magnetic disorder. The magnetic phasetransition in them can benot only of the second, but also of the first order. Becauseof the presenceof disorder, it is difficult to distinguish thesetwo cases with the use of magnetic data alone; therefore, we analyze in detail the opportunity to apply the well-known Banerjæ criterion in inhomogeneous ferromagnets. This part of the review, just as the examination of the magnetocoloric effed, is, we believe, of geneal physical interest

Since the CMR effect is connected with the transition between the ferromagnetic and paramagnetic phases, we will discuss in detail the differences between manganites experiencing second- and first-order magnetic transitions.

A quantitative analysis of transport phenomena is possible only on the basis of data obtained on singlecrystalline samples. It is also of fundamental import anceto utilize the results of optical studies: without taking them into account, in our opinion, it is simply impossible to discuss such key problems of the physics of manganites as phases eparation and the role of polarons.

The main focus of this review is on the lanthanum manganites La<sub>1ÿ x</sub>Sr<sub>x</sub>Mn O<sub>3</sub>, La<sub>1ÿ x</sub>Ba<sub>x</sub>Mn O<sub>3</sub>, and La<sub>1ÿ x</sub>Ca<sub>x</sub>Mn O<sub>3</sub>, sinceonly for thesecompounds there a sufficiently complete set of experimental data. We, however, do not doubt that the basic regularities, especially observed in the vicinity of the magnetic transition, are identical in all CMR manganites. A discussion of the results of measurement is conducted on the phenomendogical level, since, in our opinion, at presenta consistent microscopic theory of the properties of manganites is absent.

The literature on CMR manganites extremely large, and there is no opportunity to take into account all published data. For this reason, the bibliography does not pretend to be complete; in it, only those studies that were directly used by the authors in this review are indicated.

# 2. Specific features of manganite samples

In experimental work, polycrystalline and single-crystallne samples are, as a rule, used equally with thin films. The properties of thin films strongly depend on the method of preparation, utilized substrate, and thickness of the film; therefore, the data obtained on such samples will be discussed only in certain cases. Polycrystals are most frequently prepared by the method of solid-phasesynthesis. The data on the crystal structure and magnetization are sufficiently reliable, but the temperature dependence of the resistivity of polycrystals depends substantially on the temperature of annealing[27] and is to a considerabledegree determined by the size of crystallites [28]; therefore, for a study (at leasta qualitativ eone) of the mechanisms of electron transfer, such samples are inapplicable.

Reliable data on the nature of transport phenomenain CMR manganiteswereobtained after developingthe production methods of single crystals. They are usually grown by the floating-zone melting method with radiation heating, which is widely used for growing single crystals of oxides [29]. Brief information on the growth method of  $La_{1\bar{y}x}Sr_xMnO_3$  single crystals is given in Ref. [30]; detailed studies of the specific features of growing the different lanthanum manganites are published in Refs [31±34. The single crystals grown have the shape of cylinders with a length on the order of  $60\pm70$ mm with a diameter of about 5 mm. As a rule, they are twinned.

The real composition of samplesof manganitesusually differs from the nominal composition. In the majority of

cases the oxygen content is not equal to 3. Since the radius of the O<sup>2ÿ</sup> ion is great (1.40 A), the excessof oxygen does not mean the presence of oxygen in the interstitials, but rather the appearance of vacancies in the positions of La and Mn in approximately equal quantities [35, 36]. For example, the LaMnO<sub>3‡d</sub> formula in reality implies La<sub>1ÿ e</sub>Mn<sub>1ÿ e</sub>O<sub>3</sub>, where e<sup>^</sup> d=.3 ‡ d† [36]. Because even the production of La<sub>1ÿ x</sub>D<sub>x</sub>MnO<sub>3‡d</sub> polycrystals with d<sup>^</sup> 0 presents ignificant difficulties [37±39]; therefore, in the majority of cases, the magnitude of d is in fact not controlled.

The composition of single-*a*ystalline samplesutilized in different experiments is more poorly controlled than the composition of polycrystals. First, during growth of singlecrystals, manganese evaporates intensely; therefore, it is frequently necessary to add a small excessof this element to the charging feed. Second, the distribution coefficient K  $\hat{C}_s=C_m$ , where  $C_s$  and  $C_m$  are the concentrations of the bivalent element in the solid and liquid phases at the solidification front, can be substantially less than unity. The greatest value, K ^ 0:9, of the distribution coefficient was found in the case of the La±Sr manganites and it weakly dependson the concentration of Sr and on other parameters. If D ^ Baor Ca, then the distribution coefficient is noticeably less(0.7±0.8if D ^ Ba, and 0.6±0.7if D ^ Ca) and substantially depends on the concentration of Ba or Ca in the polycrystalline feedstock, on the gas pressure in the chamber, and on the crystal growth rate [31±33]. As a consequence, the distribution of the elementsover the ingot in the caseof La<sub>1ÿ x</sub>Ba<sub>x</sub>MnO<sub>3</sub>, and especially in the case of La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub>, is strongly inhomogeneous. An attempt at a quantitative analysis of this distribution was made in Ref. [40]. Data about the oxygen content in manganitesingle crystals were not apparently published. There is reason to believe that the vacancies of oxygen are present in all single crystals of manganitesstudied to date.

# 3. Crystal structure

The crystal structure of CMR manganites is called perovskite, which is not completely correct. In the true (cubic) perovskite cell, which contains one formul a unit, manganeseons would be located in the environment of six oxygenions, which form a regular octahedron, and the angle of the Mn±O±Mn bond would be equal to 180. In the lanthanum manganites, the perovskitestructure is always somewhat distorted, since, first, the oxygen octahedra are rotated relative to each other and, second, the octahedra can undergo distortions as a result of the Jahn±Tellereffect. An essential role is also played by the presence of vacancies especially oxygen type ones As a result, the lattice can be orthorhombic, can be rhombohedral, or (in rare cases) can belong to some other crystal system.

To describe the orthorhom bic structure of manganites (Group No. 62 in the International Tables for Crystallography [41]), various settingscan be involved, which differ in the choice of both the origin of coordinates and of coordinate axes. A detailed analysis of the symmetry elements and different settings that are encountered in the literature is given in the survey by Naish [42]. Further, we will consider the Pnmasetting, since it is precisely this setting that is utilized in the International Tables [41]. The orthorhom bic unit cell in this setting contains four formula units.

It was established in Ref. [43] that two orthorhom bic phasescan be realized in lanthanum manganites. The first of



Figure 1. Phase diagram of the La<sub>1 $\bar{y}$ xSr<sub>x</sub>MnO<sub>3</sub> system. Filled symbols correspond to the data for polycrystals taken from Ref. [38]. Open symbolsare the data for singlecrystals from Refs[30,44].</sub>

them (O<sup>0</sup>), with the lattice parameters b= 2 < c < a < b, is characterized by strong Jahn±Teller distortions of oxygen octahedra. The secondphase(O) is called pseudocubic. In this phase, the distortions of octahedra are weaker and b= 2 c a; however, the Mn±O±Mn bond angles, just as in the O<sup>0</sup> phase, differ noticeably from 180.

The rhombohedral lattice of manganiteshas the symmetry R3c. The unit cell of this lattice is described by specifying the lattice parametera and the anglea (see,e.g., Ref. [30]) or (more frequently) as a hexagonalunit cell. In the first case, the unit cell contains two formula units; in the second case six formula units.

Figures 1±4 demonstrate the phase diagrams of La±Sr, La±Ba, and La±Ca manganites for compositions corresponding to the ferromagnetic ground state, i.e., for x from 0.1 to 0.5.

For La<sub>1 $\ddot{y}x$ </sub>Sr<sub>x</sub>MnO<sub>3</sub>, data from Refs[30,38,44]havebeen borrowed: the filled symbols show the data for polycrystals, while the open symbolsshow the data for singlecrystals. The regions of existence of the phase are known sufficiently well; the transition temperatures determined from the experiments on polycrystals, which do not contain vacancies, and on single crystals barely differ.

In the case of La<sub>1 $\bar{y}$  x</sub>Ba<sub>x</sub>MnO<sub>3</sub>, the situation is different The line dividing the regions of existence of the Pnmaand R3c phases is known only partially, and the boundary between the rhombohedral R3c and cubic Pm3m phases, carried out according to Ref. [45], is very condition al, since it is based on measurements performed only at room temperature. According to Ref. [37], the large Jahn±Teller distortion sof the oxygen octahedron at T ^ 300 K occur in the case of x ^ 0:1; at x ^ 0:12, these distortions are considerably weaker. Whether it is possible in this case to separate the regions of existence of the O<sup>0</sup> and O phases or not is unknown.

Notice that, according to Ref. [46], a transition from the rhombohedral to the monoclinic rather than to the orthorhombic phase occursin a singlecrystal of La<sub>0:815</sub>Ba<sub>0:185</sub>MnO<sub>3</sub> at temperature T  $^{1}$  187 K. According to the authors of Refs [47, 48], in the polycrystalline La<sub>0:7</sub>Ba<sub>0:30</sub>MnO<sub>3</sub> the low-temperature orthorhomb ic phase has an Imma symmetry (Group No. 74), in which the distortions of octahedraare absent, and the Imma and R3c phases coexist in the temperatureinterval from 0 to at least300K [48].

The polycrystalline sample of  $La_{1\ddot{y}x}Ba_xMnO_3$  with x ^ 0:12 was investigated at T ^ 300 K in Ref. [37]; it



Figure 2. Phasediagram of the  $La_{1\bar{y}x}Ba_xMnO_3$  system. Solid symbols correspondto the data for the polycrystal staken from the work [37]. Open symbols are the data for single crystals from the studies[45, 49].



Figure 3. (T ±x) phasediagram for the single crystals of La  $_{1\bar{y}x}$ Ba<sub>x</sub>MnO<sub>3</sub>, in which the following crystalline phase are observed:( ) Pnma; (‡) R3c, or ( ) their mixture [49].

contains 97% orthorhombic phase and 3% rhombohedral phase, which indicates a noticeable `smearing out' of the boundary between the Pnma and R3c phases, even in high-quality polycrystals. In Ref. [49], basedon measurements of powders prepared by grinding single crystals, it was established that this smearing is a characteristic property of La<sub>1ŷx</sub>Ba<sub>x</sub>MnO<sub>3</sub>. Figure 3 shows regions in which the Pnma and R3c phases were revealed. It can be seen that the width of the region of coexistence for La<sub>0:75</sub>Ba<sub>0:25</sub>MnO<sub>3</sub> and La<sub>0:80</sub>Ba<sub>0:20</sub>MnO<sub>3</sub> is on the order of 15±20 K, whereasat x  $^{\circ}$  0:14 and 0.15, the width of this region is on the order of 100K.

Figure 4 depicts the phase diagram of  $La_{1\bar{y}x}Ca_xMnO_3$  constructed based on the data taken from Refs [50±53]. The rhombohedral phase exists at temperatures that exceed700K [50]; this part of the diagram will not be considered since the CMR effect is observed at lower temperatures. The main area is occupied by the pseudocubicO phase; the Jahn±Teller phaseO<sup>0</sup> exists only for x < 0:2. Althou gh the symmetry of the lattice doesnot changeupon a magnetic phase transition, a significant decrease (of about 0.13%) is observed in the La<sub>0:75</sub>Ca<sub>0:25</sub>MnO<sub>3</sub> volume upon the transition to the ferromagnetic phase [54]. According to Ref. [55], the relative change in the La<sub>2=3</sub>Ca<sub>1=3</sub>MnO<sub>3</sub> volume upon the magnetic transition is about 0.1%.

The physical properties of CMR materials strongly depend on the synthesis conditions, which determine the



Figure 4. Phasediagram of the La<sub>1 $\tilde{y}x</sub>Ca<sub>x</sub>MnO<sub>3</sub> system. Filled symbols correspond to the data for polycrystals taken from Ref. [50]. Open symbolsare the data for single crystals taken from Refs [51±53].</sub>$ 



Figure 5. Dependences of the lattice parameters on the oxygen content. For d < 0, the data from Ref. [56] for the  $La_{0:80}Ca_{0:20}MnO_{3\ddagger d}$  polycrystals are used; for positive d, the data from Ref. [39] are taken.

stoichiometry of the samplesobtained. As has already been noted, in the majority of cæsesthe oxygen content differs from 3. A changein the oxygen content can lead to a change in the type of crystal structure. For example the manganite of composition  $La_{0:9}Ca_{0:1}MnO_{3\ddagger d}$  has an  $O^0$  structure at room temperature if d<sup>°</sup> 0; a pseudocubic O structure if d<sup>°</sup> 0:042, 0.077, or 0.089, and a rhombohedral R3c structure if d<sup>°</sup> 0:126 and 0.159 [39]. Typical dependences of the parameters of the orthorhombic lattice on d are illustrated in Fig. 5, where the data from Refs [39] and [56] are taken.

Upon substituting part of the lanthanum by strontium, barium, or calcium, the volume per formula unit decreases, and the  $Mn\pmO\pmMn$  bond angle increase $(37\pm3956, 57]$ . An increase in the pressurealso leads to a decrease in the  $Mn\pmO$  bond lengths and an increase in the  $Mn\pmO\pmMn$  bond angle [58, 59].

