal method of synthesis in organic solvents led to a revolution in the production of colloidal quantum dots, which was noted by the 2023 Nobel Prize in Chemistry "for the discovery and synthesis of quantum dots." The laureates of the prize were M.S. Bawendi, L.E. Brus, and our compatriot A.I. Ekimov. In 1981, A.I. Ekimov, together with A.A. Onushchenko, became the first to find that CuCl nanoparticles in a glass matrix absorbed light of different wavelengths, depending on their size. Two years later, L.E. Brus and colleagues found that the optical properties of CdS nanoparticles in a colloidal solution differ from those of coarse-crystalline CdS and change as the nanoparticles grow. M.G. Bawendi and co-authors developed a reproducible method for synthesizing colloidal nearly monodisperse quantum dots of cadmium sulfide, selenide, and telluride with a narrow size distribution in organic solvents such as trioctylphosphine and trioctylphosphine oxide.

An important task is to ensure a homogeneous morphology of nanostructured sulfides, which significantly depends on the production method, composition, and crystal structure. Zinc and lead sulfides have a particularly diverse morphology of nanostructures. In general, the morphology of particles is determined by minimizing their surface energy and kinetic growth conditions. Nanoparticles are usually thermodynamically nonequilibrium, so their diverse morphology is a consequence of metastability, i.e., the system is in one local minimum of free energy or another. Varying the kinetic parameters of synthesis (temperature, pressure, reagent concentration, synthesis duration, supersaturation and pH of solutions, and heating and cooling rates) allows controlling the shape of nanoparticles.

Sulfides are widely used in micro- and optoelectronics to produce elements for various optical instruments and devices in biology and medicine. They are used to create infrared sensors and photodetectors, near and medium infrared lasers, nonvolatile memory devices, ultrasound detectors, thermoelectric converters, and optical switches. These sulfides are used as phosphors for fluorescent devices, light-emitting diodes, and liquid crystal displays and as photocatalysts, biosensors, and antibacterial drugs. Sulfide nanoparticles  $\sim 10$  nm or smaller in size can be used as effective contrast agents in the study of biological tissues.

It can be expected that further development of the synthesis of sulfide nanoparticles with specified sizes and shapes will expand their application in optoelectronics, biology, and medicine.

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