# 4. Thermodynamiccharacteristics of manganites

# 4.1 Structural transitions

The temperature of a first-order phase transition dependson external pressure P and magnetic field H. The Clapeyron

equationshave the following form

$$\frac{qT}{qP} \stackrel{f}{\sim} \frac{Dv}{DS} \stackrel{f}{\sim} \frac{TDv}{q}; \quad H \stackrel{f}{\sim} const; \qquad .1.1$$

where Dv and DM . H † are the changes in the volume and in the magnetization upon the transition, DS is the changein the entropy, and q is the latent heat of the transition. In all manganites, the temperature of the transition from an orthorhombic (O) to a rhombohedral (R) phasedependson the pressure in a linear manner:  $T_S$ . P<sup>+</sup>,  $T_S$ . O<sup>+</sup>, A<sup>-p<sup>+</sup></sup>P, from which it follows that DS ^ q=T\_S ^ .v^R  $\ddot{y} v^O \dagger = A^{pt}$ . The heat of the transition can also be determined based on the change in  $T_S$  in a magnetic field. If  $T_S < T_C$ , then the changein the magnetization DM ^ M R ÿ M O can be considered to be independent of the magnetic field strength, so that  $T_S T_S.0$ <sup>+</sup>  $B_1H$ , where the coefficient  $B_1$  is given by the right-hand side of Eqn (2). If the structural transition occurs in the paramagnetic region, then DM . H + ^ DwH, where Dwis the changein magnetic susceptibility; therefore, the shift of T<sub>S</sub> upon changing the field from 0 to H is equal to  $B_2H^2$ , where B<sub>2</sub> ^ ÿ T<sub>S</sub>.0†Dw=.2q†.

Let us estimate the quantity q. Althou gh many authors have mentioned the influence of pressureand magnetic field on the Pnma±R3c transition, the data on Dv and DM are scarce,to say nothing of Dw For the  $La_{1\ddot{y}x}Sr_xMnO_3$  single crystals, the necessary information is given in Refs [60, 61]. The values of Dv lie between 0.1 and 0:2 A<sup>3</sup>=Mn; the magnitude of A<sup>.pt</sup> is equal to 5±7 K kbar<sup> $\ddot{y}$ 1</sup>. The obtained values of the heat of the transition are on the order of 0.1± 0.2 kJ mol<sup> $\ddot{y}$ 1</sup>. The values of q determined from data on the shift of the transition temperature in a magnetic field are close to those obtained from data on the pressure dependences.

In La<sub>1ÿx</sub>Ba<sub>x</sub>MnO<sub>3</sub>, the changein the volume of the unit cell upon the Pnma±R3c transition is on the order of 0:01ÿ 0:02 A<sup>3</sup> [49] and, in fact, lies within the limits of the experimental error; therefore, for q we can perform only a plausible estimation. For an La<sub>0:8</sub>Ba<sub>0:2</sub>MnO<sub>3</sub> single crystal, an A<sup>^</sup> ÿ 3 K bar<sup>ÿ 1</sup> value wasfound in papers[62,63], so that q<sup>^</sup> 0:04ÿ 0:08 kJ mol<sup>ÿ 1</sup>. On the other hand, B<sub>1</sub><sup>^</sup> ÿ 0:45  $10^{ÿ}$ <sup>4</sup> K  $0e^{ÿ}$ <sup>1</sup>, DM<sup>^</sup> 4 G [62, 64], from which we find q<sup>^</sup> 0:06 kJ mol<sup>ÿ 1</sup> that is in agreement with the estimate obtained from the data on the T<sub>S</sub>.P†dependence.

The latent heat of the structural transition in the manganitesin question is very small; moreover, in the case of lanthanum±barium crystals, the magnitude of q is a fraction of that in the lanthanum±strontium manganites. Possibly, it is precisely for this reason that the width of the structural transition in La<sub>1ÿ x</sub>Ba<sub>x</sub>MnO<sub>3</sub> is noticeably greater than the analoguesmagnitude in La<sub>1ÿ x</sub>Sr<sub>x</sub>MnO<sub>3</sub>.

#### 4.2 Ferromagnetic±pamagnetic transition

Temperature T<sub>C</sub> of the transition from the ferromagnetic to the paramagnetic state in La<sub>1ÿx</sub>D<sub>x</sub>MnO<sub>3</sub> manganites depends nonlinearly on the concentration of the bivalent ion (see Figs 1, 2, 4). In the case of La<sub>1ÿx</sub>Sr<sub>x</sub>MnO<sub>3</sub>, the Curie temperatures found for polycrystalline and single-crystallne samples practically coincide. If D<sup>\*</sup> Ba, Ca, then the values of T<sub>C</sub> for single crystals below the values for the polycrystals, which, apparently, indicates a noticeably larger defectiveness in the La±Ba and La±Ca single crystals.

In all lanthanum manganites, the Curie temperaturerises upon applying pressure(see, e.g., Refs [65±67]).

In La<sub>1ÿx</sub>Sr<sub>x</sub>MnO<sub>3</sub> and La<sub>1ÿx</sub>Ba<sub>x</sub>MnO<sub>3</sub> manganites, the magnetictransition proceedsas a second-order phasetransition. In La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub>, the situation is different: the transition from the ferromagnetic paramagnetic state is a second-order phasetransition if x < 0:25, whereas thigher concentrations of calcium this transition acquiressigns of the first-order phasetransition. In other words, it is possible to consider that in the phase diagram of La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub>, the concentration x<sub>tr</sub>^0:25 corresponds to a tri-critical point (see paper [53] and referencescited therein).

Since a first-order magnetic transition is observed in  $La_{0:7}Ca_{0:3}MnO_3$ , and a second-ordertransition takes place in  $La_{0:7}Sr_{0:3}MnO_3$ , it can be expected that there is some  $La_{0:7}Ca_{0:3\bar{y}y}Sr_yMnO_3$  composition in which a value of y will correspond to a tri-critical point. It was shown in Ref. [68] that the value y  $^{\circ}$  0:1 corresponds to this point.

As hasalreadybeenindicated, a characteristic property of manganite single crystals is a nonuniform distribution of elementsover the ingot. Since the Curie temperaturestrongly depends on composition, especially at small x, the Curie temperature provesto be a random function of coordinates, which leads to `smearingout' the transition. Let us consider how this smearing can be characterized in the case of a second-orderphasetransition.

Let us assume that in the region with a local Curie temperature  $t_C.r$ ; the local value of the magnetization mr; satisfies the equation of the Landau theory:

where H is the magnetic field, A.r.†^ a%ÿ t<sub>C</sub>.r.†\$and a and B are constants. Let m be a solution to the equation

wherehAi ^ a.T  $\ddot{y}$  T<sub>C</sub><sup>†</sup>. Here, the angular bracketsh:::i mean averaging over the sample, and T<sub>C</sub> ^ ht<sub>C</sub>i. In the experiment, it is in fact T<sub>C</sub> or a quantity close to it that is determined. Expanding mA<sup>†</sup> into a series over the powers of dA ^ A  $\ddot{y}$  hAi, namely

mA<sup>+</sup> m 
$$\ddagger \frac{dm}{dhAi} dA \ddagger \frac{1}{2!} \frac{d^2m}{dhAi^2} . dA \ddagger^2 \ddagger ...;$$

after the calculation of derivatives and averaging, we obtain the following expression for the experimental value of the average magnetization  $M \ mi$ :

M ^ m 
$$\ddagger \frac{hAim .dAt^2}{.A \ddagger 3Bm^2t^3}$$
: .5t

Assuming dA to be small, let us replacem by M on the righthand part of Eqn (5) and substitute the result into Eqn (4) to obtain

$$\frac{H}{M}^{\circ} \text{ hAi \ddagger BM^{2} \ddot{y} \frac{hAi^{3}}{hAi \ddagger 3BM^{2}} \frac{s_{t_{c}}^{2}}{...t_{c} \ddot{y} T^{2}}: \qquad .61$$

Here,  $s_{t_c} \cap h.t_c \ddot{y} T_c \dagger^2 i$  is the standard deviation of the Curie temperature. If the demagnetizing factor N is different from zero, the field H in Eqns (3)±(6) can be considered to be the internal field (H  $\ddot{y}$  4pNM).



Figure 6. Belov±Arrott curves for single crystals of  $La_{0:72}Ba_{0:28}MnO_3$  (open circles, T<sup>3</sup>315K; filled circles, T<sup>T</sup>T<sub>C</sub><sup>3</sup>311K) and  $La_{0:8}Sr_{0:2}MnO_3$  (open triangles, T<sup>3</sup>07K) taken from Ref. [40]. Solid lines are calculations according to equation (6); dashedline is the linear approximation.

The equation obtained is equivalent to the one that was derived many years ago by Shtrikman and Wohlfarth [69]. If the smæring-out of the transition is absent ( $s_{t_c}$  ^ 0), then equation (6) is reduced to the usual equation that is applied in the method of thermodynamic coefficients for determining the Curie temperature (Belov±Arrott curves).But, if  $s_{t_c}$  6^0, this coincidence takes place only at T ^ T<sub>C</sub>, since in this case the last term in equation (6) becomeszero. The conditions for the applicability of formula (6) are obvious: the magnetization M must be small in comparison with the saturation magnetization, and the last term on the right-hand side of formula (6) must be less than the sum of the first two terms.

Let us examinewhat the application of equation (6) gives for the investigation of the inhomogeneousmagneticstate of manganite single crystals. Figure 6 shows Belov±Arrott curves for La<sub>0:72</sub>Ba<sub>0:28</sub>MnO<sub>3</sub> and La<sub>0:8</sub>Sr<sub>0:2</sub>MnO<sub>3</sub> single crystals, taken from Ref. [40]. In the case of La<sub>0:72</sub>Ba<sub>0:28</sub>MnO<sub>3</sub>, the value of H=M is directly proportion al to M<sup>2</sup> at a temperature of 311 K; therefore, T<sub>C</sub> ^ 311 K. The use of equation (6) givess<sub>tc</sub> 3:2 K. For the lanthanum±strontium manganite, T<sub>C</sub> ^ 306 K, and s<sub>tc</sub> 0:8 K. As in the case of the Pnma± R3c structural transition, the magneticinhomogeneity of the lanthanum±strontium crystal proves to be noticeably less than in the case of the lanthanum±barium crystal.

If the magnetic transition is referred to a first-order one, a jump in magnetization must be observed at the Curie temperature. In a magnetic field, T<sub>C</sub> is displaced toward higher temperatures,  $T_C$ .  $H \uparrow T_C$ .  $Q \uparrow B_M H$ , and the magnitude of the jump decreases in a certain critical field H<sub>crit</sub>, the jump in magnetization becomes zero, and for  $H > H_{crit}$ the temperature dependence of the magnetization becomes smooth. Consequently, in the (Tÿ H) plane, we have  $T_C.H_{crit} \dagger$  at the critical point and H  $^{\circ}$  H\_{crit} is Τî T<sub>crit</sub> the endpoint of the line of phasetransitions (critical point). Such a behavior was observed in a study of the Sm<sub>0:55</sub>Sr<sub>0:45</sub>MnO<sub>3</sub> [70] and Sm<sub>0:52</sub>Sr<sub>0:48</sub>MnO<sub>3</sub> polycrystals [71]. For H < 40 kOe, a jump in the magnetization is</p> observed, and magnetic and temperature hysteresestake place, whereas for H > 40 kOe the temperature dependence of the magnetization becomessmooth, similar to the M.T.+ dependencen the vicinity of a second-orderphase transition. Sinceat H ^ 40 kOe the maximum of the heat capacity was revealedat a temperature of approximately 160 K, it can be concluded that in these manganites  $H_{\text{crit}}$  ^ 40 kOe and

 $T_{crit}$  ^ 160 K. In other manganites, no such behavior, apparently, was observed, which can be connected with the high value of the critical field.

Becauseof the inhomogeneity of the manganites, a more or lesssmooth changein the magnetization is observed in the M.T; H ^ const† curve, instead of a jump. The use of the method of thermodynamic coefficients in this caseleads to incomprehensible results. For example, the authors of Ref. [72], who investigated La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub> polycrystals, plotted a curve of the dependence of H=M on M<sup>2</sup> and used the Banerjeecriterion [73], which follows from the Landau theory: if the sign of the derivative q. H = M t=q. M<sup>2</sup> t is positive, the transition is of the secondorder; if the signis negative, the transition is of the first order. It turns out that for manganites with x ^ 0:25 and 0.275 the slope of these curves is always positive; however, their appearane differs significantly from that typical of the second-ordertransitions (seeinsetto Fig. 7). The authors of paper [72] believe that in such casesit is impossible to speak at all about the type of phase transition (therefore, they designated the temperature that corresponds to the point of inflection in the M.T.  $\pm$  curve as T<sub>f</sub> rather than asT<sub>c</sub>).

In our opinion, this conclusionis too categorical, and it is possibleto speakof the type of transition, but it is necessar to refine the rangeof applicability of the Banerjeecriterion in the caseof inhomogeneousferromagnets.For our purposes, it is reasonable to formulate this criterion as follows: if an inequality

$$\frac{qM}{qH}\ddot{y}\frac{M}{H} > 0 \qquad .7$$

is fulfilled, a first-order phase transition is observed; if the reverse inequality is fulfilled, the transition is of the second order.

Let us consider a ferromagnet undergoing the first-order phasetransition. At H ^ 0, the magnetization experiencesa jump at the transition point from M  $\,\hat{}\,$  M  $_{\rm f}$  to zero. Assume that the values of the local Curie temperaturest <sub>C</sub> at H ^ 0 lie in the range from  $T_{C1}.0\dagger$  to  $T_{C2}.0\dagger.$  If the width of the transition region is small,  $dT_{C} \uparrow T_{C2}.0$ †ÿ  $T_{C1}.0$ †5  $T_{C1}$ , then the application of a magneticfield leads to shifts of T<sub>C1</sub> and T<sub>C2</sub> toward larger temperatures with an identical rate. Let us assume that the temperature T of the sample lies between  $T_{C1}$ . 0† and  $T_{C2}$ . 0† both in a zero magnetic field and for H 6<sup>°</sup>0. If the magneticfield is sufficiently weak, it can be assumed that the change in the magnetization at a selected temperature is connected only with the shift of the transition region in the magnetic field. In this case the magnetization of the sample is proportional to the volume of the ferromagnetic phase:

$$M.T; H \uparrow^{A} M_{f} W.t_{C} \dagger dt_{C};$$
.8

where W is the distribution function of the Curie temperatures. Let us assume for simplicity that a uniform (rectangular) distribution is realized: W ^ .dT<sub>C</sub>  $\ddagger^{y^1}$  if T<sub>C1</sub>.0†< t<sub>C</sub> < T<sub>C2</sub>.0†, and W ^ 0 outside this interval. Then, the average value of the Curie temperature sequal to T<sub>C</sub> ^ .T<sub>C2</sub>  $\ddagger$  T<sub>C1</sub> $\ddagger$ 2, and the magnetization m ^ M=M<sub>f</sub> ^  $\Re_{C2}$ .0†ÿ T  $\ddagger$  B<sub>M</sub> H Š=dT<sub>C</sub>, so that

$$\frac{qM}{qH} \ddot{y} \frac{M}{H} \hat{y} \frac{.T_{C2} \ddot{y} T \dagger M_{f}}{H dT_{C}} < 0:$$



Figure 7. Belov $\pm$ Arrott curves in the case of smeared-out first-order magnetic transition (calculation). In the inset: dependenceof H=M on M<sup>2</sup> for the La<sub>0:725</sub>Ca<sub>0:275</sub>MnO<sub>3</sub> polycrystal, taken from Ref. [72].

We see that the Banerjeecriterion indicates the secondrather than the first order of the transition, i.e., the application of this criterion leads to the incorrect conclusion about the type of a phaæ transition.

Figure 7 shows the ratio h=m (where h  $B_M H=dT_C$ ) as a function of m<sup>2</sup> for three values of t ...  $\ddot{y} T_C \dagger=dT_C$ . It may be seen that the theoretical curves have the same shape as the experimental curves at small values of magnetization: M<sup>2</sup> < 2000 emu<sup>2</sup> g<sup> $\ddot{y}$  2</sup> (emu is the electromagneticunit).

A similar result is obtained with the use of a Gaussian distribution function [74]. Since in this case the local Curie temperature falls into the interval  $\mathcal{M}_{C}$   $\ddot{y} \, s_{t_c}$ ;  $T_C \ddagger s_{t_c} \check{S}$  with a probability of 0.68, into the interval with a width of two standard deviations from  $T_C$  with a probability of 0.95, and into the interval with a width of three standard deviations with a probability of 0.997, it is possible to put  $T_{C2}$  equal to  $T_C \ddagger 2s_{t_c}$  or  $T_C \ddagger 3s_{t_c}$ .

Outside the transition region, the smearing-out effect of the transition is weak and is described by equation (6). It can turn out, however, that for  $T > T_{C2}$  the magnetization of the sample grows almost linearly with an increase in the field value, which makes it impossible to determine the type of a phasetransition from magnetic data.

Earlier, we assumed that the shape of the distribution function wasgiven. It follows from formula (8) that the shape of W can be found from the temperature dependence of the magnetization in a weak field, since

An analysis performed in Ref. [74] showed that for singlecrystalline La<sub>0:7</sub>Ca<sub>0:3</sub>MnO<sub>3</sub> the coefficient B<sub>M</sub>  $^{\circ}$  0:8 K kOe<sup>ÿ 1</sup>, T<sub>C</sub>.0† 227 K, M<sub>f</sub>  $^{\circ}$  343 G, and the distribution function can be considered to be Gaussian with a standard deviation s<sub>tc</sub>  $^{\circ}$  7 K. In the La<sub>0:7ÿ x</sub>Pr<sub>x</sub>Ca<sub>0:3</sub>MnO<sub>3</sub> single crystals, the distribution function has a more complex asymmetrical form; therefore, average Curie temperature T<sub>C</sub> is not equal to temperatureT<sub>M</sub>, which corresponds to the point of inflection in the curve of the temperaturedepend@ceof the magnetization [74].

The magnetic inhomogenety of single crystals of lanthanum manganites depends on the type of the bivalent ion. The smallest standard deviation  $s_{t_c}$  of the Curie temperature was found in theLa<sub>1ÿx</sub>Sr<sub>x</sub>MnO<sub>3</sub> singlecrystals; in La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub>, the value of  $s_{t_c}$  is largest. Many authors interpret the disorder in manganitesasa consequence of the difference between the ionic radii of lanthanum and other ions in the A position of the perovskite unit-cell, using for the quantitative estimation the quantity s<sup>2</sup> yir<sub>i</sub><sup>2</sup>ÿ hr<sub>A</sub>i<sup>2</sup>, where y<sub>i</sub> is the fraction of the ith ion with a radius r<sub>i</sub>, and hr<sub>A</sub>i is the averagevalue of the ionic radius. The ionic radii of lanthanum, calcium, strontium, and barium are equal to 1.36, 1.34, 1.44, and 1.61 A, respectively [75]. It can easily be shown that at a given x the value of s<sup>2</sup> is smallestfor La±Ca crystals and is greatestfor La±Ba crystals, which contradicts the above estimations.

The singlecrystalsof manganites are usually grown by the floating-zone melting method. The uniformity of the samples depends this case on the distribution coefficient K  $^{C}s=C_{m}$ , where  $C_{s}$  and  $C_{m}$  are the concentrations of the element A in the solid and liquid phases respectively. Indeed, the distribution coefficient for strontium is close to unity (0:9); for barium, it is noticeably less (0:7ÿ 0:8), and for calcium, K 0:6±0.7(seeRefs[31,33]).

In the case of polycrystals, the width of the magnetic transition region substantially depends on the specific features of the synthes processes.

Since the phase transition from the ferromagnetic to paramagnetic state in the  $La_{0:7}Ca_{0:3}MnO_3$  manganite is a first-order one, it is possible to determine the latent heat of transition for it. Taking into account the results of Refs [54, 55], we will assume that the relative change in the volume in La±Ca manganites at a calcium content close to 0.3 is

0:1%, so that Dv ^ 0:06 A<sup>3</sup>=Mn ^ 0:036 cm<sup>3</sup> mol<sup>ÿ 1</sup>. For the polycrystalline  $La_{0:67}Ca_{0:33}MnO_3$ , it was found by Neumeier et al. [67] that  $qT_C=qP^{-1}6K$  GPa<sup>ÿ 1</sup>, from which we obtain an estimate q<sup>^</sup> 0:49 kJ mol<sup>ÿ 1</sup>. The magnitude of q can also be calculated from magnetic data. As noted above, for a single crystal of La<sub>0:7</sub>Ca<sub>0:3</sub>MnO<sub>3</sub>, the derivative qT\_c=qH ^ 0:8 K kOe $^{\!\!\rm y\,1}\!\!$  , and the jump in the magnetization upon transition is M  $_{\rm f}$  ^ 343 G. With the aid of equation(2), we find DS  $^{15}$  Jmol K<sup> $\ddot{y}$ 1  $^{71}$ </sup> 7:1 Jkg<sup> $\ddot{y}$ 1</sup> K<sup> $\ddot{y}$ 1</sup>, so that q<sup>^</sup> 0:34 kJ mol<sup>ÿ 1</sup>. The latent heat of the magnetic transition in La<sub>1ÿ x</sub>Ca<sub>x</sub>MnO<sub>3</sub> at x closeto 0.3 is several times greater than the value of q for the structural transition Pnma±R3c in the La±Sr and La±Ba manganites, although the magnitude of Dv is noticeably less. It is guite probable that the large magnitude of q in La±Ca manganites is due to magnetostiction.

Both the structural and magnetic transitions manifest themselves well in the temperature dependence of the thermal expansion DI=I. In the case of La<sub>2=3</sub>Ca<sub>1=3</sub>MnO<sub>3</sub>, a sharp peak is observed at T<sup>T</sup>C, whereas the observed feature is very weak in the curve for La<sub>2=3</sub>Sr<sub>1=3</sub>MnO<sub>3</sub> [76]. This difference is apparently caused by the fact that in La<sub>2=3</sub>Ca<sub>1=3</sub>MnO<sub>3</sub> a magnetic first-order transition occurs, and in La<sub>2=3</sub>Sr<sub>1=3</sub>MnO<sub>3</sub> the transition is of the second order.

In the transition region from the ferromagnetic to the paramagnetic state, and also in the region of structural transitions, a strong dependence of DI=I on the magnetic field is observed(see,e.g.,Refs[77,78]).

#### 4.3 Magnetocabric effect

Near a phase transition, the change in the entropy in a magnetic field, DS ^ S.H †ÿ S.0†, reacheslarge values[79, 80]. The magnetocaloric effect (MCE) was experimentally studied mainly in polycrystalline samples of manganites

work with the involvement of single crystals is scarce. A surveyof data obtained before 2007 can be found in Ref. [81]. Since the interestin the magnetocaloic effect is mainly due to the prospects for its use in magnetic refrigerators, the connections between the MCE and other properties of manganites usually draw little attention. Below, some results are given concerned with the inhomogeneties inherent in lanthanum manganites.

We begin with materials in which the magnetic transition runs as the second-order process In the case of an inhomogeneous ferromagnet, the following expression for DS.H † can be obtained within the framework of the Landau theory:

DS.H.† 
$$\ddot{y} = \frac{a}{2} m^2$$
.H.†  $\ddot{y} m^2$ .Q† : .9†

In Ref. [82], it wasnoted that this expressioncan be employed for finding the characteristics of the smearing-outof the phase transition. Assumethat T ^ T<sub>C</sub>. In this case, in a sufficiently strong magnetic field, we have M ^ .H<sub>int</sub>=B<sup>1=3</sup>, where H<sub>int</sub> is the internal field. In order to calculate hm<sup>2</sup>.0<sup>+</sup>i, we should know the distribution function W. The authors of Ref. [82] used a uniform distribution; in our opinion, a normal (Gaussian) distribution is more realistic. After calculating hm<sup>2</sup>.0<sup>+</sup>i, we obtain [83]

DS.H † 
$$\ddot{y} = \frac{A}{2} + \frac{B}{B} + \ddot{y} + \frac{B}{3B} + \ddot{y} + \frac{B}{3B} + \frac{B}{2pB} + \frac{B}{2$$

We retained here only the term that is linear in the standard deviation  $s_{t_{\rm C}}$ . It was shown in Ref. [83] that the value of  $s_{t_{\rm C}}$  determined with the aid of expression(10) for single crystals of La\_{0:72}Ba\_{0:28}MnO\_3 (s\_{t\_{\rm C}} ^ 2:7 \text{ K}) is close to the value(s\_{t\_{\rm C}} ^ 3:2 \text{ K}) found from the analysis of Belov±Arrott curves.

If the magnetic transition is of a first order, then the DS.H † dependenceproves to be substantially different. Let us first calculate DS in the vicinity of an ideally sharp first-order transition, when M ^ mand T<sub>C</sub> ^ t<sub>C</sub>; in addition, we assume that the demagnetizing factor N is equal to zero. The change in the entropy is defined by the Clapeyron equation (2). In weak magnetic fields, the Curie temperature linearly depends on the magnetic field strength: T<sub>C</sub>.H † T<sub>C</sub>.0†‡ B<sub>M</sub>H, and the dependence of DM ^ M<sub>p</sub> ÿ M<sub>f</sub> on H can be ignored (M<sub>p</sub> is the magnetization of the paramagnetic phase). Since in weak fields we have M<sub>p</sub>5 M<sub>f</sub>, it can be assumed that M.T; H † M<sub>f</sub> y<sub>mc</sub>.0†‡ B<sub>M</sub>H ÿ T Š Using the well-known relationship

DS.H 
$$\uparrow^{n} \frac{qM}{qT} H$$
 dH; .1.1 $\uparrow$ 

we find that DS  $^{\circ}$  0 for T < T<sub>C</sub>.0†, and DS  $^{\circ}$  ÿ..M<sub>f</sub>=B<sub>M</sub>†for T > T<sub>C</sub>.0†and H > .T ÿ T<sub>C</sub>.0†=B<sub>M</sub>.

If N 6<sup>°</sup>0, then the situation becomesmore complex. In this case, the uniform ferromagnetic phaseexists for T < T<sub>C</sub>.0<sup>†</sup>‡ B<sub>M</sub>.H ÿ 4pNM<sub>f</sub>†, whereas the uniform paramagnetic phase exists for T > T<sub>C</sub>.0<sup>†</sup>‡ B<sub>M</sub>H. Inside the interval T<sub>C</sub>.0<sup>†</sup>‡ B<sub>M</sub>.H ÿ 4pNM<sub>f</sub>†< T < T<sub>C</sub>.0<sup>†</sup>‡ B<sub>M</sub>H, therefore, the uniform magnetic state is not realized; the ferromagnetic and paramagnetic phase coexist in the temperature interval with the width d<sub>N</sub> ^ 4pNM<sub>f</sub>B<sub>M</sub>.

Using the data given for a single crystal of  $La_{0:7}Ca_{0:3}MnO_3$ , it can easily be shown that the real width of the magnetic transition region is an order of magnitude

greater than  $d_N$ ; therefore, the co-existence of the ferromagnetic and paramagnetic phases revealed in Refs [12, 13] is almost completely caused by the distribution of the Curie temperatures inside the crystal. Assuming that the distribution function W is Gaussian, we obtain in this case with the aid of relationships (8) and (11)[83]:

DS.I; H † 
$$\ddot{y} \frac{M_f}{2B_M}$$
 erf  $\frac{x_0}{2}$   $\ddot{y}$  erf  $\frac{x_H}{2}$  ; .12†

where

$$x_{0} \ ^{\sim} \ \frac{T \ddot{y} \ T_{C} . 0 \dagger}{s_{t_{C}}} \ ; \ \ x_{H} \ ^{\sim} \ \frac{T \ddot{y} \ T_{C} . 0 \dagger \ddot{y} \ \ B_{M} . H \ \ddot{y} \ 4 p M N \ \dagger}{s_{t_{C}}} \ ;$$

and M is determined from the equality  $T \ddot{y} T_{C}.0 \dagger \ddot{y} B_{M}.H \ddot{y} 4pNM \dagger^{\circ} 0$ . As was shown in Ref. [83], the DS.T; H  $^{\circ}$  const $\dagger$  curves calculated via equation (12) agree well with the experimental data for a single crystal of La<sub>0.7</sub>Ca<sub>0.3</sub>MnO<sub>3</sub>.

A simple analysis of Eqn (12) shows that, if N  $^{\circ}$  0, the maximum of the function jDS.T; H  $^{\circ}$  const†j with an increase in the magnetic field is displaced toward higher temperatures at a rate of B<sub>M</sub>=2, and the maximum value of this function grows with an increase in the strength of the magnetic field:

$$jDSj_{max}^{hfH} = \frac{M_{fH}}{2ps_{t_{c}}}$$
:

A shift of the point of the maximum is observed n all known cases; however, the rate of this displacement is not yet published In the La<sub>0.7</sub>Ca<sub>0.3</sub>MnO<sub>3</sub> single crystal that was investigated n Ref. [83] in the fields from 5 to 15 kOe, the shift of the maximum occurs with a rate of about 0.4K kOe<sup>ÿ 1</sup>, which indeed is half the rate of the displacement of the Curie temperature. The maximum value of jDS. It j grows approximately proportionally to the magnetic field value. Substituting M<sub>f</sub> ^ 343G, H ^ 10 kOe, and st<sub>c</sub> ^ 7 K, we obtain jDSj<sub>max</sub> ^ 3:2 J kg<sup>ÿ 1</sup> K<sup>ÿ 1</sup>. The experimental value of jDSj<sub>max</sub> ^ 2:45 J kg<sup>ÿ 1</sup> K<sup>ÿ 1</sup> [83] is somewhat less than the calculated value, which is not surprising, since we did not take into account the presence of a demagnetizing factor.

In strong magnetic fields, the situation becomesmore complex, since the difference in the magnetizations of the ferromagnetic and paramagnetic phases decreases with an increase in H, and at H  $^{\circ}$  H<sub>crit</sub> the jump in the magnetization disappears. Unfortunate ly, near the critical point the magnetocaloric effect has not been studied experimentally to date. Sometheoretical results for this case are given in Ref. [83].

It follows from the above formul as that, in the case of a second-order phase transition, the smearing-out of the transition region leads only to a small decrease in jDSj, whereasin the caseof a first-order transition the magnitude of jDSj<sub>max</sub> is proportional to H=st<sub>c</sub> and, therefore, the role of smearing is considerably more important. Consequently, in the latter case it is possible to significantly affect the magnitude of jDSj by changing  $\boldsymbol{s}_{tc}.$  Thus, it is noted in Ref. [84] that the magnitude of the effect substantially dependson the method of preparing the samples A study of speciallyprepared polycrystals of La±Ca manganites showed that the transition region in a La<sub>0:7</sub>Ca<sub>0:3</sub>MnO<sub>3</sub> sample is considerably narrower than in single crystals of the same composition, and in the field of 20 kOe the magnitude of DS reachesa value of 8 J kg<sup>ÿ1</sup> K<sup>ÿ1</sup>. We obtained above a close value of 7.1 J kg<sup>ÿ1</sup> K<sup>ÿ1</sup> with the aid of the Clapeyron equation.

## 4.4 Heat capacty

Let us examine, first, the region of low temperatures. At T  $^{3}$  3ÿ 10 K, the temperature dependence of the heat capacity can be presented in the following form:

where the first term describesthe electron contribution; the secondterm, the phonon contribution, and the third term, the magnon contribution. In sufficiently strong magnetic fields, the magnon contribution becomesnegligible becauseof the appearance of a gap in the magnon spectrum, which makes it possible to simplify the analysis of experimental curves. In Ref. [85], the measurementson La<sub>1ÿx</sub>Sr<sub>x</sub>MnO<sub>3</sub> singlecrystals were carried out in a field H  $^{\circ}$  90 kOe. It turned out that the coefficient g substantially dependson the strontium concentration: it is very small for x 4 0:1; with increasing x, this coefficient grows to  $5 \text{ mJ K}^{ÿ2} \text{ mol}^{ÿ1}$  at x  $^{\circ}$  0:16, while with a further increase in the strontium concentration the magnitude of g only weakly dependson x and is approximately 4 mJ K  $^{ÿ2}$  mol $^{ÿ1}$ .

Given the coefficient b, it is possible to calculate the Debye temperature  $y_D$ . According to Ref. [85], the magnitude of  $y_D$  in La<sub>1 $\tilde{y}x$ </sub>Sr<sub>x</sub>MnO<sub>3</sub> singlecrystalsgrowsfrom 360to 440 K with an increase n x from 0.1 to 0.3, after which it hardly changes.

The constant of the spin stiffnessD evaluated under the assumption of a gapless magnon spectrum rapidly grows from 50 to 240 meV A<sup>2</sup> with an increase in x from 0.1 to 0.2, after which it is almost independent of the strontium concentration [86].

A systematic study of the heat capacity of lanthanum± barium manganites in the low-temperature region has not, apparently, been conducted. A study of polycrystals of La<sub>0:67</sub>Ba<sub>0:33</sub>MnO<sub>3</sub> [87] showed that in this manganite the magnitude of g is on the order of 5 mJ K<sup> $\ddot{y}$ 2</sup> mol<sup> $\ddot{y}$ 1</sup>, and the Debye temperature is approximately 400 K. The constant of spin stiffn essin Ref. [87] was not determined.

The La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub> single crystals were investigated in Ref. [86]. In contrast to La<sub>1ÿx</sub>Sr<sub>x</sub>MnO<sub>3</sub>, the dependence of g on x has a stepped character: at x  $^{\circ}$  0:22, this coefficient is equal to zero; at x  $^{\circ}$  0:225, the magnitude of g is equal to 4 mJ K<sup>ÿ2</sup> mol<sup>ÿ1</sup>; at x  $^{\circ}$  0:25, g reaches maximum value of 5 mJ K<sup>ÿ2</sup> mol<sup>ÿ1</sup>, after which it somewhat decreases. With an increase in the calcium content, the Debyetemperature grows from 340 to 410 K. The constant of the spin stiffness is 50 meV A<sup>2</sup> for x 4 0:22 and experiences a jump at

 $x^{-}$  0:225; for x 5 0:25, D 140ÿ 150 meV A<sup>2</sup>.

Although at x 1=3 (the so-called optimum doping) the crystal structures of the manganitesexamined are different, and the Curie temperature of the La±Ca crystal is noticeably less than that in the La±Sr and La±Ba manganites, the magnitudes of g and, consequently, the densities of states at the Fermi level prove to be very close.

In the region of the magnetic second order phase transition there is a peak at T  $T_C$  in the temperature dependence of heat capacity (see,e.g., the curves for a La<sub>0.7</sub>Sr<sub>0.3</sub>MnO<sub>3</sub> single crystal in paper [88]). The application of a magnetic field leads to a broadening of the peak and to a decrease in its height; however, no noticeable displacement of the peak under the action of the field is observed. In La<sub>0.7</sub>Ca<sub>0.3</sub>MnO<sub>3</sub>, the magnetic transition proceeds as a first-order process; therefore, the peak is displaced toward higher temperatures. It was found in Ref. [88] that in the La<sub>0.7</sub>Ca<sub>0.3</sub>MnO<sub>3</sub> single crystal this shift is on the order of 40 K in a field of 70 kOe; measurementson the La<sub>0:67</sub>Ca<sub>0:33</sub>MnO<sub>3</sub> polycrystal gave dT<sub>C</sub>=dH<sup>^</sup> 0:8 K kOe<sup>ÿ 1</sup> [76]. Above, we used the last value for evaluating B<sub>M</sub><sup>^</sup> dT<sub>C</sub>=dH, since it is in agreement with our data on the magnetization (seeRef. [53]).

#### 4.5 Magnetic anisotropy

The magnetic anisotropy of the lanthanum manganiteswas studied mainly in thin-fil m samples, in which a large role is played by stressesexisting at the interface between the film and the substrate. Thus, it was established in Ref. [89] that the anisotropy of the epitaxial films of La<sub>0:7</sub>A<sub>0:3</sub>MnO<sub>3</sub>, where A ^ Ca, Sr, Ba, or a vacancy grown on substrates of .LaAlO<sub>3</sub>†<sub>0:3</sub>.Sr<sub>2</sub>TaAlO<sub>6</sub>†<sub>0:7</sub> and SrTiO<sub>3</sub>, can be described with the aid of a single constant of cubic anisotropy  $K_1$ . T  $\dagger$ . The majority of data relates to films on the .LaAlO  $_3$ †<sub>0:3</sub>.Sr<sub>2</sub>TaAlO<sub>6</sub>†<sub>0:7</sub> substrates. The constant K<sub>1</sub> is positive if A ^ Ca or a vacancy, and is negative if A ^ Sr or Ba. At low temperatures,  $K_1$ <sup>1</sup> 13 10<sup>4</sup> erg cm<sup>ÿ3</sup> for lanthanum±calcium films; for a film with vacancies, K1 is somewhat less, and K1 ^  $\ddot{y}$  10<sup>5</sup> erg cm<sup> $\ddot{y}$  3</sup> for lanthanum± barium film. For  $La_{0:7}Sr_{0:3}MnO_3$  films,  $K_1$  is negative,  $jK_1j < 4$  10<sup>4</sup> erg cm<sup>ÿ 3</sup>; moreover, the value of the anisotropy constant for a film on the SrTiO<sub>3</sub> substrate is approximately two times greater than for a film grown on .LaAlO 3<sup>†</sup>0:3. Sr<sub>2</sub>TaAl O<sub>6</sub><sup>†</sup>0:7 substrates.

The dependence of the magnetic anisotropy of polycrystalline La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub> (0:1254 x 4 0:19† on the concentration of a bivalent ion was investigated in Ref. [90]. It turned out that at x ^ 0:125 and 0.15 the anisotropy is uniaxial, whereasthe anisotropy of samples with x ^ 0:175 and 0.19 is cubic. The anisotropy field H<sub>A</sub> is on the order of several kilooersteds; H<sub>A</sub> > 0 for x ^ 0:125 and 0.15, and H<sub>A</sub> < 0 for x ^ 0:175 and 0.19. The anisotropy constant K<sub>1</sub> ^ H<sub>A</sub>M<sub>s</sub>=2, where M<sub>s</sub> is the saturation magnetization (for the constants of uniaxial and cubic anisotropy, we use one and the same designation). Since the magnitude of M<sub>s</sub> is on the order of 500 G, for jK<sub>1</sub>j we obtain an estimate jK<sub>1</sub>j 10<sup>5</sup>± 10<sup>6</sup> erg cm<sup>ÿ 3</sup>. The same estimate is given in Ref. [91] for a La<sub>0:82</sub>Ca<sub>0:18</sub>MnO<sub>3</sub> single crystal.

In singlecrystals of La<sub>0.9</sub>Sr<sub>0.1</sub>MnO<sub>3</sub> and La<sub>0.8</sub>Sr<sub>0.2</sub>MnO<sub>3</sub> the anisotropy is closeto cubic in the low-temperatureregion [92]. For the anisotropy field, the following values were obtained, respectively: H<sub>A</sub> 400 Oe and H<sub>A</sub> 100 Oe, so that for a crystal with 10% Sr we obtain an estimate jK<sub>1</sub>j 10<sup>5</sup> erg cm<sup>ÿ 3</sup>, and for a crystal with 20% Sr, jK<sub>1</sub>j 2:5 10<sup>4</sup> erg cm<sup>ÿ 3</sup>. It can be seen that for La±Sr single crystals the anisotropy constants are close to those obtained with thin films in Ref. [89].

Thus, the lanthanum±strontium manganitesnot only are characterizedby a larger Curie temperature than lanthanum± calcium and lanthanum±barium compounds, but also possess anisotropy constants that are the smallest among the manganitesin question, and which decrease with an increase in the strontium concentration.

## 5. Lattice vibrations. Phononsand magnons

#### 5.1 Propagation of ultrasonic waves

Deviations of the structure of manganites from the ideal perovskite structure are comparatively small; in addition, the single crystals of manganites almost always consist of a large number of twins. The anisotropy of these materials, therefore,

frequently can be satisfactorily described in the cubic approximation. If the propagation of elastic waves is examined, this means the involvement of elastic moduli  $c_{11}$ ,  $c_{12}$ , and  $c_{44}$ .

In Refs [93, 94], the velocity of propagation of the pulses of waves with respective frequencies of 10±30 and about 800 MHz was measured. The temperature dependencesof theseelastic moduli were determined only for single crystals of La<sub>1 $\ddot{v}x$ </sub>Sr<sub>x</sub>MnO<sub>3</sub> with a strontium concentration x 4 0:175. In should be noted that in Ref. [93] data are given for the moduli c<sub>11</sub>, c<sub>33</sub>, c<sub>44</sub>, and c<sub>66</sub> of the rhombohedral lattice at x 0:165 and 0.30. All the ci moduli are characterized by a strong nonmonotonic temperature dependence; the structural transitions, just as the transition from the ferromagnetic to the paramagnetic state, are revealed from the presenceof various singularities in appropriate curves. The magnetic field affects mainly the moduli .c11 ÿ c12=2 and c<sub>44</sub>, which describe transverse vibrations; the bulk modulus  $c_B$  .  $c_{11} \ddagger 2c_{12} \ddagger 3$  changes only a little in the magneticfield.

Studies on the propagation of ultrasonic waves at high frequencies impose stringent requirements on the quality of samples.As was noted above, the manganitesare characterized by a significant inhomogeneity; therefore, experiments with the high-frequency wavesoften prove to be impossible. In these circumstances, the studies of frequencies of the mechanical resonanceseemmore efficient. For example, in Ref. [95] a single-crystalline sample with a nominal composition of La<sub>0:83</sub>Sr<sub>0:17</sub>MnO<sub>3</sub> with a known orientation of crystallographic axes at the frequency of approximately 1 MHz was studied. Since the temperature of the transition from the rhombohedral to the orthorhombic phaseproved to be higher than the Curie temperature, the strontium concentration was in reality somewhat less than x ^ 0:17. The values of elastic moduli obtained in [95] are close to those given in Refs [93, 94].

In many studies, the composite oscillator method was applied, which is basedon the measurement of the resonance frequency and quality factor of the mechanical system consisting of a sample in the shape of a rod and a piezoelectric converter glued to it. This method is suitable for the investigation of not only single-crystilline but also polycrystalline samples. The frequency of longitudinal vibrations excited in the rod is usually on the order of 100 kHz. The velocity of propagation of longitudinal waves determined by Young's modulus E:  $V_1 \cap E=r$ , where r is the density. The Young modulus dependson the orientation of the axis of the cylinder relative to the crystallographic axes. In the case of a cubic crystal [96], we have

$$\frac{1}{E} \hat{\phantom{a}} \frac{c_{11} \ddagger c_{12}}{.c_{11} \ddagger 2c_{12} \ddagger .c_{11} \ddot{y} c_{12} \dagger} \ddagger \frac{1}{c_{44}} \ddot{y} \frac{2}{c_{11} \ddot{y} c_{12}} P.n\dagger;$$
.14

where P.n†  $n_x^2 n_y^2 \ddagger n_x^2 n_z^2 \ddagger n_y^2 n_z^2$ , and n is the unit vector along the axis of the cylinder. In Ref. [93], the following values of elastic moduli have been obtained for a La<sub>0:835</sub>Sr<sub>0:165</sub>MnO<sub>3</sub> single crystal at T ^ 4 K: c<sub>11</sub> ^ 13 10<sup>11</sup> erg cm<sup>ÿ 3</sup>; .c<sub>11</sub>ÿ c<sub>12</sub>†=2 ^ 4:9 10<sup>11</sup> erg cm<sup>ÿ 3</sup>; c<sub>44</sub> ^ 5:9 10<sup>11</sup> erg cm<sup>ÿ 3</sup>, so that E ^ %0085ÿ 0:035P.n†S<sup>1</sup> 10<sup>11</sup> erg cm<sup>ÿ 3</sup>. Since P.n†4 1=3, the second term (depending on n) in formula (14) is an order of magnitude less than the first term. It can be assumed hat this is also correct in the case of other manganite single crystals.



Figure 8. Temperature dependenceof longitudinal sound vibrations in singlecrystalsof lanthanum manganites,taken from Refs[53,97±99].

Figure 8 plots the temperaturedependence**s** f the velocity of longitudinal vibrations in the singlecrystals of lanthanum manganites, which were given in Refs [53, 97±99] Distinct features are quite visible in the curves, which are caused by the structural transition from the low-temperature orthorhom bic to the high-temperature hombohedral phase. The features in the curve for La<sub>0:82</sub>Ca<sub>0:18</sub>MnO<sub>3</sub> are connected with the transitions between two orthorhombic (O<sup>0</sup> and O) phases. The velocity of sound in the O<sup>0</sup> phase with strong Jahn±Teller distortions is less than that in the O structure, where such distortions are absent.

The transition from the ferromagnetic to the paramagnetic state has only a very weak effect on the magnitude of  $V_1$ . I  $\dagger$ , it is more noticeable in the temperature dependences of the velocity of torsional vibrations [100].

The La<sub>0:74</sub>Ca<sub>0:26</sub>MnO<sub>3</sub> crystal represents special case, since at T  $^{\circ}$  T<sub>C</sub> there is a jump in the speedof longitudinal sound in it, which is comparable to the jump upon structural transition; moreover, V<sub>1</sub> is greater in the ferromagnetic state than in the paramagnetic state[53].

The authors of Ref. [101] studied longitudinal vibrations in La<sub>0:67</sub>Ba<sub>0:33</sub>MnO<sub>3</sub> at frequenciesof about 70 kHz with the use of a polycrystalline sample. The Curie temperature T<sub>C</sub> was found to be 340 K. The curve of the temperature dependence for the velocity of sound proved to be similar to those shown in Fig. 8 for the La<sub>0:80</sub>Ba<sub>0:20</sub>MnO<sub>3</sub> and La<sub>0:75</sub>Ba<sub>0:25</sub>MnO<sub>3</sub> single crystals. The structural transition, which was identified as the transition from the R3c phase to the Imma phase,occurred at a temperature of approximately 190K; at the lowest temperatures,the velocity of sound was close to 4 10<sup>5</sup> cm s<sup>ÿ 1</sup>. Apparently, the velocity of sound in La<sub>1ý x</sub>Ba<sub>x</sub>MnO<sub>3</sub> for x 5 0:20 weakly dependson the barium concentration.

Acoustic vibrations were studied in Ref. [102] in a highquality polycrystalline sample of La<sub>0:75</sub>Ca<sub>0:25</sub>MnO<sub>3</sub> at frequenciesof 53±55MHz in a magneticfield of up to 40 kOe. The Curie temperature was close to 200 K. The temperature dependence of the velocity of the longitudinal wavesnear T<sub>C</sub> wassimilar to that presented in Fig. 8 for a La<sub>0:74</sub>Ca<sub>0:26</sub>MnO<sub>3</sub> single crystal. In the magnetic field, the pecularity caused by the magnetic transition is shifted toward higher temperatures at a rate that is somewhat lower than 1 K kOe<sup>ÿ 1</sup>, which is in good agreement with the value of dT<sub>C</sub>=dH  $^{\circ}$  B<sub>M</sub>  $^{\circ}$ 0:8 K kOe<sup>ÿ 1</sup> given in Section 4.2. In the region of phase transitions, peaks of the internal friction  $Q^{\ddot{y}1}$  are observed. In addition, in the  $Q^{\ddot{y}1}$ . It † curves there are other features, at least some of which are caused by the presence of point defects [97].

The structural transitions are characterized by an extremely extensive (giant) temperature hysteresis of the velocity of sound and internal friction. The only exception is the compound  $La_{0:82}Ca_{0:18}MnO_3$ . In the single-crystalline  $La_{0:80}Sr_{0:20}MnO_3$ , the difference between the velocity of sound measured during heating and cooling is noticeable in the rangefrom 50 to 350K, i.e., very far from the temperature of the Pnma±R3c transition, which is 95 K [97, 98]. Consequently the inclusions of the orthorhombic phase in the rhombohedral matrix can exist in a very wide temperature interval, which is connected, apparently, with the proximity of the thermodynamic potentials for these phases.

Using the data presented in Fig. 8, it is possible to estimate the Debye temperature. As is known [103],  $k_By_D^{-1}hu.6p^2Nn=v^{\dagger}$ , where N is the number of unit cells, n is the number of atoms in the unit cell, v is the volume,  $3=u^{-1}.1=V_1$  ‡  $2=V_t$ <sup>†</sup>, and  $V_{1.t^{\dagger}}$  is the velocity of longitudinal (transverse) acoustic waves. For simplicity, we will assume that the unit cell is cubic with a  $^{-3}.3:9$  A, n  $^{-5}$ , the velocity of longitudinal waveswill be considered equal to  $5 - 10^5$  cm s<sup>ÿ 1</sup>, and  $V_t$  equal to the velocity of torsional vibrations 3:4  $- 10^5$  cm s<sup>ÿ 1</sup> in a La<sub>0:80</sub>Sr<sub>0:20</sub>MnO<sub>3</sub> single crystal (see Ref. [100]). Then, u  $^{-3}.8 - 10^5$  cm s<sup>ÿ 1</sup> and the Debye temperature y<sub>D</sub> 500 K, which is in good agreement with the data on the heat capacity.

#### 5.2 Optical phorons

In Refs [104±106], phonons in the undoped manganite LaMnO<sub>3</sub> with the orthorhombic unit cell were investigated in detail. This cell contains 20 atoms; therefore, the number of phonon branchesis equal to 60, three of which are acoustic. At the point G of the Brillouin zone, the phonons are classified according to the irreducible representations of the group  $D_{2h}$  as follows [104, 105]:

where the  $G_A$  and  $G_O$  denote a coustic and optical modes. The mode  $A_u$  is optically inactive, but it can be investigated by the inelastic neutron scattering method.

Basedon an analysis of the spectrum of the optical density of the polycrystalline LaMnO<sub>3</sub>, the authors of Ref. [106] identified 14 types of vibrations. It turned out that the phonon frequencies lie in the range from  $10^2$  to 6:2  $10^2$  cm<sup>ÿ 1</sup> ( $10^{y^2}$  to 8  $10^{y^2}$  eV); their temperature dependenceis weak.

Sucha detailed description rarely provesto be possible in view of the presence of a noticeable decay of vibrations. Thus, only two bands were revealed in the optical spectra of some lanthanum manganites [107], which can be described with the aid of only two phonon frequencies: o<sub>1</sub><sup>^</sup> 647 cm<sup>ÿ</sup> <sup>1</sup> (8:0  $10^{y^2}$  eV) and o<sub>1</sub><sup>^</sup> 531 cm<sup>ÿ</sup> <sup>1</sup> (6:6  $10^{y^2}$  eV). The substitution of calcium, strontium, or barium for part of lanthanum only weakly influences the frequencies of phonons, since the high-frequency phonons in the lanthanum manganites are connected mainly with the vibrations of the oxygen octahed ton. Data on the dependence of phonon frequencies on the wavevector are scarce. Thus, in paper [108] dispersion curves are given (in the cubic approximation) for La\_{0:83}Ca\_{0:17}MnO\_3, La\_{0:80}Ca\_{0:20}MnO\_3, and La\_{0:875}Sr\_{0:125}MnO\_3; in [109], experimental data are given for the rhombohedral La\_{0:80}Sr\_{0:20}MnO\_3 and La\_{0:70}Sr\_{0:30}MnO\_3 manganites in comparison with the results of model calculations.

#### 5.3 Magnons

Spin waves in the manganites have been investigated by many authors. To date, the spectrum of magnons in La<sub>1ÿ x</sub>Sr<sub>x</sub>MnO<sub>3</sub> and La<sub>1ÿ x</sub>Ca<sub>x</sub>MnO<sub>3</sub> is well studied [110±114], whereas the data for La<sub>1ÿ x</sub>Ba<sub>x</sub>MnO<sub>3</sub> are extremely scarce[115, 116]. The processing of experimental data is usually carried out in the cubic approximation.

Near the centerof the Brillouin zone, the spectrumof spin waves is quadratic in terms of the wave vector:  $o.q^+$  D  $\ddagger$  Dq<sup>2</sup>. Since the anisotropy field is 10<sup>3</sup> Oe by an order of magnitude, it can be expected that D has a value of 0.01 $\pm$  0.1 meV, i.e., it is very small. Usually, this indeed is the case, but there are exceptions. For example, according to Ref. [51], for crystals of La<sub>1ÿx</sub>Ca<sub>x</sub>MnO<sub>3</sub> with 0:14 x 4 0:2 at T<sup>^</sup> 15 K the energy gap in the spectrum is approximately 0.2 meV, and in the case of La<sub>0:83</sub>Sr<sub>0:17</sub>MnO<sub>3</sub> the magnitude of the gap is D<sup>^</sup> 0:18 meV [108].

The temperature dependence of the spin stiffness coefficient D in a wide temperature range is described by the expression D.T  $\uparrow^{1}$  D.0 $\uparrow$ .1.ÿ aT <sup>5=2</sup> $\uparrow$ , where a  $^{1}$  const[111].

The constant of spin stiffnesscharacterizes the spectrum of magnons only near the center of the Brillouin zone. Near the boundary of the Brillouin zone, a softening of the spectrum of spin waves occurs. Detailed data for La<sub>0:75</sub>Ca<sub>0:25</sub>MnO<sub>3</sub> and La<sub>0:70</sub>Ca<sub>0:30</sub>MnO<sub>3</sub> were published in paper [113]. The crystal lattice was assumed to be cubic. It turned out that the dependence of the magnon energy on the wave vector can be successfully described within the framework of the Heisenberg model, but it is necessary to take into account not only the exchange interaction between the nearestneighbors (i.e., along the Mn±O±Mn bond), which is described by the exchange integral J<sub>1</sub>, but also the interaction J₄ betweenmanganeseions in the fourth coordination shell (i.e., along Mn $\pm$ O $\pm$ Mn $\pm$ O $\pm$ Mn). The ratio J<sub>4</sub>=J<sub>1</sub> is approximately equal to 0.065 in the case of La<sub>0:75</sub>Ca<sub>0:25</sub>MnO<sub>3</sub> and 0:20 for La<sub>0:70</sub>Ca<sub>0:30</sub>MnO<sub>3</sub>, so that the role of the J₄=J₁ interaction with ions in the fourth coordination shell grows with an increase in the content of calcium.

# Magnetic resonance

Studiesof the ferromagnetic (for T < T<sub>C</sub>) and paramagnetic (for T > T<sub>C</sub>) resonancesin single crystals of La<sub>1ÿx</sub>D<sub>x</sub>MnO<sub>3</sub> havegiven similar results[52,91,92,117±124]In all casesan anisotropy was revealed,which frequently can be considered uniaxial. The value of the g-factor is close to two, and a noticeable temperature dependences observed at that (see, e.g.,Ref. [122]).In the ferromagnetic state, lines cause dby the excitation of magnetostatic waves were revealed besides the basic resonance (EPR) showed that, at a temperature somewhat higher than T<sub>C</sub> in the paramagnetic matrix, inclusions of a ferromagnetic phase exist [92, 120, 121], which is considered by some authors as evidence of the existence of the Griffith phase.

The smallest width DH of the basic resonanceline was observedin La<sub>1yx</sub>Sr<sub>x</sub>MnO<sub>3</sub> singlecrystals. An increase in the content of strontium leadsto a decrease in DH. For example, at the temperature of the transition from the ferromagnetic the paramagnetic state, the width of the resonance line induced by the single crystals investigated in Ref. [117] is equal to 300 Oe at x  $^{\circ}$  0:1, whereasat x  $^{\circ}$  0:3, DH  $^{\circ}$  50 Oe (at a frequency of approximately 9 GHz). Other authors give a somewhat larger value of DH, which is connected, most likely, with the different quality of the investigated samples.

In  $La_{1\bar{y}x}Ba_xMnO_3$  and  $La_{1\bar{y}x}Ca_xMnO_3$ , the resonance line is noticeably wider than in  $La_{1\bar{y}x}Sr_xMnO_3$ .

The temperature dependence of the width of the resonanceline is similar in all the manganites under consideration. The minimum DH is reached near T<sub>C</sub>. In the ferromagnetic region, a decrease in the temperature leads to an increase in DH, which indicates the existence of a magnetic inhomogeneity [118]. In the paramagnetic state, the removal from the point of the magnetic transition also leads to an increase in DH, which occurs according to a linear law: DH. I, t^ DH. I, t^ DH. I, t^ t b. I, ty T<sub>C</sub> t. The coefficient b decreases with increasing content of the doping impurity [117]. For La<sub>0.7</sub>Ba<sub>0:3</sub>MnO<sub>3</sub> and La<sub>0.7</sub>Ca<sub>0:3</sub>MnO<sub>3</sub> single crystals, the same value of b ^ 2:5 Oe K<sup>y 1</sup> was obtained in Ref. [122] that wasfound in Ref. [117] for La<sub>0.7</sub>Sr<sub>0:3</sub>MnO<sub>3</sub>.

The width of the resonance in La  $_{1\bar{y}x}$ Ca<sub>x</sub>MnO<sub>3</sub> single crystals sharply decreases by approximately 180 Oe in the entire investigated range of temperatures (200±600K) when x grows from 0.18 to 0.20, where as the width of the EPR line diminishes insignificantly with a further increase in the content of calcium [122]. This jump, just as the above-considered jumps in the electron contribution to the heat capacity and in the value of spin stiffness, is caused by changes in the electron subsystemand related changes in the exchange interactions.

The patterns in changing the width of the magnetic resonance in the lanthanum manganites are discussed detail by Auslender et al. [124].

The measurements of EPR spectrum can be used for the investigation of structural transitions. In Ref. [52], the EPR signal was measured in the vicinity of structural transitions in  $La_{1\ddot{v}x}Ca_{x}MnO_{3}$  single crystals with x varying from 0.1 to 0.18, and also in La<sub>0:9</sub>Sr<sub>0:1</sub>MnO<sub>3</sub> and La<sub>0:85</sub>Ba<sub>0:15</sub>MnO<sub>3</sub>. The processingof the experimental data under the assumption of the Gaussianfunction fitting the distribution of the concentration of the doping elementmade it possible to determine the standard deviation D of the structural transition temperature. It turned out that with increasingx in the La±Cacrystals the width of the structural transition decreasesfrom 32 K at 0:1 to 14K at x  $^{\circ}$  0:18; in the case of La<sub>0:9</sub>Sr<sub>0:1</sub>MnO<sub>3</sub>, the ХŶ standard deviation D<sup>^</sup> 33 K. These values are in good agreement, for example, with the results of studies [97, 99]. For a  $La_{0:85}Ba_{0:15}MnO_3$  singlecrystal, the value of D does not exceed2 K, which is considerably less than follows, for example, from the results of ultrasonic measurements [98]. The reasons for this divergence are not clear.

In many manganites, the nuclear magnetic resonance (NMR) was studied. This method is one of the most informative in the study of local properties of magnetic compounds, since from the analysis of NMR spectra it is possible to obtain information about the local charge distribution. With the aid of NMR, in particular, reliable data were obtained about the charge-inhomogeneous state of manganites. In this review, we will not describe the results



Figure 9. Temperature dependence of the resistivity of the lanthanum manganites single crystals [138, 140, 144].



**Figure 10.** Magnetoresistance of the lanthanum manganite single crystals in a magnetic field H = 10 kOe [138, 140, 144]. Solid line corresponds to the calculated result for the magnetoresistance of the La<sub>0.70</sub>Ca<sub>0.30</sub>MnO<sub>3</sub> single crystal, obtained by formula (19).

 $La_{1-x}Ba_xMnO_3$  and  $La_{1-x}Ca_xMnO_3$  are noticeably greater than in  $La_{1-x}Sr_xMnO_3$  [86, 138, 139, 45].

In the paramagnetic state, the temperature dependence of resistivity in the majority of cases has a semiconductor nature. It is natural to expect that, in the absence of a magnetic field,  $\rho(T) = \rho_0 \exp(E_0/k_B T)$ . This dependence is indeed observed if a first-order phase transition occurs at the Curie point (see Fig. 9). In a La<sub>0.7</sub>Ca<sub>0.3</sub>MnO<sub>3</sub> single crystal [140], the energy of activation  $E_0 = 78$  meV, and  $\rho_0 = 1.7 \times 10^{-3} \Omega$  cm.

In manganites with a second-order magnetic transition, a simple exponential dependence of resistivity is observed only at a significant distance from  $T_{\rm C}$ , which appears to be connected with an increase in fluctuations of the order parameter with an approach to the transition point. It is known [141] that an increase in fluctuations in ferromagnets with a weak s-d exchange leads to the appearance of singularities in the derivative  $d\rho/dT$  at  $T = T_{\rm C}$ . It can be expected that the same occurs in the manganites, and in them the derivative  $dE_0/dT$  has singularities at the transition point. It is suitable to analyze the local activation energy  $\varepsilon_{\rm a} = d \ln \rho/d(T^{-1})$ , since  $\varepsilon_{\rm a} = E_0 - T(dE_0/dT)$ . An analysis of data on the temperature dependence of the resistivity of different lanthanum manganites in Ref. [138] showed that

$$\varepsilon_{a}(T) = \varepsilon_{a}^{\infty} - \frac{C}{T - T_{a}}, \qquad (16)$$

where C = const, and  $T_a$  is close to the Curie temperature (more precisely, to its average value). For example, the following values were obtained for a single crystal of  $\text{La}_{0.72}\text{Ba}_{0.28}\text{MnO}_3$  ( $T_{\text{C}} = 311$  K):  $\varepsilon_a^{\infty} = 0.072$  eV,  $T_a = 304$  K, and C = 2.33 eV K.

The determination of  $E_0(T)$  from the data for  $\varepsilon_a$  is, generally speaking, impossible, since the pre-exponential factor  $\rho_0$  is unknown. It is possible, however, to take advantage of the fact that, upon moving away from the point of the phase transition, the local activation energy tends to  $\varepsilon_a^{\infty}$ . Considering the expression for  $\varepsilon_a$  through  $E_0$  as the differential equation for  $E_0$  with the boundary condition  $E_0(T \to \infty) = \varepsilon_a^{\infty}$ , it can easily be found that

$$E_0 = \varepsilon_a^{\infty} + \frac{C}{T_a} \left[ 1 + \frac{T}{T_a} \ln \left( 1 - \frac{T_a}{T} \right) \right].$$
(17)

Here,  $T > T_a$ . The calculation of  $E_0$  by this formula showed [138] that  $E_0$  and  $\varepsilon_a$  differ from each other, even at a noticeable distance from the Curie temperature  $[\varepsilon_a(T=400 \text{ K})\approx 0.048 \text{ eV}, \text{ whereas } E_0(T=400 \text{ K})\approx 0.066 \text{ eV}].$ 

The results of evaluations of the resistivity for  $La_{0.85}Sr_{0.15}MnO_3$ ,  $La_{0.7}Ca_{0.3}MnO_3$ ,  $La_{0.72}Ba_{0.28}MnO_3$ , and  $La_{0.75}Sr_{0.25}MnO_3$  via the above-given formulas are shown in Fig. 9 by solid lines. The theoretical curves agree very well with the data from experiments.

Notice that the use of expression (17) makes it possible to adequately describe the temperature dependence of resistivity for La<sub>0.75</sub>Sr<sub>0.25</sub>MnO<sub>3</sub> as well, although in the paramagnetic region  $d\rho/dT > 0$ . The value  $\varepsilon_a^{\infty} = 0.022$  eV proves to be, however, less than  $k_BT$ . To speak about the purely exponential dependence of resistivity on temperature is impossible, but the metallic conductivity also hardly occurs, the more so as the conductivity for  $T > T_C$  is noticeably less than the minimum metallic conductivity  $\sigma_{\min}$ , which in manganites is on the order of 1 m $\Omega^{-1}$  cm<sup>-1</sup> [14, 15]. The behavior of the crystals of La–Sr manganites with  $x \ge 0.25$  resembles the behavior of gapless or narrow-gap semiconductors rather than of metals.

Near the Curie temperature, the resistivity of all manganites sharply decreases as the temperature decreases. Figure 11 illustrates the dependence of  $\ln \rho(T, H = 10 \text{ kOe})$  on the square of the relative magnetization  $m^2(T, H = 10 \text{ kOe})$  for crystals experiencing a magnetic transition of the second



Figure 11. Dependence of the resistivity  $\rho$  measured in a magnetic field H = 10 kOe on the relative magnetization squared  $m^2$  measured in the same field [138, 144].



Figure 9. Temperature dependence of the resistivity of the lanthanum manganitessinglecrystals[138,140,144].



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$$e_{a}.I \uparrow^{a} e_{a}^{1} \ddot{y} \frac{C}{T \ddot{y} T_{a}}; \qquad .16\uparrow$$

where C  $^{\circ}$  const, and T<sub>a</sub> is close to the Curie temperature (more precisely, to its average value). For example, the following values were obtained for a single crystal of La<sub>0:72</sub>Ba<sub>0:28</sub>MnO<sub>3</sub> (T<sub>C</sub>  $^{\circ}$  311 K): e<sup>1</sup><sub>a</sub>  $^{\circ}$  0:072 eV, T<sub>a</sub>  $^{\circ}$  304 K, and C  $^{\circ}$  2:33 eV K.

The determination of  $E_0.T$  † from the data for  $e_a$  is, generally speaking, impossible, since the pre-exponential factor  $r_0$  is unknown. It is possible, however, to take advantage of the fact that, upon moving away from the point of the phase transition, the local activation energy tends to  $e_a^1$ . Considering the expression for  $e_a$  through  $E_0$  as the differential equation for  $E_0$  with the boundary condition  $E_0.T$ ! 1†  $\hat{e}_a^1$ , it can easily be found that

$$E_0 \hat{e}_a^1 \ddagger \frac{C}{T_a} 1 \ddagger \frac{T}{T_a} \ln 1 \ddot{y} \frac{T_a}{T}$$
 : .1.7†

Here, T > T<sub>a</sub>. The calculation of E<sub>0</sub> by this formula showed [138] that E<sub>0</sub> and e<sub>a</sub> differ from each other, even at a noticeable distance from the Curie temperature  $\Re_{a}$ .T<sup>400</sup>K<sup>+</sup> 0:048 eV, whereas E<sub>0</sub>.T<sup>400</sup>K<sup>+</sup> 0:066 eVŠ

The results of evaluations of the resistivity for  $La_{0:85}Sr_{0:15}MnO_3$ ,  $La_{0:7}Ca_{0:3}MnO_3$ ,  $La_{0:72}Ba_{0:28}MnO_3$ , and  $La_{0:75}Sr_{0:25}MnO_3$  via the above-givenformul as are shown in Fig. 9 by solid lines. The theoretical curves agreevery well with the data from experiments.

Notice that the useof expression(17) makesit possibleto adequatelydescribethe temperature dependence f resistivity for La<sub>0:75</sub>Sr<sub>0:25</sub>MnO<sub>3</sub> as well, although in the paramagnetic region dr =dT > 0. The value e<sub>a</sub><sup>1</sup> ^ 0:022 eV proves to be, however, lessthan k<sub>B</sub>T. To speakabout the purely exponential dependence of resistivity on temperature is impossible, but the metallic conductivity also hardly occurs, the more so as the conductivity for T > T<sub>C</sub> is noticeably less than the minimum metallic conductivity s<sub>min</sub>, which in manganitesis on the order of 1 mO<sup>ÿ 1</sup> cm<sup>ÿ 1</sup> [14, 15]. The behavior of the crystals of La±Sr manganites with x 5 0:25 resembles the behavior of gaplessor narrow-gap semiconductors rather than of metals.

Near the Curie temperature, the resistivity of all manganitessharply decrease as the temperature decreases Figure 11 illustrates the dependence of ln r.T; H ^ 10 kOe† on the square of the relative magnetization m<sup>2</sup>.T; H ^ 10 kOe† for crystals experiencing a magnetic transition of the second



Figure 11. Dependence of the resistivity r measured in a magnetic field H  $^{\circ}$  10 kOe on the relative magnetization squared m<sup>2</sup> measured in the samefield [138,144].

$$r \hat{r}_{0} \exp \frac{E_{0} \ddot{y} E_{1} m^{2}}{k_{B} T}$$
; .1.8†

where  $E_0$  dependson temperature as was described above. The data on the  $E_1$ . I. †dependence are scarce apparently, this dependence is weak [138]. Simple estimations show that  $E_1$  is on the order of 0.1 eV.

In the magnetic field, the activation energy decreases so that the magnetoresistance

$$\frac{Dr}{r} \stackrel{\text{r.H}}{\xrightarrow{}} \frac{r.H + \ddot{y} r.0}{r.0}$$

provesto benegative. From formula (18), it follows that

...

In a weak magnetic field, a change in the magnetization is small; therefore, one has

$$\frac{Dr}{r} \ \ \ddot{y} \ \frac{E_1}{k_BT} \ \ m^2.H \ \ \ddot{y} \ \ m^2.0 \ \ :$$

The quadratic dependence of the magnetoresistance on the magnetization has been observed in many materials [141]; for lanthanum±strontium manganites, it was established in Ref. [30]. Detailed data for the  $La_{1\ddot{y}x}Ba_xMnO_3$  single crystals are reported in paper [45].

In manganites with the first-order magnetic transition, formula (18) is valid only in the paramagnetic region, where the magnetoresistances small. Large values of Dr =r are observed near the Curie temperature, or, to be more precise, near its average value. We will assume that the values of the local Curie temperature  $t_{\rm C}.r$ ; lie in the region whose width  $d_{\rm c}$  is much less than  $T_{\rm C}$   $^{\rm h}t_{\rm C}i$ . In the region of the magnetic transition, the resistivity depends on the difference T  $\ddot{\rm y}~t_{\rm C}.r$ ; the noncritical contribution to r is a smooth function of temperature. In the magnetic field, the resistivity depends on H due to changes in the probability of scattering, concentration of charge carriers, etc., and also becaused the shift in the transition temperature in the magnetic field.

The resistivity is, therefore, a functional of T  $\ddot{y}$  t<sub>C</sub>.r.†. r.I.†  $F_{T;H}fT\ddot{y}$  t<sub>C</sub>.r.†g where the subscripts indicate the presence f a noncritical dependence on T and H. The shift in the transition temperature can be considered to be independent of r. We will also assume that the change in the noncritical contribution to the resistivity in the temperature range under consideration can be ignored. Then, the following relationship holds true:

r.I;H<sup>+</sup> F<sub>T<sup>+</sup>T<sub>G</sub>;H<sup>+</sup>0</sub> T ÿ t<sub>C</sub>.r;H<sup>+</sup> 0<sup>+</sup>ÿ DT<sub>C</sub>.H<sup>+</sup>  
^ 
$$r^{\ddot{y}}$$
T ÿ DT<sub>C</sub>.H<sup>+</sup>;H<sup>+</sup>0 ;

where  $DT_C$ . H + B<sub>M</sub> H, and we arrive at a simple formula for the magnetoresistance:

$$\frac{\text{Dr}.\textbf{I}; \textbf{H} \dagger}{r} \wedge \frac{r^{y} \textbf{T} \ddot{y} \text{ DT}_{C}.\textbf{H} \dagger \ddot{y} r.\textbf{I} \dagger}{r.\textbf{I} \dagger}; \qquad .19 \dagger$$

where r. I † r. I; H ^ 0†. It has been shown in Ref. [139] that this formula well describes the dependence of the magnetoresistance of a La<sub>0.7</sub>Ca<sub>0.3</sub>MnO<sub>3</sub> single crystal on temperature in a constant magnetic field. Consequently, in the region of a first-order magnetic transition, the shapeof the Dr. I; H ^ const=r curve is determined by the temperature dependence in a zero field and by the shift in the Curie temperature in the magnetic field.

The assumptions made can easily be understood if we take into account that near  $T_C$  there is a mixture of the metallic ferromagnetic and semiconductor paramagnetic phases in the sample. The application of a magnetic field causes an increase in the volume of the metallic phase as a result of the shift in the transition temperature and, therefore, a decrease in the resistivity. These assumptions mean disregarding the temperature and magnetofield dependences of the resistivity of the phases indicated. Previously, similar approximations were made by us in describing the magnetocal oriceffect.

The above considerations about the origin of the magnetoresistanceof manganitesare phenomerological and say nothing about the nature of the parameters used to describe the dependenceof Dr =r on the temperature and magneticfield value. It can easily be shown, however, that the dependenceof the activation energy on the magnetization is similar to the dependence of the width of the electron energy band. It can, therefore, be assumed hat the crux of the matter lies in the reconstruction of the electron energy-band structure upon changing the state of the magnetic subsystem in the crystal.

## 7.3 Hall effect

In ferromagnetic materials, the Hall effect is determined not only by the induction B of the magnetic field in the sample, but also by the magnetization [142]:

$$r_{H} = R_0 B \ddagger R_s M$$
; .20

wherer  $_{\rm H}$  is the Hall resistivity, and R<sub>0</sub> and R<sub>s</sub> are the normal (ordinary) and anomalous (spontaneous,extraordinary) Hall coefficients. Measurements of the Hall effect are usually conducted using samples in the form of thin plates; therefore, the induction B may be considered to be equal to the external field H.

For T 5 T<sub>C</sub>, the magnetization is almost independent of the field, so that the second term on the right-hand side of formula (20) can be assumed o be equal to  $R_sM_s$ , where  $M_s$  is the saturation magnetization. In this case, the Hall coefficients can easily be determined by plotting the curve of the dependence of  $r_H$  on H, which is usually indeeddone. With an increase in the temperature, the dependence of the magnetization on the field become sessential and the Hall coefficient is conveniently determined from the curves of the dependence of  $r_H$ =H on M=H. In the paramagnetic region, M ^ wH, so that  $r_H$  ^ . $R_0 \ddagger wR_s$ †H ^  $R_{eff}$ H. In this case, it is impossible to determine  $R_0$  and  $R_s$  from the dependence of  $r_H$  on H. However, if  $R_0$  and  $R_s$  weakly (in comparison with w) depend on temperature, then it is possible to find them by constructing the dependence of  $R_{eff}$  on w Experimental Hall-effect data obtained on single-crystalline samples are comparatively scarce The first measurements (seepaper [143]) were carried out on single crystals of La<sub>1ÿ x</sub>Sr<sub>x</sub>MnO<sub>3</sub> (0:184 x 4 0:50).Later on, papers[144±146] appeared,in which single crystals of La±Sr, La±Ba, and La± Ca compounds were investigated; similar data were published in Refs [147, 148] for Nd<sub>1ÿ x</sub>Sr<sub>x</sub>MnO<sub>3</sub> crystals. The main results obtained in these studies are the follow ing.

The anomalous Hall coefficient in all the manganitesis negative. The magnitude of  $R_s$  increase with an approach to the point of the phasetransition, and near  $T_c$  it exceed  $R_0$  by one±twoordersof magnitude, which indicates the presence of strong spin±orbital interaction. In metals, the connection between the anomalous Hall coefficient and resistivity can be presented in the form [149, 150]

$$R_{s}^{2} a_{1}r \ddagger a_{2}r^{2};$$
 .21

wherethe constantsa<sub>1</sub> and a<sub>2</sub> describe the contribution of the asymmetric(skew)scattering and lateral (sidejump) displacement. If the conductivity in the ferromagnetic state is metallic, and r ...T ↑ r .0†‡ AT <sup>2</sup>, then in manganites the dependence of R<sub>s</sub> on r is usually (but not always: seeRef. [143]) close to linear. In the paramagnetic region, the anomalous Hall coefficient remains negative in the vicinity of T<sub>C</sub> and is large in magnitude [138, 144]. But if a semiconductor type conductivity is realized for T < T<sub>C</sub>, as, for example, in La<sub>0:85</sub>Sr<sub>0:15</sub>MnO<sub>3</sub> [144], then the behavior of R<sub>s</sub> with varying r can be described by the formul a obtained in Ref. [145]:

$$R_{s}^{r} r_{xy}^{.0\dagger} \frac{.1 \ddot{y} m^{2} t^{2}}{.1 \ddagger m^{2} t^{2}}; \qquad .22 \ddagger$$

where  $r_{xy}^{,0\dagger}$  const; no data are available for the paramagnetic region.

The temperature behavior of the normal Hall coefficient dependson the level of doping and the type of magnetic phase transition. In the crystals of  $La_{1\ddot{y}x}Sr_xMnO_3$  with  $x > x_c$ , the coefficient R<sub>0</sub> is positive in the ferromagnetic range of temperatures [143, 144]. The dependence of R<sub>0</sub> on the content of Sr in the interval of 0.18 < x < 0.5 is weak. If we assume that R0 ^ 1=eneff, then for the charge-carrier concentration one obtains a value n<sub>eff</sub> 10<sup>22</sup> cm<sup>ÿ 3</sup>, which correspondsto one±two holes per strontium ion; this is considerably greater than would be possible to expect based on the doping level. Obviously, such a small value of R<sub>0</sub> indicates the presence not only of a hole, but also of an electron contribution, which is in agreement with the results of calculations of the band structure given in Section 7.1. In a La<sub>0:72</sub>Ba<sub>0:28</sub>MnO<sub>3</sub> singlecrystal, the normal Hall coefficient is negative for T < 145 K, which indicates a larger role of electrons in this manganite [138]. With the growth in temperature, R<sub>0</sub> increase; near T<sub>C</sub>, this increase becomes sharper. If a semiconductor type of conductivity is realized in the ferromagnetic state, i.e., if  $x < x_c$ , then, at low temperatures, R<sub>0</sub> is less than zero [136±138,144]; however, when approaching the Curie temperature, it can become positive.

An increase in  $R_0$  as  $T ! T_C$  is observed only if the magnetic transition is a second-order one. However, if magnetic transition is a first-order transition, as in the case of  $La_{0:70}Ca_{0:30}MnO_3$ , then the growth of  $R_0$  in the vicinity of  $T_C$  is absent[139,144].

Important information about the mechanisms of conductivity can be obtained from data on the temperature



Figure 12 Hall mobility in the  $La_{0:80}Sr_{0:20}MnO_3$  (T<sub>C</sub><sup>308</sup> K; open symbols, the data from Ref. [144]) and  $La_{0:70}Ca_{0:30}MnO_3$  (T<sub>C</sub>.0<sup>+</sup> 227 K; filled circles, data from Ref. [140]; filled triangles, the data from Ref. [145]) single crystals.

dependenceof the Hall mobility  $m_{H} \ \hat{R}_{0}\text{=r}$ . Figure 12 plots the temperature dependence of  $m_{H}$  for  $La_{0:80}Sr_{0:20}MnO_{3}$  ( $T_{C} \ ^{3}$  308 K) and  $La_{0:70}Ca_{0:30}MnO_{3}$  ( $T_{C}.0\uparrow^{2}$  227 K) single crystals. In  $La_{0:80}Sr_{0:20}MnO_{3}$ , up to the temperature of

200 K, i.e., where r .T  $\uparrow$  r .0 $\uparrow$ ‡ AT <sup>2</sup>, the temperature dependenceof the mobility is typical of a `poor' metal, in which the majority carriers are holes, and the resistivity is causedby the decreasen their mobility. However, above200± 250 K, the mobility is almost independent of T and small in magnitude, m<sub>H</sub> 0:3 cm<sup>2</sup> V<sup>ÿ</sup> <sup>1</sup> s<sup>y</sup> <sup>1</sup>, so that the main contribution to the conductivity comesfrom the chargecarriers with an energycloseto the mobility edge[151], and an increasein resistivity is causedby a decrease the concentration of chargecarriers in the delocalized states.Hence, it follow sthat the metal±semiconductor transition takes place in the temperature interval of 200±250 K, rather than at a temperature that corresponds to the maximum of resistivity, which in our case equal to about 340K.

In a  $La_{0:70}Ca_{0:30}MnO_3$  single crystal, the mobility decreases monotonically, which indicates the metallic nature of conductivity up to the temperature T 220 K, at which a sharp increase in the resistivity begins.

If in the ferromagnetic state the conductivity is that of a semiconductor, then the mobility  $m_H < 0$  and it is small (on the order of  $0.1 \text{ cm}^2 \text{ V}^{\ddot{y}\,1} \text{ s}^{\ddot{y}\,1}$  or less),which, asis known [151], indicates a hopping conductivity.

Data on the Hall effect in the paramagnetic region far from the Curie temperature are extremely scarce. For the La<sub>0:70</sub>Ca<sub>0:30</sub>MnO<sub>3</sub> single crystal at T<sup>400</sup>K, i.e., sufficiently far from the Curie point, the coefficient R<sub>eff</sub> is on the order of  $\ddot{y} 10^{\ddot{y}\,9}$  Om T<sup> $\ddot{y}\,1$ </sup> [139, 140]. The resistivity of the crystal at 400 K is approximately  $10^{\ddot{y}\,2}$  O cm. If we assume that R<sub>eff</sub> at this temperature is completely determined by R<sub>0</sub> and that the anomalous Hall effect can be disregarded, then the following estimate is obtained: m<sub>H</sub>  $\ddot{y} 0.1$  cm<sup>2</sup> V<sup> $\ddot{y}\,1$ </sup> s<sup> $\ddot{y}\,1$ </sup>. The magnitude and the sign of m<sub>H</sub> indicate that for T 4 T<sub>C</sub> a hopping conductivity is realized between the nearestneighbors.

#### 7.4 Thermopowe

The thermal emf S and its dependenceon the temperatureand magnetic field have been studied by many authors. Let us examine first the S.T; H † dependencein manganites with a second-ordermagnetic transition. There are detailed data for

 $La_{1\ddot{v}x}Sr_xMnO_3$  single crystals [144, 152, 153]. In the case of  $La_{0.85}Sr_{0.15}MnO_3$  (x < x<sub>c</sub>), the thermal emf is positive at almost all temperatures, except for T < 50 K. In the S.T.<sup>+</sup> curve, there are two maxima, the first of which is located at 100 K, while the secondlies somewhat higher than the Curie temperature T<sub>C</sub>. The maximum value S<sub>max</sub>, according to Ref. [144], is equal to 56 mV K<sup>ÿ 1</sup>, whereas, according to Ref. [153], Smax ^ 35 mV K<sup>ÿ1</sup>. The difference between two valuesis most likely due to a small difference in the strontium content. In the samples with  $x > x_c$  0:17, the value of the thermal emf is significantly less, the maximum at T  $^{\circ}\,$  T  $_{C}$  is pronounced weakly, and for x > 0.20 it is completely absent. Although the ferromagnetic manganites with the bivalent ions content x < 0.5 are usually considered materials with hole conductivity, in crystals with x ^ 0:20 and 0.25 the sign of S is positive only in the ferromagnetic temperature range, whereas for  $T > T_C$  the thermal emf is negative. In crystals with the strontium content x ^ 0:4, the thermal emf is negative at all temperatures [152]. Notice that the normal Hall coefficient remains in this casepositive [143].

The application of a magnetic field leadsto a decrease jSj, which is most significant near the Curie temperature, wherethe difference DS  $\hat{S}$ . H  $\uparrow$ ÿ S.0 $\uparrow$  is proportional to the squareof the relative magnetization: DS m<sup>2</sup>.

Similar dependences are characteristic of the  $La_{1\bar{y}x}Ba_xMnO_3$  singlecrystals[136±138,154].

If a first-order magnetic transition takes place, as in a  $La_{0:70}Ca_{0:30}MnO_3$  singlecrystal [140], then the dependence of the thermal emf on the temperature and magnetic field is different. In the S.T †curvenear the Curie temperature, there is a sharp maximum, which is absent in the La±Sr and La±Ba crystals with the samelevel of doping. This maximum is not suppressed by a magnetic field, but is only shifted toward larger temperatures, which is caused by the shift in the temperature of the transition in a magnetic field. In the region of transition, the dependence of S on T and H is determined by the co-existence of the low-temperature (It) ferromagnetic and high-temperature (ht) paramagnetic phases; in the region of transition, this dependence well described by a simple formula derived in Ref. [155]:

where r . I; H † is the resistivity of the sample in a magnetic field, and r . I † r . I; H ^ 0†.

In all cases the dependence of S on T in the paramagnetic region is well described by the relationship

$$S^{A} \frac{k_{B}}{e} \frac{E_{a}^{S}}{k_{B}T} \ddagger A^{S} ; \qquad .24 \ddagger$$

where  $k_B = e = 87 \text{ mV K}^{\ddot{y}1}$ ,  $E_a^S$  is the energy of activation for the thermal emf, and  $A^S$  is a constant on the order of unity. For example,in the caseof La<sub>0:70</sub>Ca<sub>0:30</sub>MnO<sub>3</sub>, this activation energy  $E_a^S = 12 \text{ meV}$ ,  $A^S = \ddot{y} = 0.47$  [140]; similar values were obtained for other manganites. It should be emphasized that the value of the activation energy is noticeably lower than  $k_BT$ . This cannot be understood if we assume that the thermal emf and resistivity are caused by electrons in the conduction band or by holes in the valence band. But if we accept in accordance with data on the Hall effect, that in the paramagnetic state a hopping conductivity takes place, then the features indicated obtain a natural explanation, since in this case  $E_a^S$  is cauædby the asymmetry (though small) of the density of states near the Fermi level [156].

The singularities caused by magnetic and structural transitions are also observed in the temperature dependences of the coefficient of thermal conductivity measured in the polycrystalline and single-crystallne samples of La<sub>1ÿ x</sub>Sr<sub>x</sub>MnO<sub>3</sub> [153, 157], and in the La<sub>1ÿ x</sub>Ca<sub>x</sub>MnO<sub>3</sub> polycrystals [158].

# Optical properties

Important information about the electron band structure can be obtained from the study of optical properties; however, the number of articles devoted to the optics of manganites is rather small.

The most detailed data are available for single crystals of  $La_{1\ddot{v}x}Sr_xMnO_3$  [159±163]For the photon energy ho > 6 eV, wide maxima were revealed in the spectral dependence of the dielectric constante, at energiesof approximately 25, 17, and 8 eV. The position of these peaks is practically independent of x [159]. For ho < 6 eV, in curves of the dependence of the optical conductivity sopt on the frequencythere are two wide peaks at energies of approximately 2 and 4.5 eV; in this region, an essential dependenceof spectra on the strontium concentration and on the temperature is observed. If ho is less than 1 eV, then, in the case of undoped LaMnO<sub>3</sub>, the absorption is very small, which indicates the presenceof a direct gap in the electron band spectrum; however, the true absorption edgeis formed, as was noted above, by indirect transitions (seeRef. [162]). The substitution of strontium for part of the lanthanum leads to a shift in the peaks toward smaller energies and to an increase in sopt. When ho < 0.1 eV, the interaction with lattice vibrations prevails in the spectrum.

The interpretation of optical spectrais usually based on the analysis of optical transitions in complexes formed by the manganese on and by surrounding oxygenions, rather than on the basis of existing band calculations. The exception is Ref. [162], where the experimental spectrum of the optical conductivity of a  $La_{0:7}Sr_{0:3}MnO_3$  single crystal is compared with the results of calculations based on the data of Ref. [128].

If x > x<sub>c</sub>, then, for T 5 T<sub>C</sub>, a quasi-Drude increase is observed in the optical conductivity with a decrease in the frequency, which is caused by the presence of metallic conductivity. In the paramagnetic region, the quasi-Drude peak is absent even if the temperature dependence of the resistivity has a characteristic `metallic' form, i.e., dr =dT > 0, as in the case of La<sub>0:6</sub>Sr<sub>0:4</sub>MnO<sub>3</sub> [163]. A decrease in the temperature leads to a gradual increase in the optical conductivity; a distinct quasi-Drude behavior in this single crystal (T<sub>C</sub> ^ 366 K) is observed only for T < T , where T is approximately equal to room temperature. For a single crystal of La<sub>0:825</sub>Sr<sub>0:175</sub>MnO<sub>3</sub> with the Curie temperature T<sub>C</sub> ^ 283 K, the value of T is on the order of 200 K [160]. It can be seen that these data completely agree with the results of our analysis ftransport phenomena.

Similar results were obtained for the  $La_{1\ddot{y}x}Ba_{x}MnO_{3}$  singlecrystals[164].

In the La<sub>0:7</sub>Ca<sub>0:3</sub>MnO<sub>3</sub> manganite, in which the magnetic transition is of the first order, the evolution of the optical spectra has a sharper character. In Ref. [165], results of measurements of the optical spectra of a La<sub>0:7</sub>Ca<sub>0:3</sub>MnO<sub>3</sub> film with a thicknessof 165 nm (T<sub>C</sub> ^ 256 K) are given. For

T 5 255 K, the  $s_{opt}$  o † curveshave the shapecharacteristic of the semiconductor state, whereas lready at T ^ 245 K the shapeof the curve is completely similar to that observed in La<sub>0:6</sub>Sr<sub>0:4</sub>MnO<sub>3</sub> and La<sub>0:825</sub>Sr<sub>0:175</sub>MnO<sub>3</sub> samples at considerably lower temperatures.

The above results show that for ho < 6 eV the optical properties of CMR manganitesstrongly dependon the state of the magnetic subsystem. Near the Curie temperature, this state changes upon applying even a comparatively weak magnetic field, which should lead to a substantial dependenceof light absorption and reflection on H. Such effects, called giant magnetotransmission and magnetoreflection, are indeedobserved and haveprospects for practical applications [166, 167]. Unfortunately, the dependenceof these effects on the parameters of the magnetic subsystem has thus far been studied insufficiently.

Becauseof the presenceof different kinds of inhomogeneities in manganites, metallic and semiconductor regions can coexist in them in a certain temperature range. This coexistencefrequently is considereda `phaseseparation.' The questionarisesabout the ratio of the volumesof these regions and about whether the effect of colossalmagnetoresistace is connected with this `phaseseparation'. In papers[168,164], it was shown that a study of the optical absorption of CMR manganites in the region of interaction of light with the charge carriers makes it possible to give an answer to this question.

The idea consists in a comparison of the temperature dependences of the static conductivity  $s_{dc}$  1=r and of the absorption coefficient a. The studies were carried out on single crystals with  $x < x_c$ . In the paramagnetic region, the  $s_{dc}$ . T + and a. T + dependences have an identical character: upon cooling from room temperature to  $T_{\rm C}$ , the absorption coefficient decrease  $\mathbf{s}$  sin semiconductors, while for T < T<sub>C</sub>, the absorption grows as in conducting materials. Sincein the ferromagnetic state the resistivity of the investigated crystals increasesupon a decrease in T, an increase in the absorption can be explained only by the presence of regions with `metallic' conductivity, which are separated from each other by the semiconductor matrix and therefore do not make a noticeable contribution to  $s_{dc}$ . On the assumption that the conductivity in metallic droplets is, by the order of magnitude, equal to the minimum metallic conductivity smin, which is on the order of 1 mO<sup>y1</sup> cm<sup>y1</sup>, the authors of Ref. [168] estimatedthe relative volume Dv=vof metallic regionsin some weakly doped manganites. It turned out that in La<sub>0.9</sub>Sr<sub>0.1</sub>MnO<sub>3</sub>, even at T<sup>1</sup> 100 K, the volume of the metallic phase is only 0.2% of the volume of the sample; in crystals with a smaller content of bivalent ions, the magnitude of Dv=v is noticeably less.For La<sub>0:85</sub>Ba<sub>0:15</sub>MnO<sub>3</sub>, a value of Dv=v<sup>^</sup> 0:6% wasobtained in a similar mannerat T<sup>^</sup> 190 K [164].Near the Curie temperature, where coloss almagnetoresistanceis observed, the content of the metallic phaseis still less.Henceit follows that the CMR effect is not connected with the appearance of metallic droplets.

An analysisof optical properties madeit possibleto clear up the problem of the existencænd of the role of polaron type carriers in the manganites. In the article by Mostovshchikova [169], the optical properties . reflection coefficients R. <code>a + and absorption coefficientsa. a + tof La \_1y \_x A\_x MnO \_3 singlecrystals with A^ Sr, Ca, and Ba were considered for temperatures T > T<sub>C</sub>. The basic feature of the reflection spectra for the manganites, which contained no more than 15% substitutional ions, is the weak dependence of the reflection coefficients.</code>

cient on energy in the region of ho > 0.1 eV. This form of dependenceis characteristic of materials with the polaron type conductivity, in particular of ferrites [170] and titanates of barium [171]; therefore, an assumption was made that the polarons play the main role in the manganites indicated as well. The use of known theoretical formul as for the electrostatic polarons of a small radius madeit possible with a good accuracyto describe the reflection spectrum and to determine the activation energy of polarons E<sub>a</sub><sup>pol</sup>. The obtained values of Ea<sup>pol</sup> were used for calculating the absorption spectra, which were then compared with the experimental spectra. The calculated a.E t curves for La0:92Ca0:08MnO3 and La<sub>0:85</sub>Ba<sub>0:15</sub>MnO<sub>3</sub> manganites practically coincide with the experimental curves in the region of ho > 0:16 eV. For La<sub>0:93</sub>Sr<sub>0:07</sub>MnO<sub>3</sub>, the difference between the experimental and calculated values of the absorption coefficient is noticeable, and in the case of  $La_{0:85}Sr_{0:15}MnO_3$  (for the La±Sr manganites,xc<sup>^</sup> 0:17), the calculated and experimentala.ot curves diverge significantly. This indicates that in a La<sub>0:85</sub>Sr<sub>0:15</sub>MnO<sub>3</sub> single crystal, whose resistivity is small, the small-radius polarons are not the majority charge carriers.

A comparison of the values of the activation energy for electrical resistivity,  $\mathsf{E}_0$  and  $\mathsf{E}_a^{\text{pol}},$  showed that the radius of the wave function of a polaron is more than the distance to the neighborsthat are nearest to Mn (oxygenions), so that more than one Mn ion participates in the formation of a polaron. Hence it follows that the polarons in manganites are not purely electrostatic, and that exchangeinteraction between the Mn moments makes a certain (most likely small) contribution to  $E_a^{pol}$ . The magnetic moment of such a complex is different both from the Mn<sup>3‡</sup> moment and from the Mn<sup>4‡</sup> moment. The correlation length decreases with an increasein the temperature, which must lead to a decreasein the magneticmoment of the polaron, so that at temperatures that are much higher than T<sub>C</sub>, the moments of Mn ions are independentof one another. Specifically, it is precisely such a behavior of the effective magnetic moment that follows from the analysis of the temperature dependence of the magnetic susceptibility in a number of manganites[172,173].

Let us emphasize that polarons of the type indicated are the majority charge carriers only in the case of weak doping. The reason appears to lie in the fact that an increase in the number of bivalent ions leads to an overlap of the wave functions of separate polarons.

# 9. Conclusions

The variety of crystalline phasesrevealedin manganites of various compositions and the low value of the heat of structural transitions indicate the proximity of the energy of thesephases. This proximity is the natural consequence of the fact that the crystal lattice of manganites is, in essence a relatively weakly distorted perovskite lattice, so that in the very rough approximation it is possible considerit a cubic lattice. The weakness of the distortions of the perovskite structure is supported by the fact that the magnetic anisotropy in many instances well described as cubic.

The proximity of the energy of the crystal structures generatedby the distortion of a perovskite lattice leads to a high sensitivity of the crystal structure of manganites to details of the processes of synthesis and of heat treatment of the samples, and also to small deviations from the stoichiometric composition. As a consequence y different crystal structures have been discovered in manganites: from cubic to

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